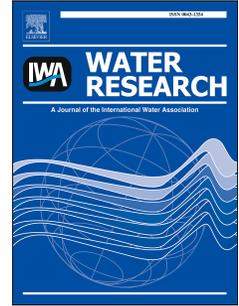


# Accepted Manuscript

Artificial neural networks as emulators of process-based models to analyse bathing water quality in estuaries

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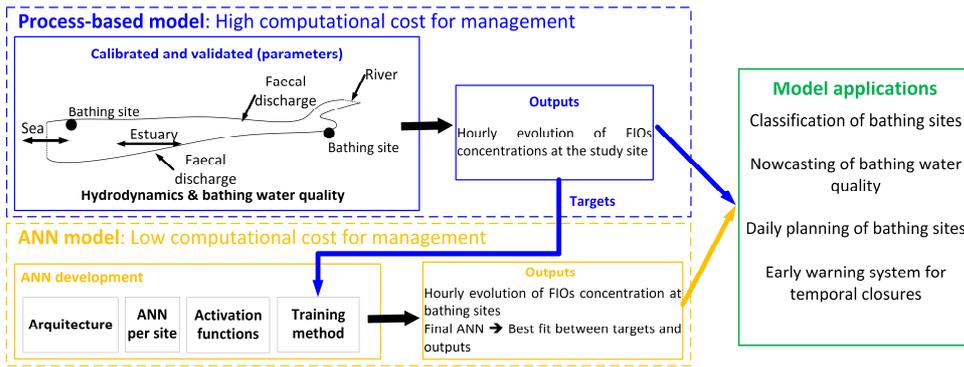
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1 **Artificial neural networks as emulators of process-based models to analyse bathing**  
2 **water quality in estuaries**

3

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10

11 **Highlights**

- 12 • The method integrates laboratory analyses, numerical modelling and machine  
13 learning.
- 14 • ANN configuration for predicting *E. coli* concentration in estuaries is  
15 determined.
- 16 • ANNs are viable emulators of process-based models driven by highly variable  
17 forcing.
- 18 • The longer forecasting, the greater the reduction in computational time using  
19 ANN.
- 20 • Real-time management of bathing water quality is enabled by using ANNs.

21

22 **Abstract**

23 This study aims to provide a method for developing artificial neural networks in  
24 estuaries as emulators of process-based models to analyse bathing water quality and its  
25 variability over time and space. The methodology forecasts the concentration of faecal

26 indicator organisms, integrating the accuracy and reliability of field measurements, the  
27 spatial and temporal resolution of process-based modelling, and the decrease in  
28 computational costs by artificial neural networks whilst preserving the accuracy of  
29 results. Thus, the overall approach integrates a coupled hydrodynamic-bacteriological  
30 model previously calibrated with field data at the bathing sites into a low-order emulator  
31 by using artificial neural networks, which are trained by the process-based model  
32 outputs. The application of the method to the Eo Estuary, located on the northwestern  
33 coast of Spain, demonstrated that artificial neural networks are viable surrogates of  
34 highly nonlinear process-based models and highly variable forcings. The results showed  
35 that the process-based model and the neural networks conveniently reproduced the  
36 measurements of *Escherichia coli* (*E. coli*) concentrations, indicating a slightly better fit  
37 for the process-based model ( $R^2=0.87$ ) than for the neural networks ( $R^2=0.83$ ). This  
38 application also highlighted that during the model setup of both predictive tools, the  
39 computational time of the process-based approach was 0.78 times lower than that of the  
40 artificial neural networks (ANNs) approach due to the additional time spent on ANN  
41 development. Conversely, the computational costs of forecasting are considerably  
42 reduced by the neural networks compared with the process-based model, with a  
43 decrease in hours of 25, 600, 3900, and 31633 times for forecasting 1 h 1 day, 1 month  
44 and 1 bathing season, respectively. Therefore, the longer the forecasting period, the  
45 greater the reduction in computational time by artificial neural networks.

46

**47 Keywords**

48 Bathing water quality; *Escherichia coli* (*E. coli*); Hydrodynamic-bacteriological model;  
49 Machine learning; Eo Estuary

50

## 51 1. Introduction

52 Estuarine water quality is strongly impacted by anthropogenic activities (García et al.,  
53 2010; De los Ríos et al., 2016; Bárcena et al. 2017a). For instance, people are very  
54 concerned about bathing water quality since estuarine waters are used not only for  
55 recreational activities but also for others including transport and food production and as  
56 a repository for sewage and industrial waste (Bárcena et al. 2017b). Therefore, faecal  
57 pollution is one of the most relevant issues in the evaluation and management of  
58 estuarine water quality since it may cause socio-economic and environmental losses  
59 such as infections and diseases, beach degradation, or closures of shellfish-growing  
60 areas (de Brauwere et al., 2014).

61 In Europe, Directive (2006/7/EC) sets the quality of bathing waters based on two faecal  
62 indicator organisms (FIOs): *intestinal Enterococci* (*Enterococci*) and *Escherichia coli*  
63 (*E. coli*). The limit values of *E. coli* for transitional waters are 250 *E. coli*/100 ml  
64 (excellent quality) and 500 *E. coli*/100 ml (good quality) based upon a 95<sup>th</sup> percentile  
65 evaluation and 500 *E. coli*/100 ml (sufficient quality) based upon a 90<sup>th</sup> percentile  
66 evaluation. Although laboratory analyses are the most accurate and reliable methods for  
67 evaluating water quality, they require between 24 and 48 h to provide results (Rompré  
68 et al., 2002); as a result, the public may be exposed to elevated FIO concentrations  
69 during the time required to produce an analytical result. Furthermore, these samples are  
70 usually collected either 8 h to 13 h, neglecting the influence of diurnal variation in FIO  
71 concentration (Boehm et al., 2002; Thoe et al., 2014). Thus, environmental managers  
72 are not able to evaluate faecal pollution variability over time. Although these issues  
73 could be overcome by increasing the temporal resolution and window of sampling, the  
74 time-consuming laboratory methods will continue to be a bottleneck for the rapid  
75 detection of critical conditions such as pollution events.

76 Therefore, real-time methods have been developed to monitor *E. coli* concentrations  
77 based on flow cytometry (Besmer et al., 2014), ATP assays (Vang et al., 2014), online  
78 optical sensors (Højris et al., 2016), or quantitative PCR (Walker et al., 2017).  
79 However, the current high costs associated with these methods are a drawback to their  
80 implementation at bathing sites for most health administrations.

81 Process-based models have also been used to evaluate the spatial and temporal  
82 evolution of FIOs, considering the diurnal variation in FIO concentration (López et al.,  
83 2013; Bedri et al., 2014; Wang et al., 2016; Huang et al., 2017). Notwithstanding the  
84 increase in computer power, process-based model complexity is also growing at the  
85 same rate, if not faster (Washington et al., 2009), suggesting that computational  
86 requirements will be an impediment to applications where a quick answer is required,  
87 e.g., the nowcasting of FIO concentrations for managing temporal closures of bathing  
88 sites.

