Investigating the sensitivity of observed spectral energy distributions to clumpy torus properties in Seyfert galaxies

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ABSTRACT

We present nuclear spectral energy distributions (SEDs) from 1 to 18 µm of a small sample of nearby, nearly face-on and undisturbed Seyfert galaxies without prominent nuclear dust lanes. These nuclear SEDs probe the central ∼35 pc of the galaxies, on average, and include photometric and spectroscopic infrared (IR) data. We use these SEDs, the clumpy torus models of Nenkova et al. and a Bayesian approach to study the sensitivity of different IR wavelengths to the torus parameters. We find that high angular resolution 8–13 µm spectroscopy alone reliably constrains the number of clumps and their optical depth ($N_0$ and $\tau_V$). On the other hand, we need a combination of mid- and near-IR subarcsecond resolution photometry to constrain torus width and inclination, as well as the radial distribution of the clouds ($\sigma$, $\iota$ and $q$). For flat radial profiles ($q = 0, 1$), it is possible to constrain the extent of the mid-IR-emitting dust within the torus ($Y$) when $N$-band spectroscopy is available, in addition to near-IR photometry. Finally, by fitting different combinations of average and individual Seyfert 1 and Seyfert 2 data, we find that, in general, for undisturbed, nearly face-on Seyferts without prominent nuclear dust lanes, the minimum combination of data necessary to reliably constrain all the torus parameters is $J+K+M$-band photometry + $N$-band spectroscopy.

Key words: instrumentation: high angular resolution – galaxies: active – galaxies: nuclei – galaxies: Seyfert – infrared: galaxies.

1 INTRODUCTION

Recent success in explaining several properties of the nuclear infrared (IR) spectral energy distributions (SEDs) of Seyfert galaxies has been gathered with the assumption of a clumpy distribution of dust surrounding active galactic nuclei (AGN). Clumpy torus models (Nenkova, Ivezić & Elitzur 2002; Hönig et al. 2006; Nenkova et al. 2008a,b; Schartmann et al. 2008, 2009; Hönig & Kishimoto 2010; Stalevski et al. 2012) propose that the dust is distributed in clumps, instead of homogeneously filling the torus volume. The latter authors explain in detail how different model parameters control the shape of the synthetic SEDs, and in some cases compare with observations.

From the observers’ point of view, our aim is to reproduce nuclear SEDs of nearby AGN with torus models. In turn, the goal is to look for trends in the torus model parameters with different observational AGN properties such as luminosity, AGN class and presence or not of broad lines (Mason et al. 2006, 2009, 2013; Horst et al. 2008, 2009; Mor, Netzer & Elitzur 2009; Nikutta, Elitzur & Lacy 2009, Ramos Almeida et al. 2009, 2011a,b; Hönig & Kishimoto 2010, Alonso-Herrero et al. 2011, 2012, 2013, Lira et al. 2013).

In a series of papers, we performed detailed fits to the nuclear near- and mid-IR (NIR and MIR) emission of Seyfert galaxies using the clumpy torus models of Nenkova et al. (2008a,b) and a Bayesian approach (see below). In the first two works of the series (Ramos Almeida et al. 2009, 2011a, hereafter RA2009 and RA2011, respectively), we only fitted subarcsecond resolution photometry...
from 1 to 20 µm. The main results of these studies are as follows. (1) The NIR/MIR emission of Seyfert galaxies can be reproduced with small torus sizes, ranging from 1 to 6 pc. (2) Seyfert 2 (Sy2) tori generally have larger covering factors and smaller escape probabilities than those of Seyfert 1 (Sy1) galaxies. (3) The classification of a Seyfert galaxy as a type 1 or type 2 might depend not only on torus inclination, but also on the intrinsic properties or that torus.

In the third paper of the series (Alonso-Herrero et al. 2011, hereafter AH2011), we combined ground-based subarcsecond MIR spectroscopy and NIR/MIR photometry of 13 Seyfert galaxies at a median distance of 31 Mpc. In general, the photometry+spectroscopy fits resulted in more constrained torus widths (σ), torus radial extents (Y) and viewing angles (i). From the study presented in AH2011, we learnt that clumpy torus models provide good fits only for those Seyferts with low to moderate amounts of foreground extinction (AV ≲ 5–10 mag). The 8–13 µm spectra of galaxies with very deep silicate features, normally hosted in highly inclined or interacting galaxies and/or showing prominent dust lanes, cannot be reliably reproduced with clumpy models (Levenson et al. 2007). The latter result was confirmed in the recent analysis of ground-based MIR spectra of nearby Seyferts presented in González-Martín et al. (2013). The host galaxies of the Seyfert nuclei with the largest nuclear 9.7 µm apparent optical depths show nuclear dust lanes at optical wavelengths, are highly inclined and/or are part of a merger. The dust associated with these galaxy properties is likely contributing to the deep silicate features observed. A similar conclusion was reached by Goulding et al. (2012) for a sample of Compton-thick Seyfert galaxies using data from the Spitzer Infrared Spectrograph (IRS) and probing kpc scales.

The previous works are useful for testing the models and constraining the torus parameters of AGN, considering that with current instrumentation we cannot obtain direct observations of the torus itself. The problem is that, when fitting SEDs with torus models, we normally use the IR data available in the literature for our targets. This implies that, for different objects of a given sample, the data were obtained with distinct filters and instruments, and the sampling of the SEDs may not be the same. Distinct SEDs of the same target can provide different fitting results, and for that reason, it is important to analyse how IR observations at various wavelengths constrain the torus model parameters. This analysis is important because, to isolate as much as possible the torus emission, subarcsecond resolution data from ground-based 8–10 m class telescopes or the Hubble Space Telescope (HST) are necessary, and their over-subscription factors are very high.

BayesClumpy (Asensio Ramos & Ramos Almeida 2009) is a computer program that can be used for the fast synthesis of SEDs emerging from the clumpy dusty torus models of Nenkova. These fast synthesis capabilities are used in a Bayesian scheme for carrying out inference over the model parameters for observed SEDs. In the latest version of BayesClumpy,1 the inference can be done either using neural network interpolation (as described in Asensio Ramos & Ramos Almeida 2009) or multilinear interpolation in the full data base. After running different tests, we recommend the latter interpolation to the users for fitting the clumpy torus models of Nenkova. In addition, we have recently incorporated Bayesian adaptive exploitation (BAE) in BayesClumpy to predict which photometric filter is needed to maximize the expected utility (Asensio Ramos & Ramos Almeida 2013). In other words, we used the information already present in the data and clumpy torus models to evaluate the optimum next observation that maximizes the constraining power of the newly observed photometric point.

