Atomic structure and segregation in alkali-metal heteroclusters

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The ground-state atomic and electronic distributions in Na$_m$Cs$_n$ clusters with composition $m = n$ and $m = 2n$ have been calculated by minimizing the total cluster energy using the density-functional formalism. The approximation is made by replacing the total external potential of the ions by its spherical average around the cluster center during the iterative process of solving the Kohn-Sham equations for each geometry tested. In the size range studied here (up to 90 atoms per cluster), the cluster is composed of well-separated homoatomic Na and Cs shells, the external one always being a Cs shell. We have also found that the cohesive energy goes rapidly to the bulk limit. An analysis of the geometries shows strong cluster reconstruction with increasing size. By comparing the geometry of pure Na$_n$ with that of the Na$_n$ core in Na$_m$Cs$_n$ for clusters formed by only an inner Na layer and an outer Cs layer, we have observed that the Na$_n$ core adopts a geometry different in most cases from that of the free Na$_n$ cluster, and such that the number of faces of the polyhedron formed by the Na$_n$ core is as close as possible to the number of external Cs atoms, in order to accomodate these Cs atoms on top of the faces of the polyhedron.

I. INTRODUCTION

Clusters with an atomic content below, say, 100 atoms, have a substantial part of them on the surface. Their atomic arrangements are usually different from their bulk counterparts due to the surface effect. When the cluster size decreases, the geometry depends more sensitively on the detailed electronic structure and bonding. In pure bulk metals we know that only a few types of crystalline structures occur; in contrast, clusters with few atoms reconstruct their geometries with increasing size in a way not yet known.

The delocalized character of the electrons in alkali-metal clusters and heteroclusters has been inferred from experiments. A model of electrons in a spherical or an ellipsoidal potential well due to a positive jellium background accounts for many experimental results. Properties depending on the discrete nature of the ions are evidently outside the scope of the jellium model.

In a study of the liquid-vapor interface of the Na metal and Na-Cs alloys, Rice and co-workers have performed Monte Carlo simulations for very large aggregates in the size range between 100 and 1000 atoms. These authors have shown that a pronounced stratification of the atomic distribution develops near the surface, with a layer spacing of about one atomic diameter. Furthermore, segregation of Cs to the surface was found in the simulations for the Na-Cs alloy.

In small alkali-metal heteroclusters, with most atoms at or very near to the surface, it is expected that stratification and segregation effects will dominate the entire cluster structure. Some preliminary results presented by the authors have shown that the cluster Na$_{10}$Cs$_{10}$ is formed by an inner Na shell surrounded by a Cs shell.

Using the Car-Parrinello method, Ballone et al. have found segregation of potassium to the surface of a Na$_{30}$K$_{10}$ cluster.

Relevant questions in this area are the following: How does the segregation effect depend on cluster size? Evidently, segregation is a surface effect. But what happens when one looks at the whole cluster? Is there random mixing of Na and Cs? Or, rather, do ordering or full phase separation occur? Bulk Na-Cs alloys are miscible in the liquid state. In the solid state a single intermetallic compound, of composition Na$_3$Cs, forms at low temperature, but solid solutions do not exist. This indicates the importance of the temperature for mixing. In summary, it should be interesting to know if the miscibility properties change in microalloys with fewer than 100 atoms. In this work we study the atomic arrangements of Na$_m$Cs$_n$ heteroclusters with $m = n$ and $2n$, and with a total number of atoms up to $N = n + m = 90$, paying particular attention to questions like mixing, ordering, segregation, and relative stability of the clusters as a function of size and magic numbers.

II. MODEL

In this section we give a brief sketch of the computational method used to obtain the ground-state geometry, and the corresponding energy, of the clusters.

First of all, the atoms are placed at random positions, and the valence-electron distribution is self-consistently calculated by minimization of the total energy, according to the Kohn-Sham version of density-functional theory using the local-density approximation for exchange and correlation effects. At this moment, the net forces at the ionic sites are nonzero, and then the ions are allowed
to move a small distance in the force directions. The
electron distribution is computed for this new atomic
arrangement, and the whole cycle is iterated until a
minimum of the total energy with respect to all ionic
coordinates is obtained, that is, until all the forces vanish.
As the only guarantee for reaching the absolute
minimum, and not a relative one, the whole process is
repeated for a sufficient number of random initial
configurations of the atoms (in practice, this number has
been taken to be larger than 40).