89 Accordingly, different techniques have been proposed in the last few years to overcome  
90 the large computational burden associated with process-based models, called dynamic  
91 emulation modelling (Castelletti et al., 2012). An emulator is a computationally  
92 efficient low-order model identified from the original large model and then used to  
93 replace it for computationally intensive applications. In the field of bathing water  
94 quality monitoring, data-based models such as ANNs may efficiently detect and analyse  
95 FIO concentrations and, hence, serve as surrogates for computationally demanding  
96 water quality models (Tufail et al., 2008; Shaw et al. 2017). Thus, ANNs may help  
97 reduce the computational costs of bathing water quality management, preserving the  
98 accuracy of results when large datasets are available for model fitting (van der Merwe et  
99 al., 2007; Maier et al., 2010; Shaw et al. 2017). ANNs have been used for nowcasting  
100 and forecasting of FIO concentrations in rivers (Chandramouli et al., 2007; Tufail et al.,

101 2008; Motamarri and Boccelli, 2012), reservoirs (Mas and Ahlfeld, 2007), coastal areas  
102 (He and He, 2008; Thoe et al., 2012; Thoe et al., 2014; Zhang et al., 2015), and surface  
103 runoff (Kim et al., 2008; Kazemi Yazdi and Scholz, 2010). However, their application  
104 as emulators of process-based models in estuaries has not been widely investigated.

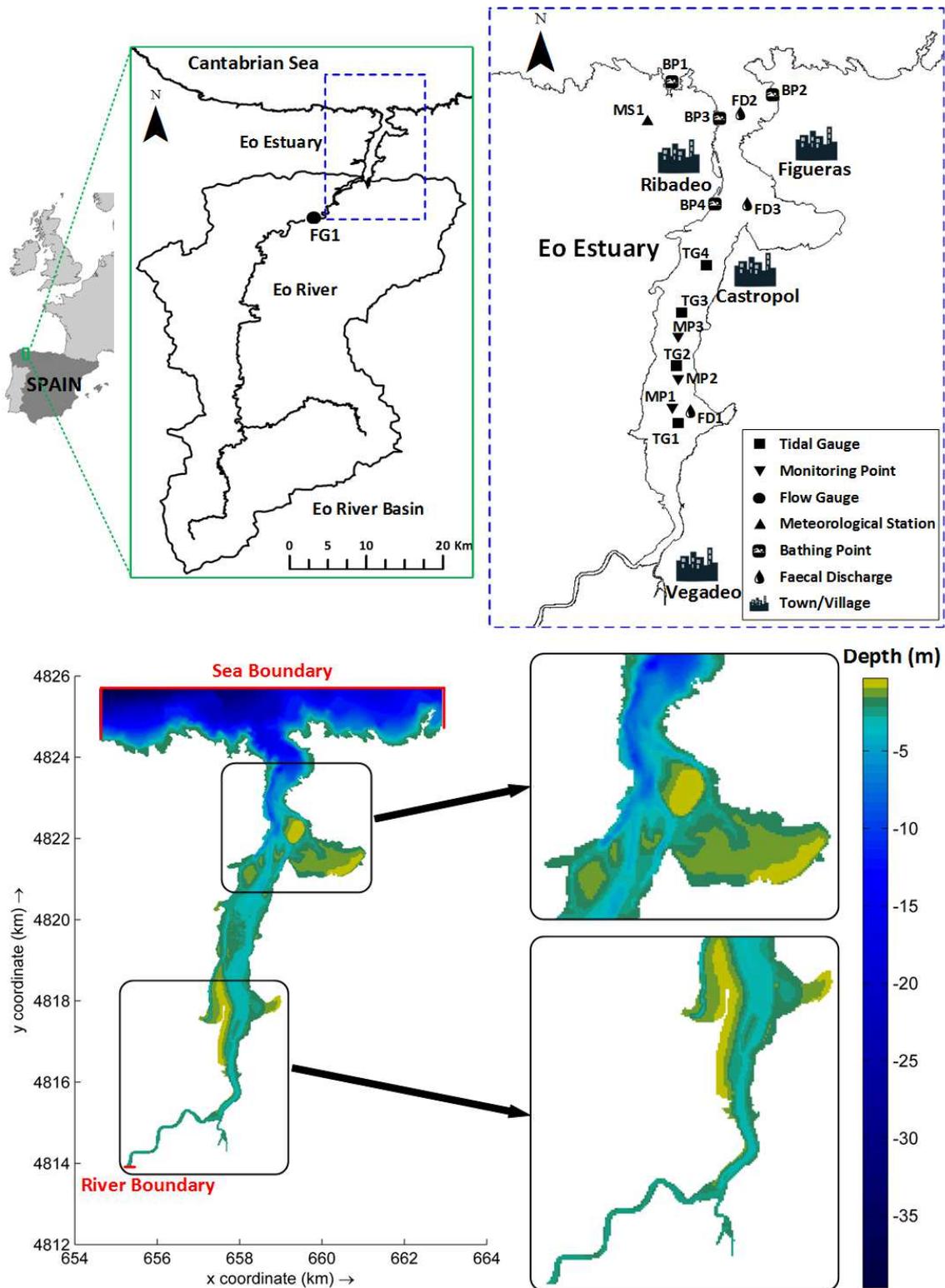
105 Within this context, the main objective of this study is to develop a method to compute  
106 the spatial and temporal evolution of FIO concentrations in estuaries using ANNs  
107 trained by a calibrated hydrodynamic-bacteriological model. This method integrates the  
108 benefits of the three approaches used to calculate *E. coli* concentrations: (1) the  
109 accuracy and reliability of field measurements; (2) the spatial and temporal resolution of  
110 numerical modelling; and (3) the decrease in computational costs caused by ANNs  
111 accompanied by preserved accuracy of the results.

112

## 113 **2. Material and methods**

### 114 **2.1. Study area and available data**

115 The Eo Estuary (see Fig. 1), located on the northwestern coast of Spain (43°28'33"N;  
116 7°00'03"W), is a shallow mesotidal system with a semidiurnal tidal range varying from  
117 1.2 m to 4.8 m (de Paz et al., 2008). This estuary has been historically divided into two  
118 regions. The first region, extending from the estuarine mouth to Vegadeo, presents an  
119 N-S alignment over a length of 9.9 km and an average width of 800 m (Flor et al.,  
120 1993). The second region, extending from Vegadeo to San Tirso de Abres (FG1),  
121 presents NNE-SSW alignment over a length of 4.5 km and a width varying from 95 to  
122 571 m (Flor et al., 1993). The Eo River Basin occupies a catchment area of 819 km<sup>2</sup>  
123 with a length of 9 km. The freshwater inflow under natural conditions varies from  
124 approximately 0.6 to 425 m<sup>3</sup>/s, with an annual average of 19.61 m<sup>3</sup>/s and ranging from  
125 7.93 m<sup>3</sup>/s in summer to 39.67 m<sup>3</sup>/s in winter (Piedracoba et al., 2005).



126

127 Fig. 1. Map of the Eo River Basin and the Eo Estuary, indicating the locations of the  
 128 tidal gauges (TG1-TG4), monitoring points (MP1-MP3), flow gauge (FG1),  
 129 meteorological station (MS1), bathing water quality control points (BP1-BP4), and  
 130 faecal discharges (FD1-FD3), used in the setup of the predictive tools. Bathymetry is

131 also presented with a zoomed-in image of the outer and inner areas of the Eo Estuary  
132 (UTM projection ED50 30N).