Here we use BAE to study the SED sensitivity (including photometric and spectroscopic IR data) to the six clumpy torus parameters of Nenkova. We also propose the optimum filter set required to constrain these parameters, using average and individual Sy1 and Sy2 SEDs of a small sample of nearly face-on, undisturbed Seyfert galaxies without prominent nuclear dust lanes. Although the Nenkova models are generic and widely used by the community, we note that some of the parameters that describe them might vary from model to model (Hönig et al. 2006; Schartmann et al. 2008; Stalevsksi et al. 2012). Besides, distinct models often treat differently the radiative transfer problem. In fact, a given SED can be reproduced with a different set of two distinct model parameters. Thus, the results from SED fitting with torus models should be interpreted in the context of the chosen model only, as the resulting parameters are just a possible description of the geometry and properties of the torus, provided that the data are dominated by torus emission. See Hoenig (2013) for further discussion on SED fitting caveats. In summary, the results presented here are only valid, in principle, for the clumpy torus models of Nenkova. Throughout this paper, we assume a cosmology with H0 = 70 km s⁻¹ Mpc⁻¹, Ωm = 0.27 and ΩΛ = 0.73.

2 SAMPLE SELECTION

This work aims to study the sensitivity of different IR wavelengths to the clumpy torus parameters of Nenkova. We then need a sample of nearby Seyfert galaxies whose SEDs and spectra can be accurately reproduced with these models. Thus, we selected three Sy1 and three Sy2 galaxies from AH2011 and González-Martín et al. (2013) hosted in nearly face-on galaxies (inclination ≲ 45°) without prominent nuclear dust lanes and which are not part of merging systems.2 The galaxies are NGC 1068, NGC 3081 and NGC 5643 (Sy2s) and NGC 1365, NGC 3227 and NGC 4151 (Sy1s) and they are at distances smaller than 19 Mpc, with the exception of NGC 3081 (see Table 1). This implies that, at the average resolution of ground-based N-band observations (~0.3–0.4 arcsec), we are probing the central 20–30 pc (~55 arcsec for NGC 3081).

Table 1. Basic galaxy data. Inclination angle = 0° corresponds to face-on galaxies.

<table>
<thead>
<tr>
<th>Galaxy</th>
<th>Seyfert type</th>
<th>Distance (Mpc)</th>
<th>Scale (pc arcsec⁻¹)</th>
<th>Inclination (deg)</th>
</tr>
</thead>
<tbody>
<tr>
<td>NGC 1365</td>
<td>1.8</td>
<td>18.6 (a)</td>
<td>90</td>
<td>46 (g)</td>
</tr>
<tr>
<td>NGC 3227</td>
<td>1.5</td>
<td>17.0 (b)</td>
<td>82</td>
<td>46 (h)</td>
</tr>
<tr>
<td>NGC 4151</td>
<td>1.5</td>
<td>13.0 (c)</td>
<td>63</td>
<td>31 (h)</td>
</tr>
<tr>
<td>NGC 1068</td>
<td>2</td>
<td>14.4 (d)</td>
<td>70</td>
<td>28 (h)</td>
</tr>
<tr>
<td>NGC 3081</td>
<td>2</td>
<td>32.5 (e)</td>
<td>138</td>
<td>31 (i)</td>
</tr>
<tr>
<td>NGC 5643</td>
<td>2</td>
<td>16.9 (f)</td>
<td>82</td>
<td>29 (j)</td>
</tr>
</tbody>
</table>

References: (a) Madore et al. (1998); (b) Garcia (1993); (c) Radomski et al. (2003); (d) Bland-Hawthorn et al. (1997); (e) Tully (1988); (f) González-Martín et al. (2013); (g) Jorsater & van Moorsel (1995); (h) Hunt & Giovanardi (1992); (i) Buta & Purcell (1998); (j) Jungwiert, Combes & Axon (1997).

1 https://github.com/aasensio/bayescumulus

2 The only exception is the Sy1.5 NGC 3227, which is interacting with its companion galaxy NGC 3226 (Mundell et al. 2004). However, there are no signs of morphological disturbance in its nuclear region, and the apparent depth of the 9.7 µm silicate feature is low (τ9.7 < 0.4; González-Martín et al. 2013).
3 OBSERVATIONS

3.1 Photometry

The NIR and MIR nuclear fluxes of the six galaxies considered here are reported in Tables 2 and 3. For the galaxies NGC 1068, NGC 3081, NGC 3227 and NGC 4151, the data are the same as reported in AH2011 and RA2011, and for NGC 1365, in Alonso-Herrero et al. (2012), with the following exceptions.

In the case of NGC 3227, we discarded the 8.99 μm VISIR/VLT flux from Höning et al. (2010) and the 11.2 μm MICHELLE/Gemini North flux from RA2009 because they appear contaminated by [Ar III] and polycyclic aromatic hydrocarbon (PAH) 11.3 μm emission, respectively. In the NIR, we considered the L- and M-band fluxes of NGC 3227 and NGC 4151 (Ward et al. 1987a) as upper limits, because of the limited angular resolution of the images (from NSFCam/IRTF in the case of NGC 1068, and from NSFCam/IRTF (L) and IRCam3/UKIRT (M) for NGC 3227 and NGC 4151).

The Seyfert 2 galaxy NGC 5643 was observed in 2012 May with the MIR camera/spectrograph T-ReCS (Telesco et al. 1998) on the Gemini-South telescope. The narrow Qa filter was employed (λ_c = 18.3 μm, Δλ = 1.5 μm) and the angular resolution was 0.5 arcsec at 18.3 μm, as measured from the observed point-spread-function (PSF) star. The data were reduced using the RedCan pipeline (González-Martín et al. 2013), and the nuclear flux obtained from scaling the flux of the PSF star to the peak of galaxy emission, as described in RA2011. The nuclear Q-band flux of NGC 5643, together with an 11.88 μm flux from Höning et al. (2010) obtained with VISIR/VLT (Lagage et al. 2004), is reported in Table 3. The galaxy was also observed with T-ReCS using the narrow Si-2 filter (λ_c = 8.74 μm, Δλ = 0.78 μm), but we did not include the Si-2 nuclear flux in the SED because it does not match the SED shape of the >10 μm points and the spectrum, as the flux calibration in this filter is uncertain.3

In the NIR, NGC 5643 was observed with SOFI/New Technology Telescope (NTT) in 1999 June in the Ks filter with a seeing of full width at half-maximum = 1.6 arcsec. See Grosbol, Patsis & Pompei (2004) for further details on the SOFI observations. We performed aperture photometry on the Ks-band image of the galaxy in an aperture of 1 arcsec radius, and considered the resulting flux as an upper limit because of the image resolution (see Table 2). Finally, we also included the ISOCAM/ISO 6 μm flux reported in Lutz et al. (2004) in the SED as an upper limit.