Empty-core model potentials\textsuperscript{14} are used to describe
the pseudopotentials of the individual ions. The empty-core
radii, $r_e$(Na) = 1.74 a.u. and $r_e$(Cs) = 2.74 a.u., lead to the
experimental ionization potentials in the free-atom limit
for the same density-functional method.

An essential approximation of the method is that the
total ionic potential due to the ions at positions $\mathbf{R}_i$

$$V_f (r) = \sum_i \nu(|r - \mathbf{R}_i|),$$

is substituted by its spherical average around the cluster
center (center of ionic charge), $V_f^\text{av}(r)$, in the process
of integrating the Kohn-Sham equations. For this reason
we call this method the spherically averaged pseudopotential (SAPS) method.\textsuperscript{15} However, the exact ion-ion
Coulombic repulsion is evaluated in our calculations,
which makes the total energy a function dependent on
the precise location of the atoms.

Additional details concerning the density-functional
formalism used here can be consulted in Ref. 15, where
applications to different pure-metal clusters have been
done.

\section{III. Results}

\subsection{A. Layering, segregation, and growth}

Let us consider first the main features of the atomic
distribution in Na$_m$Cs$_n$ clusters with $m = n$ and $2n$ and a
total number of atoms $N \leq 90$. A common characteristic
for the two concentrations and all sizes is the formation of
homoatomic shells, that is, separated shells of Na and
Cs atoms, respectively, with the most external shell always
occupied by Cs atoms. The most salient features
concerning the formation and evolution of these shells
with cluster size can be observed in Fig. 1. The radial
distribution of atoms (with respect to the center of ionic
charge of the cluster) has been plotted for a few representat-
ive cases ($N$ = 8, 20, 40, 58, and 90) for Na$_4$Cs$_4$ and
$N$ = 9, 21, 39, and 90 for Na$_2$Cs$_2$. Clusters up to about
$N$ = 42 have two homoatomic layers (for both concentra-
tions), the inner one formed by the Na atoms and the
outer one by the Cs atoms. The definition of the Na layer
is more ambiguous than that of the Cs layer, this one be-
ing appreciably thinner. For Na$_4$Cs$_4$, it is perhaps more
realistic to describe the distribution of the Na atoms by
a well-defined shell only in the restricted size range $N \leq 26$.
Instead, from $N$ = 28 up to $N$ = 44 there are a few inter-
mediate Na atoms halfway between the internal (Na) and
external (Cs) shells (see, for instance, Na$_{20}$Cs$_{20}$ in Fig. 1).

For Na$_{2n}$Cs$_n$ one observes an appreciable broadening
of the whole Na shell with respect to Na$_4$Cs$_4$. Larger
clusters with $46 \leq N \leq 60$ develop a Cs layer in the inner re-
region. Then their configuration is that of a Na region with
a large dispersion of radial distances bound on the inside
by one Cs shell and on the outside by another, more pop-
ulated, Cs shell. It is noticeable that the cluster size $N$ at
which the inner Cs shell appears is about the same for the
two concentrations studied here. One could have expec-
ted some difference due to concentration because the Cs-
Na-Cs stratification can be considered as a precursor of
the tendency to superlattice formation in the bulk solid
alloy and the only stable intermetallic compound that has
the Na$_x$Cs composition.\textsuperscript{11} Many more atoms are needed,
however, to resemble closely the bulk behavior. Finally,
the figure also shows the atomic distributions for the two
concentrations at $N$ = 90. In this case a new Na shell ap-
pears in the inner region of Na$_{40}$Cs$_{20}$ but not in Na$_{28}$Cs$_{45}$.
This difference is due to the different concentration, and
it suggests that the stoichiometry Na$_x$Cs develops order-
more easily than the NaCs stoichiometry, which is in
agreement with the situation observed in the bulk phase.\textsuperscript{13} In summary, we can look at the process of cluster
growth as the successive formation of inner homoa-
atomic shells, at least in the size range $N < 100$.

