





Auto-Tuning of a Modified L1-Adaptive Controller with Genetic Algorithms for Dynamic Positioning of a Remotely Operated Vehicle Under Marine Currents

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ABSTRACT

In this article, a modified L1-adaptive controller with auto-tuning using a genetic algorithm is presented for dynamic positioning of remotely operated vehicles (ROVs) under marine currents, based on a six-degree-of-freedom nonlinear model of an ROV. To enable tuning of some of the parameters of the controller, a cost function related to the error of the steady state positions of the system is minimised with the use of the genetic algorithm. A series of simulations are conducted to ascertain the performance of the system with the implemented controller, taking into consideration the vehicle position, orientation, and control signals sent as commands to the thrusters. The simulations are carried out with noise levels representative of those encountered by the standard underwater instrumentation on an ROV, as well as with underwater current velocities. In addition, the results are compared with those of a classical controller to verify the improvements offered by the controller proposed in this paper.

Keywords: Auto-tuning; dynamic positioning; genetic algorithm; modified L1-adaptive; ROV

INTRODUCTION

Today, the use of remotely operated vehicles (ROVs) and unmanned underwater vehicles has become widespread, due to their versatility and the multitude of complex and potentially dangerous operations that these vehicles can perform [1]. Zhao [2] described the development of a mathematical and computational model to improve the planning and execution of missions combining different types of marine vehicles such as Autonomous Surface Vehicles (ASVs) and ROVs. In work by Fay [3], the design of ecological interfaces was proposed as

a paradigm for ROVs, to facilitate optimal future performance and the interaction between a human and the ROV interface. Soylu [4] presented a method for the precise control of the trajectory of an ROV for inspection to improve accuracy when performing inspection tasks. These applications are related to exploration and research, the offshore energy industry, underwater archaeology, environmental monitoring, search and rescue operations, infrastructure inspection, defence and security, aquaculture and fisheries, underwater filming, hazardous environment exploration, pipeline maintenance, and cable installation.

The nonlinear manoeuvring model can be expressed in the following form [5] (for more details about the model and the value of the parameters, see von Benzon [16]):

$$M\dot{v} + C(v)v + D(v)v + g(\eta) = \tau \quad (1)$$

$$\dot{\eta} = J(\eta)v; y_s = \eta + w_n \quad (2)$$

In the NED frame, the position and Euler angle vectors are given by the expression: $\eta = [x, y, z, \phi, \theta, \psi]^T$, and y_s is the output vector with sensor noise. The linear and angular speeds in the body frame velocities are represented by the vector $v = [u, v, w, p, q, r]^T$, while the forces and moments exerted by the thrusters are represented by the vector $\tau = [X, Y, Z, K, M, N]^T$. The vector w_n represents the measurement noise. The matrix M represents the rigid body and added mass, the vector $C(v)v$ denotes the Coriolis term, the matrix $g(\eta)$ represents the restoring matrix, and the matrix $J(\eta)$ is the rotation matrix. The vector $D(v)v$ represents the hydrodynamic damping forces, which are a combination of linear and nonlinear damping.

In the context of ocean currents, as described in the works of Fossen [5] and von Benzon [16], Eq. (1) can be expressed as follows:

$$M_{RB}\dot{v} + M_A\dot{v}_r + C_{RB}(v)v + C_A(v_r)v_r + D(v_r)v_r + g(\eta) = \tau \quad (3)$$

$$v_r = v - v_c \quad (4)$$

The current velocity in the body-fixed coordinate system is:

$$v_c = [V_{cf1}, 0, 0, 0]^T; v_{cf1} = J_1(\eta)^T \times V_{cn} \quad (5)$$

where $V_{cn} = [V_{cun}, V_{cvt}, V_{cwn}, 0, 0, 0]$ is the current velocity in the NED coordinate system, and $J_1(\eta)$ is the first component of the matrix $J(\eta)$. For more details of the model parameters, thrusters, their layout on the ROV, and the system of distributing forces and moments, see von Benzon [16] and Ng [17].