References: (1) Alonso-Herrero et al. (2012); (2) Höning et al. (2010); (3) RA2009; (4) Tomono et al. (2001); (5) Gandhi et al. (2009); (6) this work; (7) González-Martín et al. (2013); (8) AH2011; (9) Mason et al. (2006).

### Table 2. High spatial resolution NIR fluxes.

<table>
<thead>
<tr>
<th>Galaxy</th>
<th>J band</th>
<th>H band</th>
<th>K band</th>
<th>L band</th>
<th>M band</th>
<th>Ref(s).</th>
</tr>
</thead>
<tbody>
<tr>
<td>NGC 1365</td>
<td>–</td>
<td>8.3 ± 0.8</td>
<td>–</td>
<td>–</td>
<td>–</td>
<td>1</td>
</tr>
<tr>
<td>NGC 3227</td>
<td>–</td>
<td>7.8 ± 0.8</td>
<td>16.6 ± 1.7</td>
<td>≤47</td>
<td>≤72</td>
<td>2, 3</td>
</tr>
<tr>
<td>NGC 4151</td>
<td>69 ± 14</td>
<td>104 ± 10</td>
<td>177 ± 18</td>
<td>≤325</td>
<td>≤449</td>
<td>4, 3</td>
</tr>
<tr>
<td>NGC 1068</td>
<td>9.8 ± 2.0</td>
<td>≤98</td>
<td>190 ± 28</td>
<td>920 ± 138</td>
<td>2270 ± 341</td>
<td>5, 6, 7</td>
</tr>
<tr>
<td>NGC 3081</td>
<td>–</td>
<td>0.22 ± 0.13</td>
<td>–</td>
<td>–</td>
<td>–</td>
<td>8</td>
</tr>
<tr>
<td>NGC 56433</td>
<td>–</td>
<td>–</td>
<td>–</td>
<td>≤12.2</td>
<td>–</td>
<td>9</td>
</tr>
</tbody>
</table>

References: (1) Carollo et al. (2002); (2) Kishimoto et al. (2007); (3) Ward et al. (1987a); (4) Alonso-Herrero et al. (2003); (5) Alonso-Herrero et al. (2001); (6) Thatre et al. (1997); (7) Marco & Alloin (2000); (8) Quillen et al. (2001); (9) this work.

*3We included in the SED the 6 μm flux, from ISOCAM/ISO reported by Lutz et al. (2004) as an upper limit. All the J, H and K fluxes are from NICMOS/HST observations (F110W, F160W and F222M filters) except the K-band fluxes of NGC 1068 and NGC 5643, which are from SHARP/INT and SOFI/INTT, respectively. L and M fluxes are from COMIC/3.6 m ESO telescope in the case of NGC 1068, and from NSFCam/IRTF (L) and IRCam3/UKIRT (M) for NGC 3227 and NGC 4151.*

### Table 3. High spatial resolution MIR fluxes from T-ReCS/Gemini South, OSCIR/Gemini North, VISIR/VLT and MIRTO/Subaru.

<table>
<thead>
<tr>
<th>Galaxy</th>
<th>N band</th>
<th>NIR flux densities (mJy)</th>
<th>Ref.</th>
<th>N-band spectra</th>
<th>Ref.</th>
</tr>
</thead>
<tbody>
<tr>
<td>NGC 1365</td>
<td>203 ± 30</td>
<td>T-ReCS/Si-2</td>
<td>818 ± 204</td>
<td>T-ReCS/Qa</td>
<td>1</td>
</tr>
<tr>
<td>NGC 3227</td>
<td>320 ± 48</td>
<td>VISIR/PAH2,2</td>
<td>–</td>
<td>–</td>
<td>2</td>
</tr>
<tr>
<td>NGC 4151</td>
<td>1320 ± 200</td>
<td>OSCIR/N</td>
<td>3200 ± 800</td>
<td>OSCIR/IHW18</td>
<td>3</td>
</tr>
<tr>
<td>NGC 1068</td>
<td>10000 ± 1500</td>
<td>MIRTO/8.72 μm</td>
<td>21800 ± 5450</td>
<td>MIRTO/18.5 μm</td>
<td>4</td>
</tr>
<tr>
<td>NGC 3081</td>
<td>83 ± 12</td>
<td>T-ReCS/Si-2</td>
<td>231 ± 58</td>
<td>T-ReCS/Qa</td>
<td>3</td>
</tr>
<tr>
<td>NGC 5643</td>
<td>161 ± 24</td>
<td>VISIR/PAH2</td>
<td>–</td>
<td>–</td>
<td>5</td>
</tr>
<tr>
<td>NGC 5643</td>
<td>287 ± 43</td>
<td>VISIR/PAH2,2</td>
<td>790 ± 200</td>
<td>T-ReCS/Qa</td>
<td>2.6</td>
</tr>
</tbody>
</table>

References: (1) Alonso-Herrero et al. (2012); (2) Höning et al. (2010); (3) RA2009; (4) Tomono et al. (2001); (5) Gandhi et al. (2009); (6) this work; (7) González-Martín et al. (2013); (8) AH2011; (9) Mason et al. (2006).
### Table 4. Normalized average Sy1 and Sy2 SEDs constructed by using the individual photometric and spectroscopic data of NGC 1365, NGC 3227, NGC 4151 (Sy1), NGC 1068, NGC 3081 and NGC 5643 (Sy2).