Besides the existence of homoatomic shells, we ob-
serve, for most clusters with $N > 10$, a strong tendency
to find one single atom at the cluster center. For Na$_n$Cs$_n$
the central atom is Na up to $N$ = 26, whereas at larger
sizes the nature of the central atom is anticorrelated with
that of the innermost shell; that is, the central atom is Cs
when the innermost shell is formed by Na atoms and vice
versa. For Na$_{2n}$Cs$_n$ the central atom is Na with very few
exceptions.

The valence-electron density is also plotted in Fig. 1, in
units of the average bulk electron density $\rho_{av}$, defined as
$\rho_{av} = 1/\Omega_{av}$, where $\Omega_{av} = [m\Omega_{(Na)} + n\Omega_{(Cs)}]/N$, $\Omega_{(Na)}$
and $\Omega_{(Cs)}$ being the volumes per atom in bulk Na and Cs,
respectively.

The (average) radii of the shells and their widths (mea-
sured by the standard deviations) are given in Fig. 2 for
Na$_n$Cs$_n$. The width of the surface (Cs) shell never
exceeds 1 a.u. In contrast, the dispersion in the Na shell
is larger, about 2 a.u. in some cases, and it would increase
further if the intermediate Na atoms in the size range
$N$ = 28–44 (these have been omitted from the figure) were
ascribed to this shell. The radius of the surface shell,
which is a measure of the cluster size, is a linear function
of $N^{1/3}$ with a slope approximately equal to $r_s^* = (3\Omega_{av}/4\pi)^{1/3}$. Radii for Na$_{2n}$Cs$_n$ are not shown in
the figure, but it is interesting to note that the radius of
the external Cs shell is very similar for the two concen-
trations at each size, considering the large atomic size
difference, between Na and Cs.

The distribution of Cs atoms in Na$_n$Cs$_n$ is given in Fig.
3. The majority of Cs atoms is in the surface shell. First,
the number of atoms in the surface shell increases steeply
with $n$, but later this number grows at a lower rate due to
the formation of the inner Cs shell.

Previous calculations\textsuperscript{15,16} for homoatomic Na$_n$ and Cs$_n$
clusters using the SAPS method have also produced a structure formed by atomic layers. In the case of sodium clusters, there is one single layer for \( n < 7 \), one layer plus a central atom for \( 7 \leq n \leq 19 \) (except for \( \text{Na}_4 \)),\(^{17} \) and two layers for \( 20 \leq n \leq 50 \). The situation for \( \text{Cs}_n \) is very similar\(^{16} \) to the small difference that \( \text{Cs}_8 \) is not an exception and that the configuration of two layers starts at \( n = 19 \). The geometries of homoatomic clusters (to be discussed in more detail below) are rather similar to those obtained by Manninen,\(^{15} \) minimizing the electrostatic interactions of point positive ions in a spherical and homogeneous negative background. This trend is, however, very different from that for \( \text{Na}_n \). In heteroclusters, the difference between the core radii of the Na and Cs atoms is responsible for (a) the formation of distinct homoatomic layers, which we interpret as a precursor of the order-
ing effects found in the bulk solid alloy, and (b) the strong segregation of Cs atoms to the surface. Segregation is evident since the outer layer is always formed by Cs atoms. Segregation of Cs to the surface of very large Na/Cs clusters was also obtained in the Monte Carlo simulations of Rice,\textsuperscript{6} as well as layer stratification near the surface.

Anagnostatos\textsuperscript{19} has proposed a way of interpreting the abundance spectrum and magic numbers of alkali-metal clusters based on geometrical considerations. Compared with our results, there is, however, an essential difference in the pattern of cluster growth, both for homoatomic and heteroatomic clusters. In the model proposed by Anagnostatos, the clusters grow outward; that is, the external layers form over the previously formed inner layers. In contrast, our results indicate a strong reconstruction of the whole cluster as it grows. In the size range covered by our calculations, additional inner shells grow when the external shell is sufficiently filled. We may interpret this effect as a tendency to minimize the surface energy of the cluster. A particularly evident manifestation of this effect can be seen in Fig. 3, where, in the range \( N = 42 - 52 \), the population of the surface shell remains nearly constant, while the additional Cs atoms give rise to an internal Cs layer.