The attenuators $At(s)$ for x, y, z and for ϕ, θ, ψ are:

$$At_{(x,y,z)}(s) = \frac{0.1}{(0.05s)+0.1}; \quad At_{(\phi,\theta,\psi)}(s) = \frac{0.1}{(0.4s)+0.1} \quad (6)$$

MODIFIED L1-ADAPTIVE CONTROL

This section describes the innovative application of the modified L1-adaptive control method to implement a dynamic positioning application for the ROV illustrated in Fig. 1.

In order to achieve this, the adaptive control approach described by Cao [10] and Hovakimyan [18] is employed in combination with a LQG controller. The implementation follows a similar structure to the one described by Sainz [13],

in which this system was used for the control of a marine structure, and by Vajpayee [11], where this controller was used for the control of a nuclear power plant.

The state-space linearisation of the nonlinear model of equation Eq. (1) is carried out as follows:

$$\dot{x}_L(t) = A_L x_L(t) + B_L[u_r(t)] \quad (7)$$

$$y_L(t) = C_L x_L(t) + D_L[u_r(t)] \quad (8)$$

where

- $u_r = \tau$ are the forces and moments generated by the thrusters;
- A_L is the state matrix;
- $x_L(t) = [x_L, y_L, z_L, \phi_L, \theta_L, \psi_L]^T$ is the state vector, the elements of which correspond to the position and the Euler angles vector of the linearised model;
- B_L is the input matrix;
- C_L is the output matrix;
- $y_L(t) = [x_L, y_L, z_L, \phi_L, \theta_L, \psi_L]^T$ is the output vector;
- D_L is the feedforward matrix.

The linearised model in Eq. (7) was obtained by linearising the system around the starting conditions of the system. The Kalman filter is also implemented to filter sensor noise from the position signals that are used in the control system, by considering the linear model of the ROV in Eq. (7). The Kalman filter is implemented using an algorithm described in detail by Fossen [19] and more extensively explained in [5]. The algorithm is as follows:

- Matrix design:

$$Q(t) = Q^T > 0; \quad R(t) = R^T > 0; \quad \hat{x}_{f(0)} = x_{f(0)} \quad (9)$$

- Initial conditions:

$$P(0) = E[(x_{f(0)} - \hat{x}_{f(0)})(x_{f(0)} - \hat{x}_{f(0)})^T] \quad (10)$$

- Kalman propagation matrix:

$$K(t) = P(t)C^T(t)R^{-1}(t) \quad (11)$$

where P is the solution of the algebraic Riccati equation.

- Propagation of estimated states

$$\dot{\hat{x}}_{f(t)} = A_L(t)\hat{x}_{f(t)} + B_L(t)u_r(t) + K(t)[y_f(t) - C(t)\hat{x}_{f(t)}] \quad (12)$$

In this context, the tuning variables are represented by the terms Q and R , which correspond to the covariances of the states and the covariances of the noise, respectively. The term u_r denotes the forces and moments generated by the thrusters, while the term y_f represents the Kalman filter output vector. The estimated state vector is given by the expression \hat{x}_f , while the filtered state vector is represented by the equation $\hat{x}_f = y_f$

$$F_c(t) = -u_{LQR}(t) + u_a(t) \quad (13)$$

The term $u_{LQR}(t)$ denotes the nominal control signals of the LQR controller, whereas $u_a(t)$ represents the adaptive control. The linear feedback of the control state is calculated by minimising the cost function

$$u_{LQR} = -K_{LQR}x_f \quad (14)$$

The cost function was set up as described by Fossen [5]:

$$J(u) = \int_0^\infty [x_f^T Q_{LQR} x_f + u_r^T R_{LQR} u_r] dt; K_{LQR} = R_{LQR}^{-1} B_{LQR}^T P_{LQR} \quad (15)$$

P_{LQR} is calculated by solving the algebraic equation of Riccati:

$$A_L^T P_{LQR} + P_{LQR} A_L - P_{LQR} B_L R_{LQR}^{-1} B_L^T P_{LQR} + Q_{LQR} = 0 \quad (16)$$

The matrix Q_{LQR} is employed as a tuning parameter, while the matrix R_{LQR} represents the second of the controller tuning parameters for the LQR controller.