<table>
<thead>
<tr>
<th>( \lambda_c ) (( \mu )m)</th>
<th>Sy1 SED (mJy)</th>
<th>Sy2 SED (mJy)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1.60</td>
<td>0.036 ± 0.005</td>
<td>0.0019 ± 0.0003</td>
</tr>
<tr>
<td>2.22</td>
<td>0.075 ± 0.011</td>
<td>0.012 ± 0.002</td>
</tr>
<tr>
<td>3.50</td>
<td>0.15 ± 0.02</td>
<td>0.05 ± 0.01</td>
</tr>
<tr>
<td>4.80</td>
<td>0.23 ± 0.03</td>
<td>0.11 ± 0.02</td>
</tr>
<tr>
<td>8.74</td>
<td>0.49 ± 0.07</td>
<td>0.46 ± 0.07</td>
</tr>
<tr>
<td>11.88</td>
<td>1.00 ± 0.15</td>
<td>1.00 ± 0.15</td>
</tr>
<tr>
<td>18.17</td>
<td>1.99 ± 0.50</td>
<td>1.75 ± 0.44</td>
</tr>
</tbody>
</table>

### 3.2 Spectroscopy

In addition to the NIR and MIR photometry reported in Table 2, we compiled \( N \)-band spectra (8–13 \( \mu \)m) for all the galaxies considered here. Those spectra were obtained with the VISIR, T-ReCS and MICHELLE instruments, using the slit widths indicated in Table 3. The T-ReCS spectra are from González-Martín et al. (2013), and were reduced using the RedCan pipeline (described in detail in the latter paper). The MICHELLE spectra are from Mason et al. (2006) and AH2011 and the VISIR spectrum of NGC 3227 is from Höning et al. (2010).

We note that the apparent strength of the nuclear 9.7 \( \mu \)m optical depth measured for the six galaxies considered here is low (\( \tau_{9.7} < 1 \); Höning & Kishimoto 2010; AH2011; González-Martín et al. 2013), and thus it can be reproduced with clumpy torus models, as explained in the introduction.

### 3.3 Average Sy1 and Sy2 photometry and spectroscopy

Since we are looking for general properties of Sy1 and Sy2 SEDs, we constructed average Sy1 and Sy2 templates using our small sample of nearby, nearly face-on and undisturbed Seyfert galaxies.

The best-sampled SEDs, those of NGC 1068 and NGC 4151, define the wavelength grid, from 1.6 to 18.2 \( \mu \)m (see Table 4). This grid includes seven photometric data points, and we interpolated nearby measurements of the other galaxies on to this scale, excluding upper limits. The average Sy1 and Sy2 SEDs, normalized at 11.88 \( \mu \)m, are reported in Table 4. Errors correspond to the nominal percentages considered for NIR and MIR nuclear flux measurements (15 per cent for all of them but \( Q \)-band fluxes, for which we consider 25 per cent errors). See RA2011 for further details on IR flux uncertainties.

We also stacked the individual Sy1 and Sy2 spectra, once normalized at 11.88 \( \mu \)m, using the IRAF\(^5\) task `scombine` with the ‘average’ option to combine the data. The individual and stacked spectra are shown in Fig. 1.

Finally, in Fig. 2 we show the average Sy1 and Sy2 photometry and spectroscopy, as well as the interpolated photometric data for the individual galaxies. All the data were normalized at 11.88 \( \mu \)m, and the Sy1 data shifted in the \( Y \)-axis for clarity. The main differences between the two Seyfert types are the flatter NIR slope of the Sy1s as compared to the Sy2s, and the shallow 9.7 \( \mu \)m silicate absorption in the Sy2 spectrum, which is absent in the Sy1 data.

In RA2011, we reported average Sy1 and Sy2 SEDs as well, but constructed from a larger sample and considering photometry only. By comparing the latter with Table 4, we find no difference between the Sy1 average SEDs, and only a slightly higher \( H \)-band flux in the case of the average Sy2 SED considered here. However, this flatter NIR slope is compatible with the individual Sy2 SEDs in RA2011.

### 4 RESULTS

#### 4.1 Clumpy torus models and Bayesian approach

The clumpy models of Nenkova hold that the dust surrounding the central engine of an AGN is distributed in clumps, with a radial extent \( Y = R_o/R_d \). \( R_o \) and \( R_d \) are the outer and inner radius of the toroidal distribution, respectively (see the
The radial density profile is a power law ($r^{-\alpha}$). Optical depth per single cloud ($\tau_{\text{V, sub}}$) is 0–3 mag, based on the values of the individual galaxies; $\alpha$ was always the closest in wavelength to the previous one: $Q_{\text{2013}}$. Finally, we added the stacked and resampled SEDs (see Tables 2 and 3) with BayesClumpy are the posterior distributions for the six free parameters that describe the models. When the observed data introduce sufficient information into the fit, the resulting posteriors will clearly differ from the input uniform distributions, either showing trends or being centred at certain values within the intervals considered. A detailed description of the Bayesian inference applied to clumpy models can be found in Asensio Ramos & Ramos Almeida (2009). In addition, to see different examples of the use of clumpy model fitting to IR SEDs using BayesClumpy, see RA2009, RA2011 and AH2011.

We fit the Sy2 SED considering reprocessed torus emission and no foreground extinction, since NGC 1068, NGC 3081 and NGC 5643 are undisturbed, nearly face-on galaxies without prominent nuclear dust lanes. On the other hand, for the Sy1 SED, which is the average of Seyfert 1.5 and 1.8 SEDs, we need to consider the AGN direct emission (see RA2009 and RA2011). Following Nenkova et al. (2008a), we include a piecewise power-law distribution (Rowan-Robinson 1995) in addition to the torus reprocessed emission.

In the case of the type 1 Seyferts, we also allowed for a small amount of foreground extinction, separated from the torus, to redden the direct AGN emission. We consider this foreground extinction as an additional parameter in the fit ($A_V \leq 3$ mag, after considering the individual $A_V$ values reported in the literature for the individual Sy1s considered here) and we use the IR extinction law of Chiar & Tielens (2006) in the range $\sim 1–35$ $\mu$m, which accounts for the two silicate features at 9.7 and 18 $\mu$m. Foreground extinctions smaller than $\sim 5$ mag have negligible effect in the torus parameters derived from the Sy2 fits (Alonso-Herrero et al. 2003), but they can be significant for Sy1s, whose NIR SEDs have an important contribution from AGN direct emission (RA2009).

Finally, we resampled all the 8–13 $\mu$m spectra to $\sim 50$ points, following the same methodology as in Alonso-Herrero et al. (2013).

### 4.2 Bayesian adaptive exploration

The aim of this work is to analyse the SED sensitivity to the clumpy model parameters of Nenkova, rather than providing the best-fitting results to IR SEDs, as we did in previous studies. To this end, we used BAE to evaluate the optimum next observation that maximizes the constraining power of the SED (Asensio Ramos & Ramos Almeida 2013). In Figs 4 and 5, we show the simulated iterated BAEs for the average Sy1 and Sy2 SEDs (photometry + spectroscopy), respectively, as we did in Asensio Ramos & Ramos Almeida (2013) for NGC 3081.