133

134 At the study site, the water-related anthropic uses are recreational (e.g., swimming,  
135 sailing, and sun bathing) and economical (e.g., fishing, aquaculture, and shellfishing),  
136 and the bathing season occurs from May 1<sup>st</sup> to September 30<sup>th</sup>. Four beaches are  
137 monitored to classify their bathing quality status as regulated by Directive (2006/7/EC):  
138 Rocas Blancas (BP1), Arnao (BP2), O Cargadeiro (BP3), and Os Bloques (BP4). Due to  
139 the villages settled around the Eo Estuary, three sources of faecal pollution were  
140 discharged into the estuarine waters during the bathing seasons of 2013, 2014, and 2015  
141 (see Fig. 1): (1) a wastewater treatment plant with biological treatment, collecting  
142 sewage from Vegadeo (FD1); (2) a submarine outfall without water treatment,  
143 collecting sewage from Castropol and Figueras (FD2); and (3) a breach in the  
144 submarine outfall in place since 2010 (FD3), constituting 24% of the FD2 flow. Dry  
145 weather conditions prevail during bathing seasons since most of the rain is received  
146 between October and April (del Río et al., 2011). Thus, storm runoff is mainly diverted  
147 to FD1 and FD2 during the bathing seasons. The other potential flowing, land-based,  
148 FIO sources (storm water discharges) are not considered in the present study as they  
149 have no flow or very low flow during bathing seasons and are not believed to affect the  
150 estuarine bathing water quality.

151 Regarding the available data, we retrieved information from five sources: (1) a field  
152 survey (FLTQ, 1990); (2) the Automatic Information System of the Cantabrian  
153 Hydrographic Confederation (SAI), available online at <http://www.chcantabrico.es>; (3)  
154 the Copernicus Marine Environment Monitoring Service (CMEMS), available online at  
155 <http://marine.copernicus.eu>; (4) the Meteorological Observation and Weather Forecast

156 Service of Galicia (MeteoGalicia), available online at [www.meteogalicia.es](http://www.meteogalicia.es); and (5) the  
157 Spanish Bathing Water Information System (NAYADE), available online at  
158 <https://nayadeciudadano.msssi.es>.

159 The field survey (FLTQ, 1990) took place from the 21<sup>st</sup> to the 23<sup>rd</sup> of June 1990 and  
160 included the following measurements (see Fig. 1): (1) tidal water levels at 4 points (TG1  
161 to TG4), measured every 5 min with a tidal pressure gauge (Aanderaa WLR-5); (2) river  
162 flows, temperatures, and salinities at 1 point (FG1), measured every 2 h with an  
163 electromagnetic flow meter (Flowmate model 2000) and a limnometric scale; (3) current  
164 speeds and directions at the bottom at 3 points (MP1 to MP3), measured every 5 min  
165 with an automatic current meter (Aanderaa RCM45); and (4) salinities and temperatures  
166 at the bottom at 3 points (MP1 to MP3), measured every 5 min with a CTD device.

167 From the other four sources, we retrieved data from 2013 to 2015, including (1) the  
168 daily time series of flow, salinity, and temperature at the river boundary, measured by  
169 FG1; (2) the hourly time series of salinity and temperature at the sea boundaries,  
170 modelled by the operational Iberian Biscay Irish (IBI) system of the CMEMS (Sotillo et  
171 al., 2015); (3) the hourly time series of solar radiation at the surface, recorded by MS1;  
172 and (4) the *E. coli* concentrations at the 4 monitoring stations, measured by the  
173 NAYADE (see Fig. 1): BP1 - 25 data, BP2 - 25 data, BP3 - 26 data, and BP4 - 24 data.

174 The method for the enumeration of *E. coli* was ISO 9308-1. This method is based on  
175 membrane filtration, subsequent culture on a chromogenic coliform agar medium, and  
176 calculation of the number of target organisms in the sample.

177

## 178 **2.2. Predictive tools**

### 179 *2.2.1. Process-based model*

180 Our modelling approach was implemented in the Delft3D open-source modelling  
 181 framework (<http://oss.deltares.nl/web/delft3d>). First, estuarine hydrodynamics were  
 182 derived from the hydrodynamic module Delft3D-FLOW (Lesser et al., 2004). Second,  
 183 *E. coli* concentrations were computed by means of the transport module D-Water  
 184 Quality (Postma et al., 2003). This coupling has been applied in other studies,  
 185 confirming its ability to simulate hydrodynamics, transport and mixing in complex  
 186 aquatic systems (Los et al., 2014; Wang et al., 2016; Roberts and Villegas, 2017).  
 187 In this work, the formulation proposed by Mancini (1978) was adopted to simulate the  
 188 bacterial mortality, assuming the following conditions: (1) *E. coli* was only present in  
 189 the water column, without accumulating in or resuspending from sediment; (2) *E. coli*  
 190 did not grow in the water column; (3) *E. coli* mortality was included as a temperature-  
 191 dependent process, formulated based on first-order kinetics; and (4) the *E. coli* mortality  
 192 rate was enhanced by salinity and UV radiation in an additive way. Accordingly,  
 193 mortality was calculated with Eq. (1) to Eq. (5).

$$194 \quad CF_{decay} = K_M \cdot C_{CF} \quad (1)$$

$$195 \quad K_M = (K_B + K_{Cl}) \cdot K_T^{(T-20)} + K_R \quad (2)$$

$$196 \quad K_{Cl} = k_{Cl} \cdot C_{Cl} \quad (3)$$

$$197 \quad K_R = k_{rd} \cdot DL \cdot f_{uv} \cdot I_0 \frac{(1-e^{-\varepsilon H})}{\varepsilon H} \quad (4)$$

$$198 \quad \varepsilon = \frac{1.8}{SD} \quad (5)$$

199 where  $CF_{decay}$  is the concentration of *E. coli* over time (*E. coli*/m<sup>3</sup>·days);  $K_M$  is the first-  
 200 order mortality rate (days<sup>-1</sup>);  $C_{CF}$  is the *E. coli* concentration (*E. coli*/m<sup>3</sup>);  $K_B$  is the basic  
 201 mortality rate (days<sup>-1</sup>);  $K_{Cl}$  is the chloride-dependent mortality rate (days<sup>-1</sup>);  $T$  is the  
 202 temperature (°C);  $K_T$  is the temperature-dependent mortality rate (-);  $K_R$  is the radiation-  
 203 dependent mortality rate (days<sup>-1</sup>);  $k_{Cl}$  is the chloride-dependent mortality constant

204 ( $\text{m}^3/\text{g}\cdot\text{days}$ );  $C_{cl}$  is the chloride concentration ( $\text{g}/\text{m}^3$ );  $k_{rd}$  is the radiation-dependent  
205 mortality constant ( $\text{m}^2/\text{W}\cdot\text{days}$ );  $DL$  is the day-length (days);  $f_{uv}$  is the fraction of UV  
206 light in visible light (-);  $I_0$  is the daily solar radiation at the water surface ( $\text{W}/\text{m}^2$ );  $\varepsilon$  is  
207 the extinction of UV radiation ( $\text{m}^{-1}$ );  $H$  is the water depth (m); and  $SD$  is the Secchi disk  
208 depth (m).