Summarizing the features exposed so far, we identify three main conclusions: (a) First of all, in the small size regime considered in this paper, the geometries bear no relation to those of bulk crystals, since the surface effect is very strong and dominates the cluster reconstruction as \( N \) grows. (b) Cs atoms strongly prefer the outer part of the cluster. This is again a surface-controlled effect, since Cs segregation lowers the surface energy of the cluster. (c) However, when the cluster is large enough, Cs atoms begin to form a new shell in the inner part of the cluster, and for \( \text{Na}_{60}\text{Cs}_{30} \) we have found a sequence of layers \( \text{Na-Cs-Na-Cs} \). We interpret this as a precursor of the tendency to superlattice formation in the bulk solid alloy, due mostly to atomic size difference.

At this point it is fair to point out that in the process of calculating the equilibrium geometry of Na-Cs clusters (also of pure Na\(_n\) or Cs\(_n\)), we find a large number of relative minima with energies close to that of the ground state. This is a manifestation of the “soft” nature of clusters formed by alkali metals. This softness accounts for the strong reconstruction with increasing size, and it also suggests that very large cluster sizes are needed to exhibit the crystallographic structure of the bulk solid. This contrasts with the situation for clusters with ionic bonding. In a study of Cs\(_n\)O, we have found that the coordination around the oxygen impurity is rather stable as a function of cluster size, and furthermore, this coordination is similar to that in the bulk oxide.\textsuperscript{16}

B. Stability and magic numbers

Sharp variations in the relative stability of the clusters as a function of size give rise to the so-called magic numbers, which appear as prominent features (maxima or pronounced steps) in the abundance spectrum.

Figure 4 gives the total energy per atom, \( E(N)/N \), of

![FIG. 2. Average radii of Cs (+ and \( \bigcirc \)) and Na (*) shells and their widths (measured by the standard deviation) in Na\(_x\)Cs\(_y\) vs \( N^{1/3} \). \( N = 2n \) is the number of atoms in the cluster.](image)

![FIG. 3. Number of atoms in the inner (I) and surface (S) Cs shells of Na\(_x\)Cs\(_y\) as a function of size. Note that these clusters have an even number of atoms.](image)

![FIG. 4. Energy per atom, \( E(N)/N \), in Na\(_x\)Cs\(_y\) as a function of cluster size. Note that \( N \) has only even values. Filling of electronic shells is indicated.](image)
Na₅Csₙ as a function of the number of atoms in the cluster. $E(N)/N$ shows pronounced minima for $N=8, 20, 34, 40, \text{ and } 58$. This is a consequence of electronic shell-closing effects. Clusters with $8, 20, 34, 40, \text{ and } 58$ valence electrons have the closed-shell electronic configurations $1s^22p^6$, $1s^22p^62s^22p^{10}$, $1s^22p^62s^22p^{14}$, $1s^22p^62s^22p^{10}2p^{14}2p^{18}$, $1s^22p^62s^22p^{10}2p^{14}2p^{18}$, respectively. We then predict that these clusters should be prominent in the abundance spectra. The general trend in the energy curve is similar to that obtained for homoatomic alkali-metal clusters both in the jellium and SAPS models, and the above numbers, $N=8, 20, 34, 40, \text{ and } 58$, are, in fact, experimental magic numbers of pure alkali-metal clusters and mixed alkali-metal clusters. We then conclude that the magic numbers of pure and mixed alkali-metal clusters depend only on the number of electrons in the cluster. However, the geometry and atomic distribution are sensitive to the nature of the atoms in the cluster and to their relative proportion.