As a first step, we assumed that we only have one photometric point in the $N$ band (at 11.88 $\mu$m; see Table 4) and we let the BAE scheme select the following filters. BayesClumpy then uses that point to sample the posterior distribution and obtains marginal posteriors for the clumpy model parameters. The 11.88 $\mu$m point, together with the model SEDs sampled from the posterior, is shown in the first column of Figs 4 and 5. The remaining panels display the marginal posteriors for the six clumpy model parameters.

In order to simulate the next experiment, we selected the next observation in the observed SED that has the largest expected utility, which in the two cases is the $Q$-band data point (18.2 $\mu$m). The full process is then repeated until we have all the observed points of the SED. In both Sy1 and Sy2 BAE experiments, the next observation was always the closest in wavelength to the previous one: $Q$, $Si$-2, $M$, $L$, $K$ and $H$. This is logical if we consider that the bulk of the torus emission peaks in the MIR (see Asensio Ramos & Ramos Almeida 2013). Finally, we added the stacked and resampled $N$-band spectra.

### Table 5. Clumpy model parameters and intervals considered as uniform priors. For the Sy1s, we also considered foreground extinction as an additional parameter ($A_V \leq 3$ mag, based on the values of the individual galaxies; Alloin et al. 1981; Ward et al. 1987b; Mundell et al. 1995).

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Interval</th>
</tr>
</thead>
<tbody>
<tr>
<td>Width of the angular distribution of clouds ($\sigma)$</td>
<td>$[15^\circ, 75^\circ]$</td>
</tr>
<tr>
<td>Radial extent of the torus ($Y$)</td>
<td>$[5, 100]$</td>
</tr>
<tr>
<td>Number of clouds along the equatorial direction ($N_0$)</td>
<td>$[1, 15]$</td>
</tr>
<tr>
<td>Power-law index of the radial density profile ($q$)</td>
<td>$[0, 3]$</td>
</tr>
<tr>
<td>Inclination angle of the torus ($i$)</td>
<td>$[0^\circ, 90^\circ]$</td>
</tr>
<tr>
<td>Optical depth per single cloud ($\tau_{\text{V, sub}}$)</td>
<td>$[5, 150]$</td>
</tr>
</tbody>
</table>
Figure 4. BAE experiment for the average Sy1 SED. A new observed point from Table 4 is added in each step (indicated with labels in the first column). This SED has $N$-band fluxes at 8.74 and 11.88 $\mu$m, which are labelled as 2N when they are both included in the fit. The first column also shows the model SEDs obtained from the posterior distributions in each case. The next six columns represent the marginal posteriors of the clumpy parameters. The last row includes the stacked Sy1 spectrum shown in Fig. 1.

Figure 5. Same as in Fig. 4, but for the average Sy2 SED.
All the experiments performed for both the average Sy1 and Sy2 SEDs and the corresponding posteriors are shown in Figs 4 and 5. We did the same experiment for the individual SEDs in order to confirm the results, but we do not include the figures here for the sake of simplicity.

4.2.1 Sy1

As described in Section 4.1, we fitted the Sy1 SED with reprocessed torus emission, AGN direct emission, and allowed for a small amount of foreground extinction ($A_V \leq 3$ mag). We show the results of the BAE experiment in Fig. 4.

When we only consider MIR photometry (i.e. 8–18 μm data; three top rows in Fig. 4), we cannot constrain any of the torus parameters (i.e. the posteriors do not significantly differ from the uniform priors). It is when we add $M$- and $L$-band photometry that we start to see trends: small torus widths and inclination angles ($\sigma$ and $i$, respectively), flat cloud distributions and low number of clumps ($q$ and $N_0$) become more probable (fourth and fifth rows). We note that at this point, the silicate feature at 9.7 μm is predicted in emission in the fitted models.

When we include $H$- and $K$-band data in the fit, we observe the same trends in the posteriors, with the only exception of $\tau_1$, for which large values within the considered range are preferred (sixth and seventh rows). Finally, when we include the $N$-band spectrum in the fit, which shows a flat silicate feature, the number of clumps increases to reproduce it, and $Y$ appears well constrained. Thus, from this experiment and the individual ones we can infer the following.

(i) Flat silicate features can be reproduced with relatively large number of clouds ($N_0 \sim 10$–15) and large optical depth ($\tau_1 \sim 100$–150). On the other hand, strong silicate emission is associated with optically thin dust (low $N_0$ and $\tau_1$; Sturm et al. 2005; Mason et al. 2012). Other combinations of clumpy torus parameters can produce these features (see fig. 16 in Nenkova et al. 2008b), but here we discuss the results of experiments with real observations.

Hönig & Kishimoto (2010) claimed that silicate emission in type 1 AGN can be also associated with steeper cloud distributions (i.e. large values of $q$), in which the majority of the clouds are close to the active nucleus, and consequently hotter than in flat radial distributions (low values of $q$). The larger amount of hot dust produces a silicate feature in emission. From the fits of the average and individual Sy1 SEDs studied here (see Appendix A), which show absent silicate features, we obtain flat to intermediate radial profiles ($q = 0$–1.5; i.e. cooler dust).

(ii) Adding NIR data (1 to 5 μm) to the MIR SED constrains the torus width ($\sigma$) and the inclination angle of the torus ($i$). In the case of the Sy1s, which generally show flatter IR SEDs than Sy2s (see Fig. 2), it appears enough to add $L$- or $M$-band photometry to the MIR data to reliably constrain $\sigma$ and $i$.

(iii) Another parameter that it is constrained after including $L$- and/or $M$-band data in the fit is the index of the radial density profile ($q$), which defines the distribution of the clumps. Hönig & Kishimoto (2010) reported on a tight correlation between the MIR slope of type 1 AGN (measured from linear fitting between the 7–8.5 μm and 13.4–14.6 μm regions) and $q$, with flatter slopes corresponding to redder MIR colours.

(iv) The $q$ parameter is closely related to the torus size ($Y$). In clumpy models, for steep radial density distributions ($q = 2, 3$), the SED is never sensitive to the outer torus extent. This is because the majority of the clouds are located in the inner part of the torus, closer to the nucleus for all values of $Y$. In models with flatter radial profiles ($q = 0, 1$), more clumps are located farther from the central engine. These SEDs are more sensitive to $Y$, but only at wavelengths $\gtrsim 20$ μm, according to Nenkova et al. (2008b).