The state in Eq. (7) can be expressed as follows:

$$\dot{x}_L(t) = A_m x_L(t) + B_m[\omega_0 u_a(t) + \sigma_1(t)] \quad (17)$$

The closed loop system matrix, denoted by A_m , can be expressed as follows: $A_m = A_L - B_m K_L^T Q R$, where K_{LQR} represents the control feedback gain. The input matrix is represented by $B_m = B_L$. The disturbance is represented by the function $\sigma_1(t)$, and the input gain matrix by the function ω_0 . This indicates the cross-coupling between different inputs.

$$\omega_0(t) = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} \quad (18)$$

The control system consists of two distinct components: the first is a linear quadratic Gaussian controller, while the second is an adaptive controller comprising the FF, PE, PA and PB blocks illustrated in Fig. 1.

$$\dot{\hat{x}}_a = A_m(t)\hat{x}_a(t) + B_m[\omega_0 u_a(t) + \hat{\sigma}_1(t)] \quad (19)$$

In this case, the estimated state vector of the adaptation part, denoted by the variable $\hat{x}_a(t)$, represents the estimated state of the system. Similarly, the output vector, represented by $\hat{y}_a(t)$, is the estimated output of the system. The input matrix, $B_m = B$, represents the input to the system. The estimated disturbance $\hat{\sigma}_1(t)$ is a variable that represents the estimated disturbance in the system. Finally, the input gain matrix of the system is ω_0 . Once the states have been estimated, a subtraction is performed with the filtered states, resulting in the prediction error, denoted as \tilde{x} .

$$\tilde{x} = \hat{x}_a(t) - x_f(t) \quad (20)$$

The methodology employed for projecting disturbances is in accordance with the procedures delineated by Hovakimyan [18] and by Vajpayee [11] for a process control application in

a nuclear power plant, in the work of Sainz [13] for a controller for marine structures, and for ROVs with disturbance rejection [10].

$$\hat{\sigma}_1(t) = \Upsilon Proj(\hat{\sigma}(t) - (\tilde{x}^T(t) P_m B_m)^T) \quad (21)$$

The projection operator Proj is defined as follows [20]. In this context, the notation P_m represents the solution of the algebraic Lyapunov equation, while the parameter θ_{max} is defined as the norm limit, and the tolerance in the projection is represented by the term ε_θ . The adaptation gain, which is denoted by the symbol Υ , is given by the expression in Eq. (21). Once the disturbances have been estimated, a preparatory step is taken to calculate the intermediate variable, which is defined by the expression for $\hat{\eta}(s)$:

$$\hat{\eta}(s) = \omega_0 u_a(s) + \hat{\eta}_1(s) \quad (22)$$

where $\hat{\eta}_1(s) = \hat{\sigma}_1(s)$.

The structure of the adaptive control law is as follows:

$$u_a(s) = -(\hat{\eta}(s) - r_{ffp}(s)) \quad (23)$$

where $r_1(s)$ is the reference signal after the attenuator

$$r_1(s) = r(s)At; \quad r_{ffp}(s) = r_1(s) \times K_g \quad (24)$$

The quantity represented by K_g corresponds to the value of the feedforward filter, which is also known as a feedforward pre-filter. This filter is configured in such a way that the overall system is provided with the requisite conditions for effective control, with the signals being decoupled.

It should be noted that the usual structure of the L1-adaptive controller has been modified by eliminating the integral action that is usually incorporated between the two loops of the controller. This integral action can be eliminated due to the implementation of an auto-tuning system based on the genetic algorithm to tune the control parameter K_g to obtain the desired response and reducing the stationary state error.