The convergence of the energy of the cluster to the bulk limit can be studied by calculating the cohesive energy per atom. For the clusters with composition Na₅₅Csₙ, the cohesive energy per atom can be written

$$E_{coh}(Na_mC_s) = \frac{1}{m+n} \left[ mE(Na) + nE(Cs) - E(Na_mC_s) \right] ,$$

where $E(Na)$ and $E(Cs)$ are free-atom energies calculated by the same model. The cohesive energies are plotted in Fig. 5 for $m=n$ and $2n$. As mentioned above, the only bulk solid alloy is the ordered compound Na₅Cs. The cohesive energy (per atom) of this compound is given by

$$E_{coh}(Na_5Cs \text{ alloy}) = \frac{1}{5} \left[ 2E_{coh}(Na) + E_{coh}(Cs) \right] + \Delta H ,$$

where $E_{coh}(Na)$ and $E_{coh}(Cs)$ are the cohesive energies of the pure metals, and $\Delta H$ is the heat of formation of the alloy with respect to the pure metals. $\Delta H$ is negative, since the compound exists, but its precise value has not yet been determined. The only theoretical calculation for this compound gives the wrong sign for $\Delta H$, but at least suggests that the absolute value of $\Delta H$ is small compared to the cohesive energies of the pure metals Na and Cs, which is the usual situation for metallic alloys. Additional evidence for a small $|\Delta H|$ comes from the experimental fact that the number of intermetallic compounds in this binary system is only one (Na₂Cs). Consequently, we can approximate

$$E_{coh}(Na_5Cs \text{ alloy}) \approx \frac{1}{5} \left[ 2E_{coh}(Na) + E_{coh}(Cs) \right] .$$

Using experimental values for the cohesive energies of the pure metals, Eq. (4) gives $E_{coh}(Na_5Cs \text{ alloy})=0.037$ a.u. On the other hand, the cohesive energy of the cluster Na₂₅Cs₁₃ is already equal to 0.031 a.u./atom. From the evolution of $E_{coh}$ with cluster size in Fig. 5, we can conclude that the bulk limit of $E_{coh}$ is approached rather rapidly.

One could argue that a better idea of the convergence to the bulk limit can be obtained by using in Eq. (4) theoretical predictions for $E_{coh}(Na)$ and $E_{coh}(Cs)$ (obtained under the same assumptions used in our cluster calculations) instead of the experimental values. Nevertheless, it is well known that density-functional theory and the pseudopotential approximation work extremely well for the simple alkali metals and the theoretical predictions for the cohesive energy are in very good agreement with experiment. For instance, an all-electron density functional calculation by Moruzzi et al. gives $E_{coh}(Na)=1.116 \text{ eV/atom}$, in nearly perfect agreement with the experimental value of 1.113 eV/atom. Calculations using the empty-core pseudopotential also give very good results for the binding energies of Na and Cs. Actually, we estimate that the error from using experimental pure-metal cohesive energies instead of calculated ones is not larger than the error from neglecting $\Delta H$ in Eq. (3).

In Fig. 6 we give the energy balance of the reaction

$$Na_{2n} + Cs_n \rightarrow Na_{2n}Cs_n .$$

This reaction is exothermic; that is, the mixed cluster is stable with respect to the pure fragments, but the magnitude of the heat of the reaction, if measured per atom, decreases rapidly with increasing size. In the case $n \rightarrow \infty$ this energy balance becomes the energy of formation $\Delta H$ of the bulk Na₅₅Cs compound starting from the pure metals, but at small $n$ the formation of the Na₂₅Csₙ clusters does not proceed, evidently, through reaction (5). The heat of the reaction $Na_{2n} + Cs_n \rightarrow Na_{2n}Cs_n$ is also included in Fig. 6.

The evolution of the Kohn-Sham one-electron eigenval-
atom provides a more attractive potential than a Cs atom, giving rise to an enhanced probability for s-type electrons in the central region. For small clusters \((N \leq 26)\) this effect is strong enough to place the 2s level below the 1d level. Inversion between the 1d and 2s levels has also been found in the case of divalent impurities in alkali-metal clusters.\(^{28,29}\) This inversion is responsible for the appearance of a new magic number in those clusters, corresponding to ten electrons.