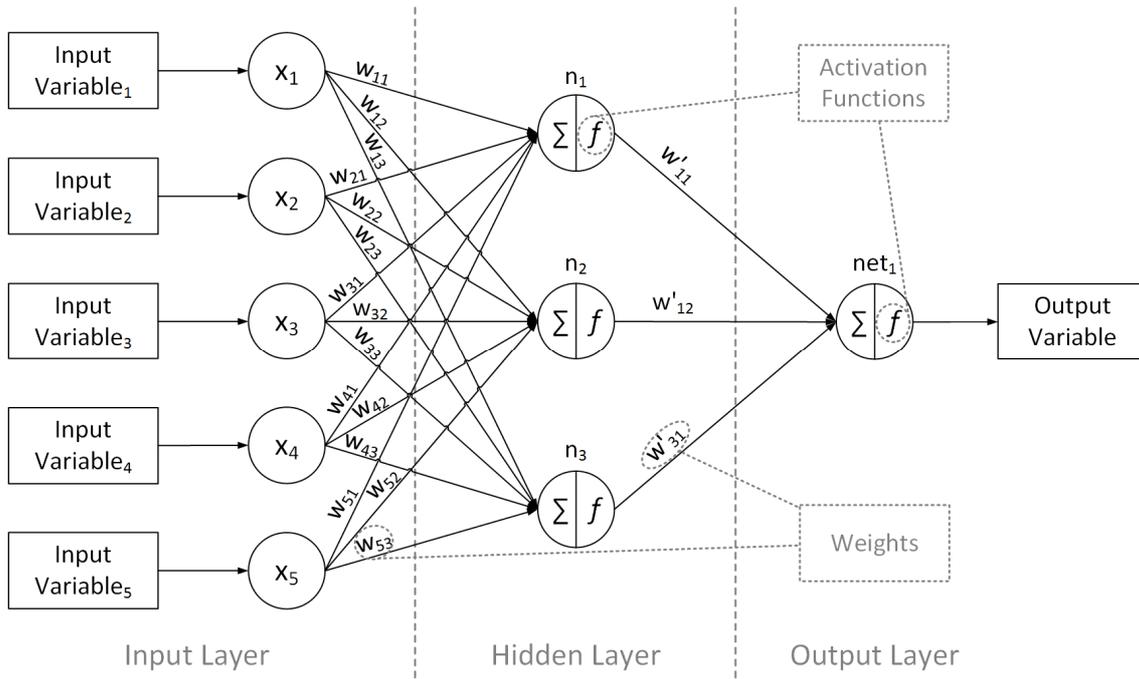
### 209 2.2.2. Artificial neural networks

210 The basic structure of ANNs is characterized by their architecture, activation functions,  
211 and training algorithm. The ANN architecture consists of three layers (see Fig. 2): one  
212 input layer, one hidden layer that is usually composed of one layer but can be built up  
213 with more sublayers (deep learning), and one output layer (Khalil et al., 2011). Every  
214 layer has several nodes that are responsible for transmitting the information from one  
215 layer to the next layer, although neither lateral connection within any layer nor feedback  
216 connection is possible (arrows in Fig. 2).

217 The functioning of the ANN is as follows: Each node in the input layer supplies  
218 information to every node in the hidden layer through the “synapses”. A summation of  
219 the contribution of each node in the input layer is performed in each node of the hidden  
220 layer by applying an activation function to transform the obtained value. Then, every  
221 value of every node in the hidden layer is multiplied by its weight and transmitted to the  
222 output node, where another summation is performed by applying a new activation  
223 function to obtain the final output (Wu et al., 2014).

224 ANNs need to be trained to assign weights accurately and, consequently, minimize  
225 errors in the output results (Motamarri and Bocelli, 2012). This task depends on the  
226 training method and the ratio of the training subset, validation subset, and test subset to  
227 the total data ( $T:V:T$ ): the training subset is used to estimate unknown connection  
228 weights between neurons, the validation subset is used to assess the generalization

229 ability of the trained network, and the testing subset is used to decide whether early  
 230 termination is needed to avoid overfitting (Maier et al., 2010).



231

232 Fig. 2. Schematic view of a feedforward neural network with five nodes in the input  
 233 layer, three nodes in the hidden layer and one node in the output layer. Synapses are  
 234 oriented from left to right.

235

### 236 2.3. Performance metrics of predictive tools

#### 237 2.3.1. Evaluation of predictive tools

238 The predictive tools' performance was evaluated by three error measurements. First,  
 239 bias was calculated as the difference between the modelled results and the observed  
 240 values on a given date. Second, the coefficient of determination ( $R^2$ ) was determined as  
 241 expressed in Eq. (6).

242

$$R^2 = \frac{\sum_{i=1}^N (S_i - \bar{R}_i)^2}{\sum_{i=1}^N (R_i - \bar{R}_i)^2} \quad (6)$$

243 where  $R_i$  is the  $i$ -field data of the measurements,  $S_i$  is the  $i$ -model data of the  
 244 simulations (process-based or ANN),  $\bar{R}$  is the average of the measurements, and  $i$  is the  
 245  $i^{th}$  value from 1 to N measurements (laboratory analyses).

246 Third, the error between the series was calculated using the model efficiency (CE),  
 247 developed by Nash and Sutcliffe (1970), as displayed in Eq. (7).

$$248 \quad CE = 1 - \frac{\sum_{i=1}^N (R_i - S_i)^2}{\sum_{i=1}^N (R_i - \bar{R})^2} \quad (7)$$

249 The CE ranges between  $-\infty$  and 1.0 (1.0 inclusive), with CE=1 being the optimal value.  
 250 Values between 0.0 and 1.0 are generally viewed as acceptable levels of performance,  
 251 whereas values  $<0.0$  indicate that the mean observed value is a better predictor than the  
 252 simulated value, which indicates unacceptable performance. Depending on the CE  
 253 value, the comparison is considered acceptable (poor) if  $CE < 0.4$ , acceptable (-) if  
 254  $0.4 \leq CE < 0.6$ , acceptable (convenient or good) if  $0.6 \leq CE < 0.8$ , and acceptable (excellent)  
 255 if  $CE \geq 0.8$ .

### 256 2.3.2. Accuracy of predictive tools for bathing water quality management

257 The contingency table (Table 1a) and its error metrics (Table 1b) were employed to  
 258 assess the accuracy of predictive tools in predicting the compliance with and/or  
 259 exceedance of the FIO concentrations at specific thresholds (Manzato, 2007; Bennett et  
 260 al., 2013; Bedri et al. 2016). Contingency tables establish the number of occurrences  
 261 where predictive tools have generated correct predictions (see Table 1a): (1) the  
 262 exceedance of specific values (hits); (2) the occurrences of correct negatives; (3) the  
 263 number of alarms missed by the model; and (4) the number of false alarms. Therefore,  
 264 an ideal model would have data in only the hits and correct negatives categories. Table  
 265 1b lists the error metrics of the contingency table used in the current study along with  
 266 their limits and ideal values.

		Observed Exceedances		
		yes	no	
Predicted Exceedances	yes	Hits	False alarms	Predicted yes
	no	Misses	Correct negatives	Predicted no
		Observed yes	Observed no	Total

a) Contingency table

Metric	Formula	Range of values	Ideal value	Notes
Accuracy (fraction correct)	$\frac{Hits + Correct\ negatives}{Total}$	0-1	1	It is heavily influenced by the most common category, usually “no event”.
Bias score (frequency bias)	$\frac{Hits + False\ alarms}{Hits + Misses}$	0-∞	1	Indicates if the model tends to under- (<1) or over- (>1) estimate.
Hit rate (Probability of detection)	$\frac{Hits}{Hits + Misses}$	0-1	1	Sensitive to hits but ignores false alarms. Good for rare events.
False alarm rate (Probability of false detection)	$\frac{False\ alarms}{False\ alarms + Correct\ negatives}$	0-1	0	Sensitive to false alarms but ignores misses.
Success index	$\frac{1}{2} \cdot \left[ \frac{Hits}{Hits + Misses} + \frac{Correct\ negatives}{Total} \right]$	0-1	1	Weights equally the ability of the model to correctly detect occurrences and non-occurrences of events.
Threat score	$\frac{Hits + Correct\ negatives}{Total}$	0-1	1	Measures the fraction of observed cases that were correctly modelled. It penalizes both misses and false alarms.