AUTO-TUNING WITH THE GENETIC ALGORITHM

In the proposed method described in the previous section, several tuning parameters need to be properly set to obtain the desired response from the system, due to the complexity of the controller. In addition to the parameters corresponding to the Kalman filter and the LQR controller, there are other parameters specific to the L1-adaptive control. The system response is highly sensitive to the tuning of the K_g parameter, corresponding to the feed-forward prefilter. Hence, an auto-tuning process for the parameter was established using the genetic algorithm [21].

A genetic algorithm is used to tune the K_g with the aim of reducing to a minimum the error in the ROV position output by performing the steps shown in Fig. 3.

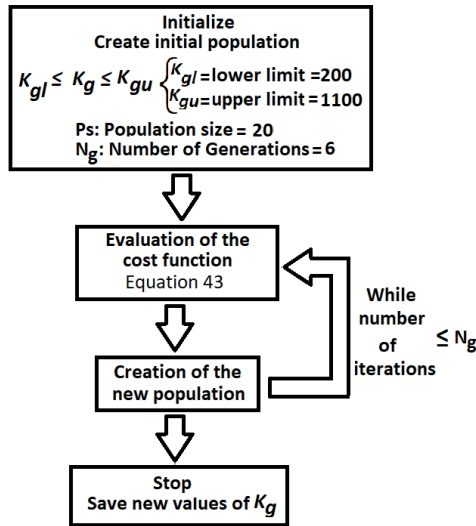


Fig. 3. Genetic algorithm

$$J_{GA} = |r_1(s) - y_f| \times time \quad (25)$$

where $r_1(s)$ is the reference signal after attenuation, and y_f is the Kalman filter output vector.

SIMULATION RESULTS AND DISCUSSION

A series of simulations were conducted in the MATLAB-Simulink environment to ascertain the viability of the proposed control scheme, using a sampling period of 0.1 s.

In the simulations, the reference vector was set to $r(s) = [1m, 1m, 1m, 0rad, 0rad, 0rad]^T$, and the Kalman filter matrices were adjusted as follows:

- $Q = diag([1, 1, 1, 9, 12, 30, 1, 1, 1, 900, 900, 900])$
- $R = diag([0.001, 0.001, 0.0001, 10^{-1}, 10^{-1}, 10^{-1}, 10^{-1}, 10^{-1}, 10^{-1}, 10^{-1}, 10^{-1}, 10^{-1}])$

The LQR tuning matrices were adjusted as follows:

- $Q^{LQG} = diag([1.99 \times 10^3, 0.300 \times 10^3, 0.013 \times 10^3, 0.005 \times 10^3, 0.005 \times 10^3, 0.005 \times 10^3, 0.005 \times 10^3, 0.005 \times 10^3, 0.005 \times 10^3, 0.005 \times 10^3, 0.005 \times 10^3, 0.005 \times 10^3])$
- $R_{LQG} = diag([0.0035, 0.0015, 0.0002, 0.5, 0.5, 0.5, 0.5, 0.5, 0.5, 0.5, 0.5, 0.5])$

Tab. 1. Tuning parameters for the modified L1-adaptive control

K_g	Υ	ε
[965.01, 866.02, 360.33, 1, 1, 1]	[0.1, 15, 12]	[0, 30, 30, 3]

A PID controller was also implemented (Eq. 26) to determine the improvements offered by the proposed controller compared to a classical PID control with the tuning parameters given in Table 2. The references and filter were the same in both scenarios. Consequently, the scenarios in which the simulations were carried out are identical, except that the proposed controller was replaced by the PID controller, as can be seen from Fig. 4.