Also, the 2p and 1g states are closer here than in the jellium model for pure clusters.\(^{27}\) This effect is also present in recent jellium-on-jellium calculations for Na clusters coated by Cs.\(^{30}\) Finally, the oscillations of the 2s eigenvalue in the region \(N=50–58\) are correlated with the number of Cs atoms in the inner shell of the cluster.

C. \(Na^+_n\) geometries

It is the purpose of the next section (Sec. III D) to discuss the geometries of small \(Na^+_nCs^-_n\) clusters formed by an inner Na shell and an outer Cs shell. In particular, we wish to show the way the external Cs layer modifies the geometrical arrangement of the internal Na content with respect to the geometry of the pure \(Na^+_n\) counterpart.

As a prior step, we first discuss the geometries of the pure \(Na^+_n\) clusters, comparing these with the results of other calculations which avoid the spherical approximation for the total ionic potential. Because of this approximation, our resulting geometries for very small clusters are more spherical than those obtained in more accurate calculations, which are restricted, however, to date, to very small clusters. \textit{Ab initio} configuration-interaction (CI),\(^{31}\) extended-Hückel,\(^{32}\) and density-functional pseudo-potential\(^{33–36}\) results are available for the equilibrium geometries of \(Na^+_n\) up to \(n=9\). These are, as ours, static calculations. Our stable geometries for some clusters are given in the left-hand part of Fig. 8. \(Na^+_9\) is a trigonal bipyramid. This is a metastable geometry in Ref. 31, lying

FIG. 6. Energy balance for the reactions \(Na^+_n + Cs^- \rightarrow Na^+_nCs^-_n\) and \(Na^+_n + Cs^- \rightarrow Na^+_nCs^-_n \) vs \(N (N=3n \ or \ 2n, \ respectively)\).

FIG. 7. One-electron Kohn-Sham eigenvalues as a function of cluster size for \(Na^+_nCs^-_n\). The outermost occupied level is indicated by a circle.
0.04 eV/atom above the stable planar form. The geometry for both Na₆ and Na₇ is the regular octahedron, but with an atom in its center in the case of Na₇. Na₆ is a pentagonal pyramid and Na₇ a pentagonal bipyramid in more accurate calculations. We have found that the pentagonal bipyramid is the first excited local minimum of Na₇ in the SAPS model, being almost degenerate with the centered octahedron (the difference in energy is only 0.004 eV/atom, whereas the cohesive energy per atom is 0.65 eV). Our geometry for Na₈ is a square antiprism, in agreement with the density functional results of Manninen and co-workers and Arvati et al. This occurs because in the later calculations the electronic configuration is close to 1s²1p⁶, which gives a spherically symmetric electron density to which the ionic lattice responds, adopting also a very spherical geometry. Na₉ is an atom-centered square antiprism. The more stable geometry obtained by Wang et al. and Cogordan et al. is, in our calculations, a local minimum, 0.03 eV/atom above the absolute minimum. The equilibrium geometries of Na₁₀ and Na₁₁ are very regular. Na₁₀ is a centered tricapped trigonal prism (D₃h), and Na₁₁ is a centered square antiprism bicapped at the square faces (C₄v). Na₁₂ is a distorted centered icosahedron with a vertex lost and Na₁₃ a perfect centered icosahedron. A configuration-interaction calculation by Pacchioni and Koutecky suggested that the equilibrium geometry of Li₁₃ is a centered icosahedron. A more complete dynamical study has been performed by Ballone et al. for Na₂₀ at T = 0 and 200 K. The equilibrium geometry at T = 200 K (in an average sense) resembles our static geometry (see Fig. 9) in that there are two atoms inside a more external arrangement of the remaining 18 atoms.

In summary, we have found that the equilibrium geometries predicted by the SAPS model for small Na clusters are often identical to those of more accurate calculations and, in other cases, coincide with the geometries of low-lying isomers. Since, first of all, the SAPS model is expected to become better for larger clusters (which are more spherical than the smaller ones) and, on the other hand, the energy differences between the ground-state equilibrium geometry and those of low-lying isomers are rather small, we can have some confidence in our predictions for “large” mixed clusters.