b) Error metrics

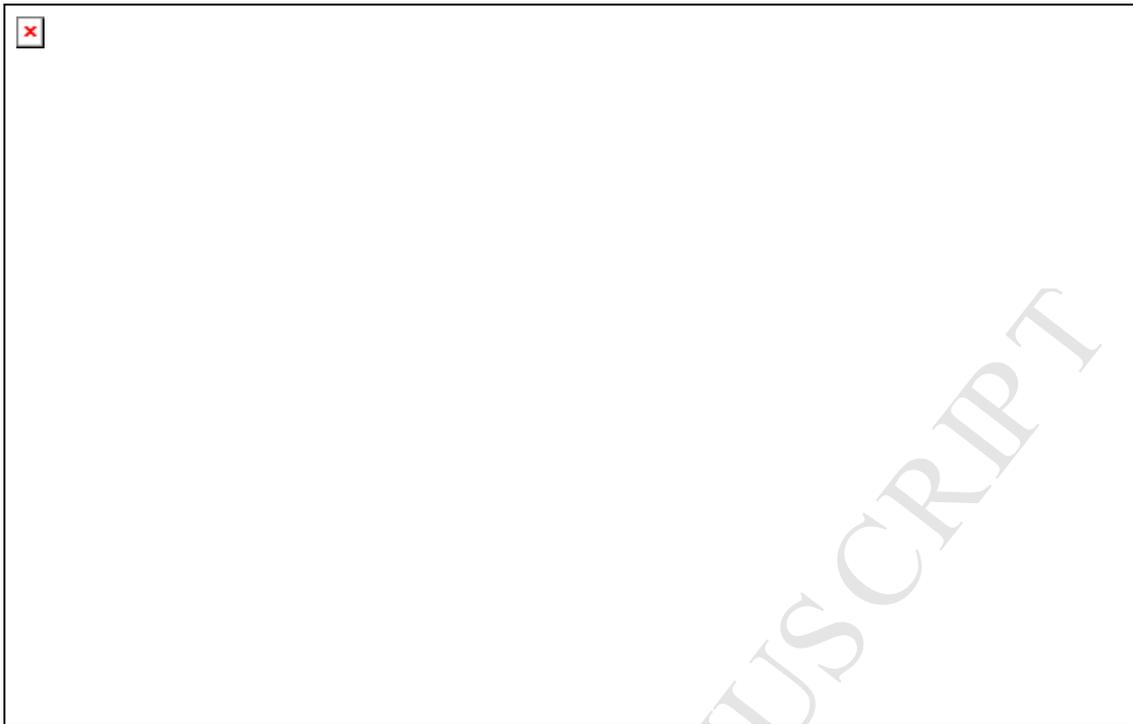
267

268 Table 1. (a): Contingency table to assess the accuracy of predictive tools for the  
 269 prediction of faecal indicator organism (FIO) concentrations. (b): Error metrics of the  
 270 contingency table (Source: Manzato, 2007; Bennett et al., 2013; Bedri et al. 2016).

271

## 272 2.4. Methodology to develop artificial neural networks for the analysis of bathing 273 water quality in estuaries

274 The overall approach, illustrated in Fig. 3, integrates a coupled hydrodynamic-  
 275 bacteriological model previously calibrated with field data at the bathing sites into a  
 276 real-time framework by using ANNs trained on the numerical model outputs (targets).

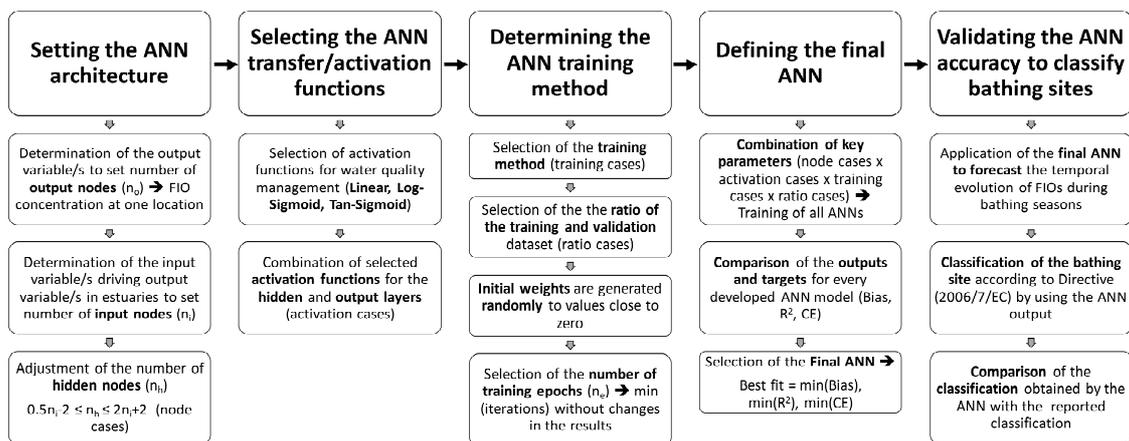


277

278 Fig. 3. Overall methodological approach.

279

280 Since critical decisions must be made when developing an ANN, we use a five-step  
 281 method (see Fig. 4).



282

283 Fig. 4. Schematic view of the proposed methodology to develop artificial neural  
 284 networks to analyse bathing water quality criteria in estuaries.

285

286 *2.4.1. Setting the ANN architecture*

287 Since the ANN output is the evolution of FIO concentration at one bathing site, the  
 288 number of nodes in the output ( $n_o$ ) is one.

289 Bearing in mind that ANN models will be emulators of process-based models, ANN  
 290 inputs should be process-based model inputs, i.e., boundary conditions, sinks and  
 291 sources. Thus, the input variables are hydrodynamic forcings, water constituents at open  
 292 boundaries, atmospheric forcings, and faecal discharges, and the number of nodes in the  
 293 input ( $n_i$ ) should therefore be determined from this preliminary selection based on site-  
 294 specific conditions.

295 The number of nodes in the hidden layer ( $n_h$ ) should be less than twice  $n_i$  (Motamarri  
 296 and Bocelli, 2012); we propose Eq. (8) to set  $n_h$ .

$$297 \quad 0.5 \cdot n_i - 2 \leq n_h \leq 2 \cdot n_i + 2 \quad (8)$$

#### 298 *2.4.2. Selecting the ANN transfer/activation functions*

299 Three different activation functions are widely used (Jiang et al., 2013) for the transfer  
 300 between the input and hidden layer ( $f_h$ ) and the hidden and output layers ( $f_o$ ): (1) the  
 301 linear transfer function (Eq. (9)); (2) the log-sigmoid transfer function (Eq. (10)); and  
 302 (3) the tan-sigmoid transfer function (Eq. (11)). Generally, sigmoid functions are used  
 303 for pattern recognition, whereas linear functions are used for fitting.

$$304 \quad f(x) = x \quad (9)$$

$$305 \quad g(x) = \frac{1}{1+e^{-x}} \quad (10)$$

$$306 \quad h(x) = \frac{2}{1+e^{-2x}} - 1 \quad (11)$$

#### 307 *2.4.3. Determining the ANN training method*

308 Several methods are used for training ANNs, with the Levenberg-Marquardt method  
 309 (Hagan and Menhaj, 1994) and the backpropagation algorithm (Rumelhart et al., 1986)  
 310 being the most common. Additionally, the initial weights are generated randomly to  
 311 obtain values close to zero, and the  $T:V:T$  ratio should be adjusted by trial and error

312 (Wu et al., 2014). Lastly, the number of training epochs ( $n_e$ ) is decided based on trials  
313 by observing the conditions under which ANN training and testing results are both  
314 independent of the number of iterations (Tufail et al., 2008).