Tab. 2. Tuning parameters for the PID controller

P	[1356.97, 764.73, 609.18, 27.39, 1.93, 81.43, 4.4466]
I	[80.49, 1.31, 152.28, 293.52, 76.20, 0.6539]
D	[0, 0, 2.08, 12.64, 20.38, 7.41]
N	[0, 100, 2.08, 100, 136.40, 17.66]

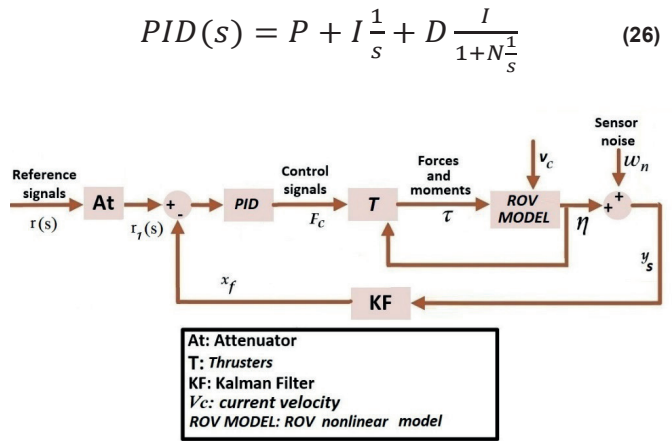


Fig. 4 Schematic of the system with the PID controller

Fig. 5, which represents the motion of the ROV in the x-direction, shows how the controller is able to follow the reference signal without overshoot or oscillations that could lead to a collision with objects or other underwater vehicles. The steady-state error for the implemented controller with self-tuning is approximately 0% of the reference signal. This is acceptable, since it can be observed that the currents that were incorporated into the system are being adequately compensated. Fig. 5 shows that the Kalman filter performs acceptable filtering of the signals.

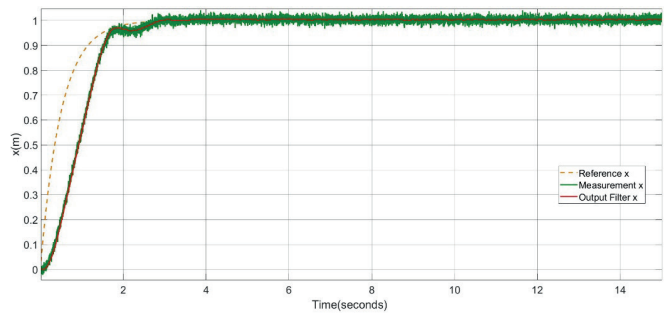


Fig. 5. Results for the ROV with modified L1-adaptive controller for position in the x-direction.

Moreover, it can be observed from Fig. 5 and Fig. 6 that the response at the surge output of x for the modified L1-adaptive controller does not show overshoot or any subsequent attenuation until the response converges to the reference, as in the response for the system with the PID.

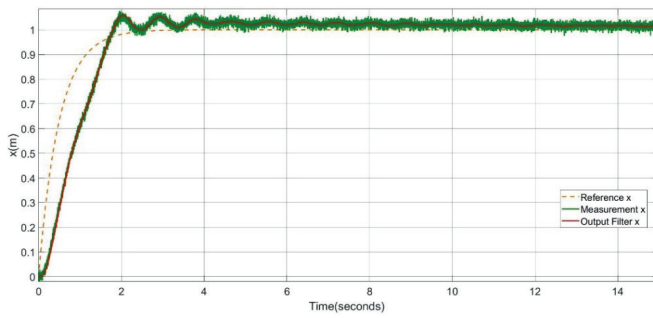


Fig. 6. Results for the ROV with PID controller for position in the x-direction.

Fig. 7 shows the movement along the x -, y - and z -axes of the system with the PID controller. As in the previous cases, a higher deviation is observed when carrying out the motion to arrive at the reference position than when carrying out the motion with the modified L1-adaptive controller, as shown in Fig. 8.