FIG. 8. Geometries of pure Naₙ (left-hand column), Naₙ part in NaₙCsₙ (central column), and whole NaₙCsₙ (right-hand column), for n = 6, 7, 8, 9, 12, and 13. Open and solid circles represent Na and Cs atoms, respectively. Distances are all in a.u.

FIG. 9. Equilibrium geometry of pure Na₂₀.
D. Geometries of Na₈Cs₄

A few representative clusters (corresponding to \( n = 6, 7, 8, 9, 12, \) and 13) have been chosen as illustrative examples of the small size range. Figure 8 shows, for each \( n \), the geometry of pure Na₈ (left-hand part), that of the Na core (denoted Na*₈) in the Na₈Cs₄ heterocluster (middle column), and the whole Na₈Cs₄ geometry (right-hand column). The pure Na₈ geometries have already been discussed in Sec. III C. Na*₈ is a nonregular centered trigonal bipyramid (D₃h). This is a polyhedron with six faces, to which the six outer Cs atoms of Na₈Cs₄ can be easily coordinated. Each Cs atom is on top of one of the faces, and the six Cs atoms then form a trigonal prism surrounding the Na*₈ core. Na*₈ brings out the central atom of Na₈ on top of a face of the octahedron. The seven Cs atoms are then on top of the remaining seven faces of the octahedron. The square antiprism Na₈ reconstructs in such a way that Na*₈ is a centered octahedron with one vertex split into two symmetrical ones and C₃v symmetry, as the way to provide the eight faces needed to host the eight Cs atoms. The Na₈ structure (centered square antiprism) remains the same in forming the heterocluster, and the nine Cs atoms become coordinated to nine of the ten faces, leaving one triangular face empty. Note, however, that the interatomic distances in the Na*₈ core have increased with respect to those in the free Na₈ cluster. The structures of the Na*₈ and Na*₁₂ cores are different from those of the pure Na clusters, the trend governing the changes being the tendency to form a polyhedron with a number of faces closer to the number of Cs atoms. The Na*₁₂ core in Na₁₂Cs₁₂ has D₃h symmetry; it is formed by one Na atom at the center of a polyhedron with 12 faces. Each of the 12 Cs atoms is coordinated to one of the 12 faces of the Na polyhedron, preserving the D₃h symmetry. Finally, Na*₁₃₈ is a little distorted with respect to Na₁₃, but it remains as an icosahedral arrangement, covered by 13 Cs atoms in the following way: Four Cs atoms (atoms E) are on top of edges of the Na₁₃ (I₈) core, and each one is coordinated to four Na atoms. The remaining nine Cs atoms are on top of nine triangular faces (atoms T), whereas three faces rest empty.

Interatomic distances are also given for Na₈ and Na*₈ in Fig. 8. When only one distance is reported, this means that the polyhedron is regular or that an average \( \langle d \rangle \) of the polyhedron edges is made. Averaged values for the edges of the external polyhedra joining Cs and Na atoms are between 8.1 and 8.3 a.u. for the clusters given in Fig. 8.

From the analysis of the cluster topologies, we conclude that the geometry of the Na*₈ core in Na₈Cs₄ is different from that of free Na₈, and that the mechanism of reconstruction is the formation of a polyhedron with a number of faces consistent with the number of external Cs atoms. Then these Cs atoms can sit on top of those faces. This result indeed suggests that specially stable clusters will be obtained by starting with the equilibrium polyhedron for Na₈ and capping each face with a Cs atom. Note, however, that the geometrical stabilization effects are expected to be very small in pure and mixed alkali-metal clusters and will be unobservable in the usual mass spectra. By looking again at Fig. 4, we note that the stability peaks of Na₈Cs₄ clusters \( (N=8, 20, 34, 40, \) and 58) correspond to electronic shell-closing effects.

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17Na*₈ was reported in Ref. 15 as an "empty" cluster. A more extensive search has shown that it contains a central atom.