#### 315 *2.4.4. Defining the final ANN*

316 The key parameters are combined to develop several ANN models ( $n_h$ ,  $f_h$ ,  $f_o$ , training  
317 methods, and  $T:V:T$ ). Next, these models are trained, and the ANN model displaying  
318 the lowest error metric between outputs and targets (final ANN) is chosen (Zou et al.,  
319 2007).

#### 320 *2.4.5. Validating the ANN accuracy to classify bathing sites*

321 The final ANN model is applied to forecast FIO concentrations at the bathing site  
322 during bathing seasons. Next, the ANN results are classified according to the standard  
323 values set in Directive (2006/7/EC) and compared with the official reported  
324 classification.

325

## 326 **2.5. Setup of predictive tools in the Eo Estuary**

### 327 *2.5.1. Setup of the process-based model*

328 The Eo Estuary was represented horizontally using a 3D rectangular mesh grid  
329 composed of 332x640 grid cells with a horizontal resolution of 25x25 m<sup>2</sup>, 3 vertical  $\sigma$ -  
330 layers equally spaced along the water column, and the bathymetry displayed in Fig. 1.

331 The hydrodynamic calibration was performed for the period between the 21<sup>st</sup> and 24<sup>th</sup> of  
332 June 1990, including a spin-up period of 30 days to allow the hydrodynamic and  
333 thermohaline variables to interact and adjust themselves. Once the hydrodynamic  
334 module was calibrated, the hydrodynamics of the 2013, 2014, and 2015 bathing seasons  
335 driven by the tidal action and river flows (see Fig. S1 in the supplementary materials)  
336 were simulated as required inputs for the water quality module calibration. For a more

337 detailed description of the hydrodynamic module setup, readers are referred to the  
338 supplementary materials.

339 Next, we implement the transport module in the same grid, the same time step (6 s), the  
340 same four open boundaries (see Fig. 1), and the same spin-up period of 30 days used in  
341 the hydrodynamic module setup (see the supplementary materials). The initial condition  
342 was 0 *E. coli*/100 ml in the whole model domain. Based on the available data at the sea  
343 and river boundaries, the mean concentration of these measurements was used as a  
344 constant boundary condition, with 0 and 850 *E. coli*/100 ml at the sea and river  
345 boundaries, respectively. Table 2 lists the parameters used in the calculation of the *E.*  
346 *coli* transport and mixing in the Eo Estuary.

Constant	Value	Units	Source
$D_H, D_V$	Time series	m <sup>2</sup> /s	Hydrodynamic module
$T$	Time series	°C	Hydrodynamic module
$C_{Cl}$	Time series	g/m <sup>3</sup>	Hydrodynamic module
$I_0$	Time series	W/m <sup>2</sup>	Meteorological station (MS1)
$K_B$	0.8	1/days	Chapra (1997)
$DL$	1	days	(*)
$f_{uv}$	0.12	-	Diffey (2002)
$\varepsilon$	0.35	1/m	FLTQ (1990); Eq. (5)
$K_T$	1.07	-	This study (calibration)
$k_{rd}$	0.086	m <sup>2</sup> /W·days	This study (calibration)
$k_{Cl}$	2·10 <sup>-4</sup>	m <sup>3</sup> /g·days	This study (calibration)

347 (\*) Day-night variations are considered within the irradiation ( $I_0$ ).

348 Table 2. Model parameters used in the calculation of *E. coli* transport and mixing.

349

350 Based on the data from Metcalf and Eddy, Inc. (2003) for a single day, the hourly flow  
351 of three faecal discharges (FD1-FD3) was introduced (see Fig. S2 in the supplementary  
352 materials). The mean discharge flow (in m<sup>3</sup>/s) was 0.00347, 0.00524 and 0.00165 for  
353 FD1, FD2 and FD3, respectively. The constant discharge concentration (in *E. coli*/100  
354 ml) was 10<sup>6</sup>, 10<sup>8</sup> and 10<sup>8</sup> for FD1, FD2 and FD3, respectively. Finally, a constant

355 salinity and temperature of 0 psu and 17 °C, respectively, were specified for the three  
356 discharges.

357

### 358 2.5.2. Setup of the artificial neural network

359 ANNs were developed for BP1, BP2, BP3, and BP4. First, the output variable was the  
360 *E. coli* concentration at every bathing site; thus,  $n_o$  was set to one for every ANN.  $n_i$   
361 was fixed by the process-based model inputs, with a value of 9 in the Eo Estuary: water  
362 level, salinity and temperature at the sea boundary; flow and temperature at the river  
363 boundary; solar radiation; and the flow of the three faecal discharges (FD1-FD3). Note  
364 that the model inputs obtained with constant values were not included as input variables  
365 in the ANN models, i.e., salinity at the river boundary (see the supplementary materials)  
366 and salinity, temperature and *E. coli* concentrations of faecal discharges (see subsection  
367 2.5.1). Following Eq. (8), 3, 7, 11, 15, or 19  $n_h$  were selected (5 node cases). Second,  
368 we combined the 3 activation functions, obtaining 9 activation cases. Third, 9 training  
369 methods were tested: BFGS quasi-Newton backpropagation, resilient backpropagation,  
370 scaled conjugate gradient backpropagation, conjugate gradient backpropagation with  
371 Powell-Beale restarts, Levenberg-Marquardt backpropagation, conjugate gradient  
372 backpropagation with Fletcher-Reeves updates, conjugate gradient backpropagation  
373 with Polak-Ribière updates, one step secant backpropagation, and gradient descent with  
374 momentum and adaptive learning rate backpropagation. Fourth, 3  $T:V:T$  ratios were  
375 defined: 60:20:20, 70:15:15, and 80:10:10. Finally, the initial weights used were  
376 generated randomly to obtain values close to zero, and  $n_i$  was set to  $10^3$  for all ANN  
377 models, based on previous trials.

378 For every bathing site, the combination of 5 node cases, 9 activation cases, 9 training  
379 cases, and 3 ratio cases resulted in 1215 ANN models. These models were trained,

380 validated and tested using the hourly evolution of *E. coli* concentration computed by the  
381 process-based model during the bathing seasons of 2013, 2014, and 2015 as targets  
382 (11019 modelled concentration measurements). Next, outputs and targets were  
383 compared by means of bias, CE, and  $R^2$ . The best fits (final ANNs) were obtained with  
384 15  $n_h$ , a tan-sigmoid function for the  $f_h$ , a log-sigmoid function for the  $f_o$ , a Levenberg-  
385 Marquardt backpropagation method, and a  $T:V:T$  ratio of 70:15:15.

386

### 387 **3. Results**

#### 388 **3.1. Hydrodynamics**

389 The results provided by the hydrodynamic module were compared with the available  
390 measurements. For water levels, the bias ranged between -0.04 and 0.10 m, and the CE  
391 ranged between 0.98 and 0.99 (see Fig. S3 in the supplementary materials). For current  
392 velocities, the bias ranged between 0.01 and 0.02 m/s, and the CE ranged between 0.87  
393 and 0.91 (see the left panels of Fig. S4 in the supplementary materials). For salinities,  
394 the bias ranged between -0.39 and -0.29 psu, and the CE ranged between 0.92 and 0.98  
395 (see the right panels of Fig. S4 in the supplementary materials). Overall, these errors  
396 confirmed that the hydrodynamic module satisfactorily reproduced water circulation  
397 and transport throughout the Eo Estuary.