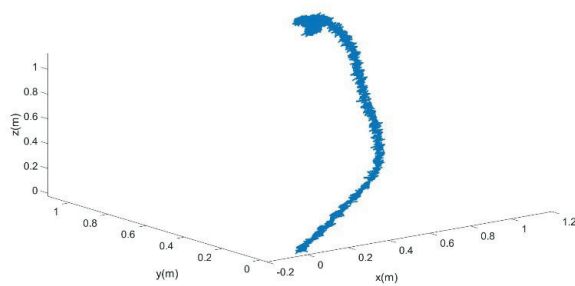


Fig. 7. Results for the ROV with PID controller for the positions in the x -, y - and z -directions

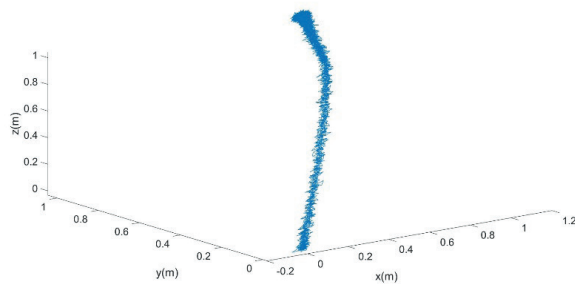


Fig. 8. Results for the ROV with modified L1-adaptive controller for the positions in the x -, y - and z -directions

It can be observed from Fig. 9 that the system despite the external perturbances induced by the currents on three of the axes, presents slight steady state errors in roll, pitch, and yaw motions (ϕ , θ , ψ), which can be considered negligible.

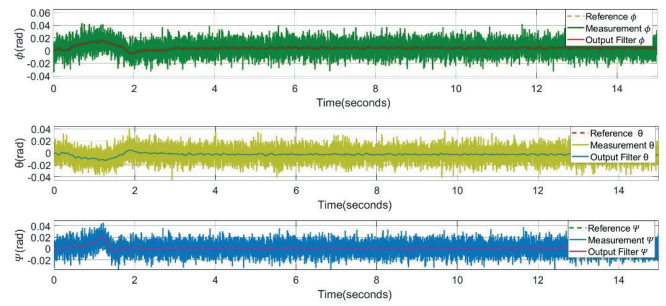


Fig. 9. Results for the ROV with modified L1-adaptive controller for the position in the directions.

The response in terms of the angular movements of both controllers in the steady state is correct, since the deviation in regard to the reference is very small, as can be seen in Fig. 10 for the PID controller and in Fig. 9 for the modified adaptive controller. However, from the output of the PID controller under pitch, it can be seen that during the manoeuvres, the deviation from the reference shown in Fig. 10 is considerably higher than for the modified L1-adaptive controller in Fig. 9.

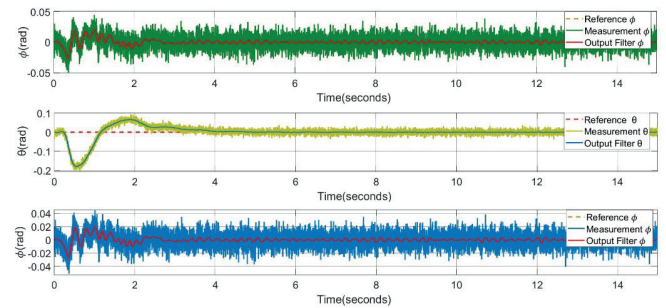


Fig. 10. Results for the ROV with PID controller for positions in the directions.

It can be seen from Fig. 11 that the control signals present no steady-state oscillations and the control effort is low. This leads to an increase in the actuators' service life, and means that an actuation margin can be maintained in the case where marine conditions require it.

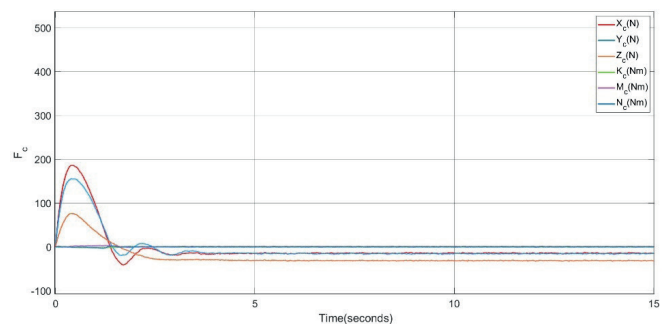


Fig. 11. Results for the ROV with modified L1-adaptive controller for the control signal calculated by the controller

Finally, a comparison of the control signals for the PID controller (Fig. 12) and the proposed modified L1-adaptive controller (Fig. 11) shows that for the PID controller, there is

greater oscillation and higher values of the control signals, which translates into a more demanding performance requirement for the actuators of the system, and hence to a reduction in the life expectancy of the actuators.