In the case of the Sy1 SED, we have a flat radial profile that allows us to constrain the torus size ($Y$) when we add the $N$-band spectrum. This means that it is possible to constrain the torus size by including an 8–13 μm spectrum when we have a flat radial profile. It is worth noting, however, that this torus size corresponds to the outer radius of the MIR-emitting disk. Cooler dust emits in the far-IR (FIR) and indeed, data from the Herschel Space Observatory at 70–500 μm have proved to be useful for constraining $Y$ and $q$ (RA2011; Alonso-Herrero et al. 2012).

Finally, we find that including a small amount of foreground extinction in the fits ($A_V^{\text{opt}} \leq 3$ mag) does not have a significant effect on the torus parameters. However, for galaxies with $A_V^{\text{opt}} \gtrsim 5$ mag, the effect of extinction has to be taken into account, not only for Sy1s, but also for Sy2s, especially when trying to reproduce the 9.7 μm silicate feature and the NIR emission (see also AH2011). For this reason, we emphasize that it is important to either select AGN with no nuclear dust lanes (undisturbed and face-on) or have accurate measurements of the nuclear foreground extinction, when attempting to derive torus parameters from SED fitting.

4.2.2 Sy2

We performed the BAE experiment for the Sy2 SED considering torus reprocessed emission only, without foreground extinction. If we look at Fig. 5, we see that, as it happens with the Sy1 fit, none of the posteriors is really constrained when we only fit MIR photometry (top three rows). It is after introducing $L$- and $M$-band photometry in the fit (fourth and fifth rows) that the parameters start to show trends. However, when we include $H$- and $K$-band data (sixth and seventh rows), the majority of these trends change, differently to what happens to the Sy1 SED (see Fig. 4). From this experiment and the individual ones, we conclude the following.

(i) The models reproduce the silicate feature in absorption (see Fig. 2) with large number of clumps ($N_0 \sim 1$–5) and intermediate optical depth of the clouds within the considered interval ($\tau_1 \sim 50$), which usually happens when fitting Sy2 SEDs (AH2011).

(ii) As in the case of the Sy1 fit, the MIR-to-NIR slope is sensitive to $q$, $\sigma$ and $i$, with higher MIR-to-NIR ratios associated, in general, with intermediate to edge-on views. In the case of the Sy2, however, we need data at $\lambda < 3$ μm to reliably constrain $q$, $\sigma$ and $i$. The steeper NIR slope of Sy2 SEDs, as compared to those of Sy1s, requires to be sampled using the $J$, $H$ and/or $K$ bands to reliably constrain these parameters.

The case of $\sigma$ appears not as clear-cut as those of $q$ and $i$ if we look at Fig. 5 only. The corresponding posterior in the seventh column (i.e. before including the spectrum) is not well constrained. However, if we consider the BAE experiments performed for NGC 3081 and NGC 5643, we find that we can reliably constrain $\sigma$ by including NIR data in the fit, without spectroscopy. We note that in the case of the Sy2 fit, we obtain a low value of $\sigma$, a behaviour that is not common in Sy2s (see RA2011 and AH2011). This is due to the slightly flatter NIR slope of the Sy2 SED, as compared to the average Sy2 SED in RA2011. In fact, the NIR SED shape...
resembles that of NGC 1068, whose fit produces similar posteriors (see Appendix A).

(iii) Regarding \( q \) and \( Y \), we see roughly the same behaviour as in Fig. 4: if we have a flat radial profile, as is the case \( (q < 1) \), we can reliably constrain \( Y \) by fitting the spectrum in addition to the photometry, which efficiently reduces the parameter space. On the other hand, in the case of NGC 3081, we have a steep radial profile \( (q > 2) \), and we cannot constrain \( Y \) by including the spectroscopy (see Appendix A).

### 4.2.3 SED sensitivity to the torus parameters

From the BAE experiments performed in the previous sections for the average and individual Sy1 and Sy2 SEDs, we can conclude the following.

First, having a well-sampled NIR/MIR SED, with photometric data only, and probing scales \( \lesssim 50 \) pc, it is possible to reliably constrain the torus width \( (\sigma) \), its inclination \( (i) \) and the radial profile of the clumps \( (q) \). The resulting posteriors are practically the same if we do and do not include \( N \)-band spectroscopy.

Secondly, in addition to the NIR and MIR photometry, we need subarcsecond 8–13 \( \mu m \) spectroscopy to put realistic constraints on the torus extent \( (Y) \). If the cloud distribution is flat \( (q = 0, 1) \), the \( N \)-band spectrum efficiently reduces the number of models compatible with the MIR data (see the bottom rows of Figs 4 and 5) and we can constrain the extent of the MIR-emitting dust \( (Y) \). On the other hand, if we have a steep radial profile \( (q = 2, 3) \) the NIR/MIR SED is not sensitive to the outer torus extent, as the majority of the clumps are close to the nucleus, and we cannot put reliable constraints on \( Y \). In any case, if we pursue a reliable estimate of the torus size, FIR data are required for probing the coolest dust within the torus.

We find that the depth of the 9.7 \( \mu m \) silicate feature is sensitive to the number of clumps and their optical depth \( (N_0, \tau_V) \). Strong emission features are normally associated with optically thin dust \( (low N_0, \tau_V) \). On the other hand, and according to the experiments performed here, flat/absent silicate features in Sy1 translate in large values of \( N_0 \) and \( \tau_V \), while the shallow absorption features normally seen in Sy2 galaxies are generally reproduced with high values of \( N_0 \) and intermediate \( \tau_V \) (see AH2011 for more examples of Sy2 fits including spectroscopy).

The silicate feature is also dependent, although to a lesser extent, on the radial cloud distribution. Absent silicate features in Sy1 and stronger absorptions in Sy2 are normally associated with flatter cloud distributions (i.e. more clumps located farther from the active nucleus and consequently cooler; Hönig & Kishimoto 2010).

In RA2011, we fitted NIR and MIR photometry only with the clumpy torus models of Nenkova, and the silicate features were generally predicted in emission. In those cases, we obtained lower values of \( N_0 \) from the fits. On the other hand, AH2011 included \( N \)-band spectroscopy in the fits, which in the case of the four Sy1 studied showed absent silicate features. As happens here, weak or absent silicate features can be reproduced with large number of clumps \( (N_0 \sim 10–15) \) and optical depths \( (\tau_V \sim 100–150) \). For the Sy2s, which generally show shallow silicate absorption features, we find large values of \( N_0 \) \( (\sim 8–15) \) and intermediate \( \tau_V \) \( (\sim 50) \), as in RA2011 and AH2011.