398

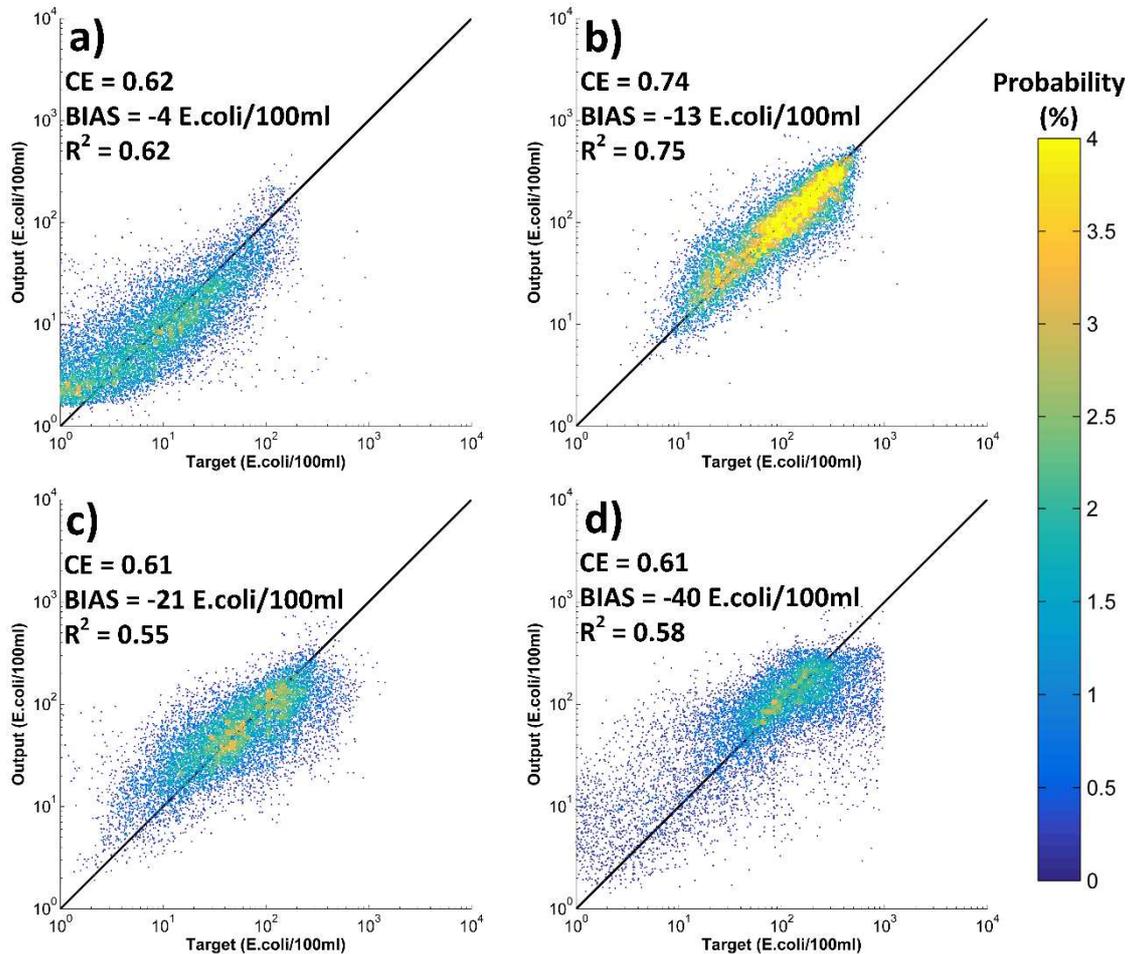
#### 399 **3.2. Predictive tools**

##### 400 *3.2.1. Evaluation of predictive tools*

401 Fig. 5 shows scatter density plots for the *E. coli* concentrations between the outputs  
402 provided by each final ANN model and the targets simulated by the process-based  
403 model at BP1 (a), BP2 (b), BP3 (c), and BP4 (d) for the bathing seasons of 2013, 2014,  
404 and 2015. The colorbar of Fig. 5 displays the occurrence probability of the scatter dots

405 defined by the *E. coli* concentration of targets (process-based model) and outputs (ANN  
 406 model).

407



408

409 Fig. 5. Performance of the final artificial neural networks (outputs) in emulating *E. coli*

410 concentrations (*E. coli*/100 ml) computed by the process-based model (targets) at BP1

411 (a), BP2 (b), BP3 (c), and BP4 (d). The bias,  $R^2$ , and CE magnitudes are also shown for

412 the four bathing sites (BP1-BP4). The colorbar shows the occurrence probability of the

413 scatter dots defined by the *E. coli* concentration of targets (process-based model) and

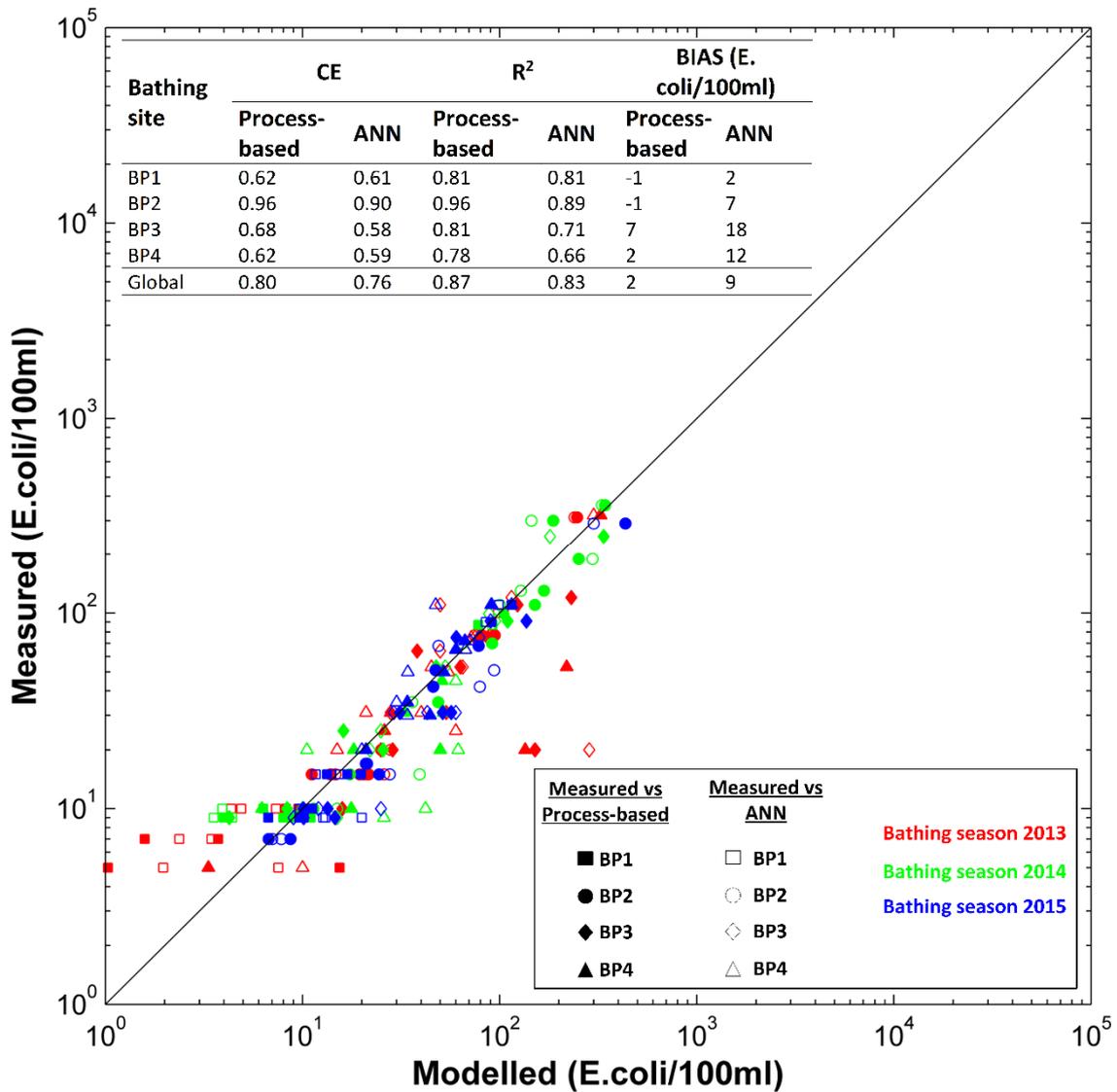
414 outputs (ANN model).