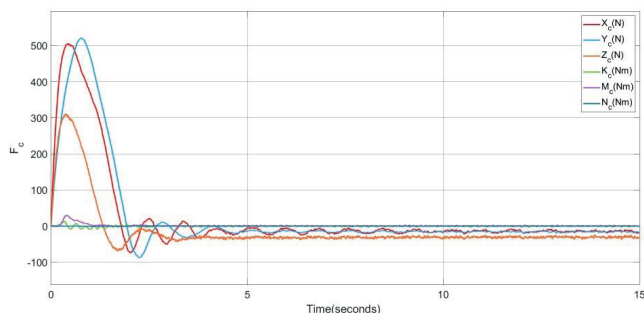


Fig. 12. Results for the ROV with PID controller for the control signal calculated by the controller

As a consequence of the abovementioned effect, the control signals in the thrusters of the system (-1 to 1) also reflect an improvement in the results of the ROV with the modified L1-adaptive controller. It can be observed from Figs. 13 to 16 that the modified L1-adaptive controller only reaches saturation at the beginning of the results for thrusters 2 and 3, and for a shorter time, without other saturation events. From a comparison between the previous results and the results for the ROV with the PID controller, it can be observed that the ROV shows saturation of the signals for all the thrusters, over a longer period, with oscillations in the saturation in some cases.

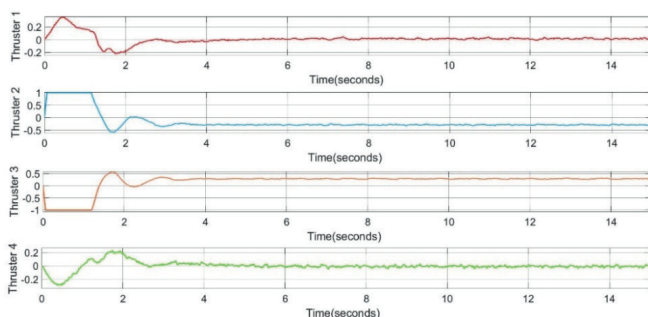


Fig. 13. Results for the ROV with modified L1-adaptive controller for the signals of thrusters 1-4; for more details on the thrusters and their layout on the ROV, see von Benzon [16]

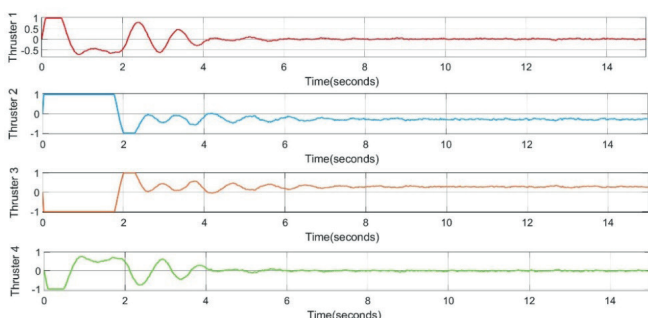


Fig. 14. Results for the ROV with PID controller for the signals of thrusters 1-4

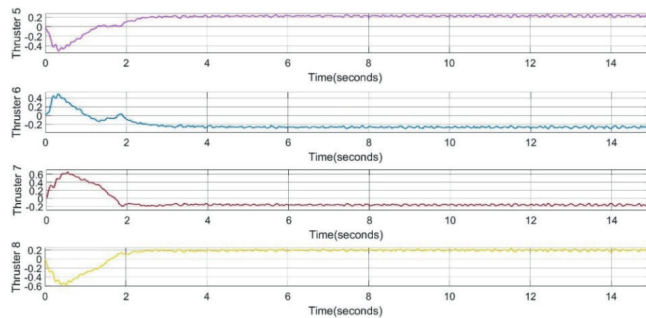


Fig. 15. Results for the ROV with modified L1-adaptive controller for the signals of thrusters 5-8