Thus, in general, we conclude that we can constrain torus width, inclination and distribution of the clouds with NIR and MIR photometry only, but MIR spectroscopy is necessary to restrict the posterior distributions of the number of clouds and their optical depth. The torus extent can also be constrained with MIR spectroscopy, but only in those cases where the clumps show a flat radial distribution. This is summarized in Fig. 3, where we represent the parameters that depend on the MIR-to-NIR ratio in blue and those that require MIR spectroscopy in red.

### 4.3 Minimization of the filter set

Looking at the evolution of the posteriors in Figs 4 and 5, we have learnt that \( N \)-band spectroscopy and NIR photometry are necessary to constrain all the torus parameters. Now we can investigate the minimum filter set needed to obtain the same posterior distributions as those in the last row of Figs 4 and 5. Thus, we repeated the experiment for the average Sy1 and Sy2 SEDs, but starting with the \( N \)-band spectrum and the 11.88 \( \mu m \) point only. In this experiment, instead of selecting the next observation with the largest utility, we tried different combinations of filters. The results are plotted in Figs 6 and 7.

#### 4.3.1 Sy1 minimum filter set

In the case of the Sy1 SED, the \( N_0 \) and \( \tau_V \) posteriors in the first row of Fig. 6 are practically identical to those obtained when we fit the whole SED (bottom row). This is because the \( N \)-band spectrum is sensitive to \( N_0 \) and \( \tau_V \), and in this case, the absent silicate feature itself rules out low values of these parameters (see Section 4.2.1). In the second, third and fourth rows of Fig. 6, we added one NIR data point to the fit \( (H, L, M, \text{respectively}) \). Including \( H \)-band data \( (or K \text{ band, as we also checked}) \) constrains the \( \sigma \) and \( i \) posteriors, as expected. If we include \( L \)- or \( M \)-band photometry instead, the resulting posteriors are exactly as those in the last row of Fig. 6. In the fifth row, we checked that adding \( Q \)-band data to the \( M + N \)-band spectrum does not have any significant effect on the fit. Finally, in the sixth row we fitted the combination of \( H + K + N \)-band data, which also produces practically the same posteriors as in the bottom row, except for \( q \) and \( i \).

The lack of constraining power of the \( Q \)-band data in the fit, when used in combination with \( N \)-band spectroscopy, is noteworthy. What is happening is that the 8–13 \( \mu m \) spectrum itself restricts the parameter space in the MIR, making it rather unnecessary to include 18 \( \mu m \) data. This effect is clearly illustrated in the top-left panels of Figs 4 and 6. The number of models compatible with the 11.88 \( \mu m \) photometry only in the first row of Fig. 4 are far more than those in the same row of Fig. 6, with the spectrum included. According to Nenkova et al. (2008b), we need data at wavelengths \( \gtrsim 20 \mu m \) to constrain torus outer extent \( (Y) \), but here we find that \( N \)-band spectroscopy reduces more efficiently the parameter space, and it is the addition of the spectrum, in combination with NIR photometry, what constrains the torus size when we have flat radial profiles \( (q = 0, 1; \text{see the two last rows of Figs 4 and 5}) \).

As we are fitting average SEDs, and different SED shapes are sensitive to different torus properties, we have repeated the previous experiment for the individual galaxies. In particular, we have chosen NGC 3227 and NGC 4151, whose SED shapes are different between them and well sampled (see Fig. 2). The results of these experiments are shown in Figs A1 and A2 in Appendix A. The individual fits confirm the results obtained for the average Sy1 SED, but suggest a slightly different minimum filter set. In both cases, the combination of \( H+K+N \)-band data produces exactly the same posteriors as when fitting the whole data set (see the fourth and third rows of Figs A1 and A2, respectively). Unfortunately, we only have \( L \)- and \( M \)-band upper limits for NGC 3227 and NGC 4151, so we cannot check if the combination of \( L/M \)- and \( N \)-band data produces the same results.
Figure 6. Same as in Fig. 4, but starting the Sy1 experiment with the N-band spectrum and 11.88 µm point, and choosing different combinations of filters.

Figure 7. Same as in Fig. 6, but for the Sy2 average SED and choosing different combinations of filters.

Thus, considering the average and individual Sy1 fits, the combinations of 8–13 µm spectrum and M- or H + K-band photometry appear to be the minimum necessary to constrain the torus parameters of Sy1 galaxies. If possible, we encourage the potential users of torus models to use a combination of two NIR data points (among J, H and K) in addition to M-band photometry + N-band spectroscopy for accurately constraining the torus parameters of Sy1 galaxies, although the minimum filter set for
individual SEDs appears to be an 8–13µm spectrum + M-band photometry.

4.3.2 Sy2 minimum filter set

The experiment with the average Sy2 SED produces similar results. In the second and third rows of Fig. 7, we added H- and M-band data, respectively, to the N-band data. As for the Sy1 fit, the combination of M- and N-band data (third row) produces posteriors which are similar to those in the last row of Fig. 7. However, it is when we fit \( H + M + N \)-band data that we obtain the same results as when we fit the whole data set (fourth row). This is likely due to the steeper slope of Sy2 SEDs, which is better defined by the \( H + M + N \)-band data. We obtain the same results when using \( H + M + N + Q \)-band and \( H + K + M + N \)-band data (fifth and sixth rows).

As we did for the Sy1 galaxies, in Appendix A we show the results from the individual SED fits of NGC 1068 and NGC 3081 (see Figs A3 and A4). In the case of NGC 1068, all the posterior plots are similar but \( \sigma \) and \( Y \) are well constrained when we fit \( J + M + N \)-band data (fifth row). In this case, we have a steep radial profile \( (q \sim 2) \) and thus, the SED is not sensitive to \( Y \), as explained in Section 4.2.1. In the fifth row of Fig. A3, we confirmed the lack of constraining power of the \( Q \)-band data when used in combination with \( N \)-band spectroscopy. Finally, the fit of \( J + K + M + N \)-band data (sixth row) produces the same \( \sigma \) posterior as in the bottom row of Fig. A3. The SED of NGC 1068 is peculiar, showing an NIR bump that it is reproduced with a small torus width, more characteristic of Sy2 galaxies in general (RA2011). In any case, it is noteworthy that the \( J \)-band data seem to work better in this case than the \( H \)-band data for constraining \( \sigma \) and \( i \).