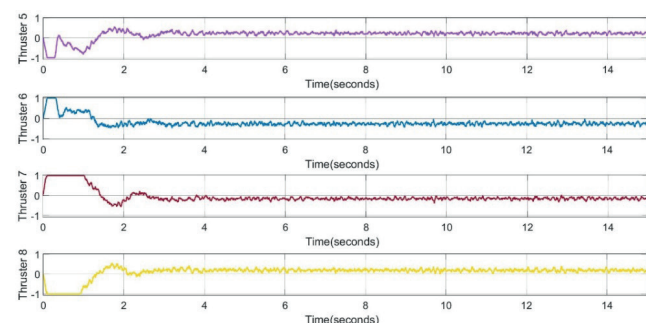


Fig. 16. Results for the ROV with PID controller for the signals for thrusters 5-8

CONCLUSION

In this paper, we have presented a modified L1-adaptive control with autotuning using a genetic algorithm for the dynamic positioning of an ROV subject to undersea currents. Dynamic control is performed in the presence of disturbances corresponding to a standard level of noise for this type of vehicle instrumentation and currents inducing motion along three of the axes. Hence, the dynamic marine environment in which an ROV operates is realistically represented. Several simulations were carried out to verify the correct behaviour of the proposed controller and the autotuning established with the genetic algorithm. Simulation results showed that the implemented controller accurately positioned the ROV at the reference point, and there were no oscillations or overshoots during the positioning manoeuvre. A Kalman filter correctly performed filtering of the ROV positioning signals, and contributed to achieving suitable control signals.

In addition, the control signals were adequate, as they did not exhibit abrupt oscillations; this means that the actuators can have a longer service life, and if the marine environment conditions become worse, the desired position can still be maintained. A comparative study of the proposed controller against a PID controller was also carried out. For all the reasons mentioned in the previous section, it can be concluded that under all the movements studied, the proposed modified L1-adaptive controller produced a better response than the

PID controller. The simulations showed that there was no overshoot and no oscillation.

This system would allow an ROV to operate in scenarios where there is a possibility of collision with other objects, and where precise motion control is required. Similarly, when capturing images using underwater vision instruments, the vehicle is sometimes required to remain as stable as possible. It is notable that with the modified L1-adaptive controller, the oscillations in these positions, which are otherwise present with the classical PID controller, are eliminated. In addition, the control signals of the proposed controller are more desirable than those of the PID controller because they do not undergo such strong oscillations, meaning a greater life expectancy for the actuators. Hence, the proposed controller extends the operational range over which an ROV can operate, due to the possibility of superior control of the vehicle with increased safety for both the human operators and the equipment involved.

The proposed controller also offers a significant advantage for underwater vision, an area which is currently expanding due to the need for supervision of offshore structures and transoceanic pipelines, since if stability can be adequately maintained while the vehicle is moving, it is possible to improve the image capture process and thus simplify the subsequent processing required. Finally, in addition to all the benefits of applying the proposed controller to ROVs that have been highlighted here, which already represent a significant advance, it should be noted that the application of the genetic self-tuning algorithm significantly reduces the difficulty of tuning the controller's parameters. As a result of this self-tuning process, the controller response is robust and adequate, without the need for difficult manual tuning. It may not have been possible to obtain the excellent results presented here with manual tuning.

ACKNOWLEDGMENTS

This project was partially supported through the project TED2021-132158B-I00, "Evolutionary Monitoring with Unmanned Underwater Vehicles for the Maintenance of the Bottom and Anchorages of Offshore Wind Farms", funded by MICIU/ AEI /10.13039/501100011033, by the European Union - Next Generation EU/ PRTR, and through the project "Intelligent and Collaborative Control of Unmanned Underwater Vehicles for the Dynamic Positioning of Floating Marine Structures at Scale" (aid financed by contract programme Gob Cantabria-UC).

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