The fit of the whole NIR+MIR data set of NGC 3081, which is shown in the fourth row of Fig. A4, produces posteriors much more typical of Sy2 galaxies (RA2011). In this case, we just need to fit \( H + N \)-band data (second row) to obtain the same posteriors as with the whole data set. In fact, using \( N \)-band spectroscopy only we have practically the same result (top row) with slightly broader posteriors. In the case of NGC 3081, we also have nuclear FIR fluxes from the Herschel Space Observatory that we published in Ramos Almeida et al. (2011b). In the fifth, sixth and seventh rows of Fig. A4, we added PACS 70, 100 and 160µm data to the fit, respectively. Including the FIR data points only affects the \( Y \) posterior, which has a maximum of probability towards larger values (bottom row). In this case, we have a very steep radial profile \( (q \sim 2) \), and thus, only with FIR data it is possible to have a weak constraint on the torus size, which in this case is relatively large, as we are probing cooler dust within the torus.

Considering the average and individual Sy2 fits discussed here, the minimum combination of data needed to reliably constrain the torus parameters is \( H + M \)-band photometry + \( N \)-band spectroscopy, although in some cases, the use of \( J + K + M \)-band fluxes, in addition to the 8–13µm spectrum, is necessary to correctly constrain the torus width. Thus, whenever possible, we encourage the reader to use two NIR data points (preferably including \( J \)-band data) in addition to \( M \)-band photometry and \( N \)-band spectroscopy. This filter set ensures a reliable determination of all the torus parameters of Sy2 galaxies.

The difference between the minimum filter sets of Sy1s and Sy2s is likely related to the AGN contribution to the SED. In the case of the Sy2s, whose IR SEDs can be reproduced with torus emission only, the parameters are very sensitive to different SED shapes. On the other hand, for the Sy1s, the intrinsic AGN emission is strong in the NIR, and thus the parameters are less sensitive to SED variations.

Summarizing, based on our analysis of average and individual IR SEDs of Seyfert galaxies, we conclude that the minimum combination of IR data necessary to constrain the torus parameters is \( M \)-band photometry + 8–13µm spectroscopy for Sy1 galaxies, and \( H + M \)-band photometry + 8–13µm spectroscopy for Sy2 galaxies. However, to reliably constrain all the torus parameters of both Sy1 and Sy2 galaxies, independently of SED shape, we recommend the use of \( J + K + M \)-band photometry and \( N \)-band spectroscopy. Finally, we emphasize that this is valid, in general, for undisturbed, face-on nearby Seyfert galaxies without dust lanes, and using high angular resolution IR data, dominated by torus emission.

5 CONCLUSIONS

We have compiled subarcsecond NIR and MIR photometry (1–18µm) and MIR spectroscopy (8–13µm) for a small sample of nearby, undisturbed, nearly face-on Seyfert galaxies without prominent nuclear dust lanes. We used average and individual Sy1 and Sy2 SEDs (photometry and spectroscopy) to (1) study the sensitivity of different IR wavelengths to the clumpy torus model parameters of Nenkova, and (2) derive the minimum combination of IR data needed to constrain torus geometry and intrinsic properties. Our major conclusions are as follows.

(i) Subarcsecond resolution 8–13µm spectroscopy alone reliably constrains the number of clumps and their optical depth \( (N_0 \) and \( \tau_v \)). Flat silicate features translate in large values of \( N_0 \) \( (\sim 10–15) \) and \( \tau_v \) \( (\sim 100–150) \) in the case of the Sy1 galaxies analysed here. On the other hand, shallow absorption features are reproduced with large values of \( N_0 \) \( (\sim 8–15) \) and \( \tau_v \) \( (\sim 50) \) in the case of Sy2 galaxies.

(ii) It is possible to constrain torus width and inclination \( (\sigma \) and \( i \)) with subarcsecond resolution NIR and MIR photometry only, with steeper IR slopes generally indicating intermediate to edge-on views and vice versa.

(iii) The radial density profile of the clouds \( q \) requires fitting of NIR and MIR photometry to be constrained. In the case of the Sy1s, adding \( L \)- and/or \( M \)-band photometry to the MIR data is enough, as there is a tight correlation between the MIR slope (measured from \( \sim 7 \) to 15µm by Höning & Kishimoto 2010) and \( q \), with flatter slopes producing redder MIR colours.

(iv) In addition to NIR photometry, we need 8–13µm spectroscopy and a flat radial profile (i.e. low values of \( q \)) to put realistic constraints on the torus extent \( (Y) \). However, to have a reliable estimate of the torus size, FIR data are required for probing the coolest dust within the torus. For steep radial profiles (large values of \( q \)); the majority of clouds located close to the inner edge of the torus), the NIR/MIR SED is never sensitive to the outer torus extent.

(v) In the case of nearby, undisturbed, nearly face-on Seyferts without dust lanes, the minimum combination of IR data necessary to reliably constrain all the torus parameters, independently of the SED shape, is \( J + K + M \)-band photometry + \( N \)-band spectroscopy.

(vi) Despite the fact that it is probing the bulk of the torus emission, the \( Q \)-band data analysed here (at 18µm) lack of constraining power when used in combination with 8–13µm spectroscopy, as the latter efficiently reduces the parameter space.

\footnote{Any combination of two NIR filters (among \( J, H \) and \( K \)) should be valid when added to the \( M + N \)-band data, but \( J + K \) is the one that better samples the NIR SED.}
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APPENDIX A: INDIVIDUAL FITS

The results of this work are based on the fits of both the average and individual Sy1 and Sy2 SEDs, as different SED shapes are sensitive to different torus properties. The individual fits are shown in Figs A1, A2, A3 and A4.

Figure A1. Same as in Fig. 6, but for the Sy1.5 NGC 3227 and trying different combinations of filters.

Figure A2. Same as in Fig. 6, but for the Sy1.5 NGC 4151 and trying different combinations of filters.
Figure A3. Same as in Fig. 7, but for the Sy2 NGC 1068 and trying different combinations of filters.

Figure A4. Same as in Fig. 7, but for the Sy2 NGC 3081 and trying different combinations of filters. In the last three rows, we have included nuclear FIR fluxes from the Herschel Space Observatory (Ramos Almeida et al. 2011b), labelled as P1, P2 and P3 (70, 100 and 160 $\mu$m, respectively).

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