415

416 In the four ANNs, the bias ranged between -4 and -40 *E. coli*/100 ml (the minus sign

417 indicates that the output concentrations were smaller than the target concentrations), the

418  $R^2$  ranged between 0.55 and 0.75, and the CE ranged between 0.61 and 0.74. These  
419 error metrics confirmed that the four ANN models efficiently detected and calculated  
420 the temporal evolution of *E. coli* concentrations, preserving the accuracy of the results.  
421 A detailed examination by location revealed that the best performance (yellow to green  
422 dots in Fig. 5) was obtained at BP2, followed by BP1, BP4, and BP3.  
423 Next, the results provided by the process-based model and the final ANNs were  
424 compared with the available measurements at the four bathing sites during the bathing  
425 seasons of 2013, 2014, and 2015 (see Figs. S5, S6, and S7 in the supplementary  
426 materials, respectively). Fig. 6 shows the performance of the process-based (filled  
427 markers) and ANN (unfilled markers) models in simulating *E. coli* concentrations at  
428 BP1 (squares), BP2 (circles), BP3 (diamonds), and BP4 (triangles) during the bathing  
429 season of 2013 (red), 2014 (green), and 2015 (blue).



430

431 Fig. 6. Performance of the process-based model (filled markers) and the ANN models  
 432 (unfilled markers) in simulating *E. coli* concentrations (*E. coli*/100 ml) at BP1 (squares),  
 433 BP2 (circles), BP3 (diamonds), and BP4 (triangles) during the bathing season of 2013  
 434 (red), 2014 (green), and 2015 (blue). The bias, R<sup>2</sup>, and CE magnitudes are also shown  
 435 for the four bathing sites (BP1-BP4) and considering all the bathing seasons and  
 436 locations at the same time (global).

437

438 As displayed in Fig. 6, the global bias, R<sup>2</sup>, and CE were 2 and 9 *E. coli*/100 ml, 0.87 and  
 439 0.83, and 0.80 and 0.76 for the process-based model and the ANN model, respectively.

440 These metrics indicate a slightly better fit for the process-based model. Moreover, Fig. 6  
 441 summarizes the performance of both predictive tools at the four bathing sites. The  
 442 results showed that the *E. coli* concentrations at BP2 were excellently ( $CE > 0.8$ )  
 443 predicted by both tools ( $R^2 > 0.89$ ). In the case of BP1, predictions were good ( $CE > 0.6$ )  
 444 for both tools ( $R^2 = 0.81$ ), and at BP3 and BP4, the *E. coli* concentrations were  
 445 conveniently ( $CE > 0.6$ ) predicted by the process-based model ( $R^2 > 0.78$ ) and acceptably  
 446 ( $CE > 0.4$ ) predicted by the ANN model ( $R^2 > 0.66$ ). Therefore, these error metrics  
 447 confirm that the process-based model and the ANN model satisfactorily reproduced the  
 448 evolution of *E. coli* concentrations throughout the Eo Estuary, indicating the ability of  
 449 both predictive tools to model the mortality, transport and mixing of *E. coli*.

450

### 451 3.2.2. Accuracy of predictive tools for bathing water quality management

452 The results provided by laboratory analyses, process-based models or ANN models led  
 453 to a bathing water classification of “excellent quality” at the 4 bathing sites (95<sup>th</sup>  
 454 percentile  $< 250$  *E. coli*/100 ml). Moreover, the 95<sup>th</sup> percentile values of the datasets for  
 455 the laboratory analyses, the process-based model, and the ANN model were 98, 97, and  
 456 102 *E. coli*/100 ml at BP1; 232, 245, and 249 *E. coli*/100 ml at BP2; 118, 164, and 211  
 457 *E. coli*/100 ml at BP3; and 110, 109, and 206 *E. coli*/100 ml at BP4, respectively.

458 Table 3 lists the calculated error metrics of the contingency table to assess the accuracy  
 459 of the predictive tools in predicting the compliance with or exceedance of *E. coli*  
 460 concentrations of 500, 250, 125, 50, and 25 *E. coli*/100 ml.

Bathing site	Contingency table (metrics)	Value = 500 <i>E. coli</i> /100 ml		Value = 250 <i>E. coli</i> /100 ml		Value = 125 <i>E. coli</i> /100 ml		Value = 50 <i>E. coli</i> /100 ml		Value = 25 <i>E. coli</i> /100 ml	
		Process-based	ANN	Process-based	ANN	Process-based	ANN	Process-based	ANN	Process-based	ANN
BP1	Accuracy	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00
	Bias score	(*)	(*)	(*)	(*)	(*)	(*)	1.00	1.00	1.00	1.00
	Hit rate	(*)	(*)	(*)	(*)	(*)	(*)	1.00	1.00	1.00	1.00
	False alarm rate	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00
	Success index	(*)	(*)	(*)	(*)	(*)	(*)	0.92	0.92	0.92	0.92

BP2	Threat score	(*)	(*)	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00
	Accuracy	1.00	1.00	0.88	0.88	0.96	1.00	0.96	0.92	0.96	0.84
	Bias score	(*)	(*)	1.33	1.33	0.86	1.00	1.09	1.00	0.93	0.78
	Hit rate	(*)	(*)	0.67	0.67	0.86	1.00	1.00	0.92	0.93	0.78
	False alarm rate	0.00	0.00	0.09	0.09	0.00	0.00	0.07	0.08	0.00	0.00
	Success index	(*)	(*)	0.73	0.73	0.79	0.88	0.76	0.70	0.67	0.53
BP3	Threat score	(*)	(*)	0.88	0.88	0.96	1.00	0.96	0.92	0.96	0.84
	Accuracy	1.00	1.00	0.96	0.96	0.88	0.96	0.77	0.92	0.88	0.96
	Bias score	(*)	(*)	0.00	0.00	0.25	0.50	0.85	0.82	0.83	0.94
	Hit rate	(*)	(*)	0.00	0.00	0.25	0.50	0.69	0.82	0.83	0.94
	False alarm rate	0.00	0.00	0.00	0.00	0.00	0.00	0.15	0.00	0.00	0.00
	Success index	(*)	(*)	0.48	0.48	0.55	0.71	0.56	0.68	0.56	0.62
BP4	Threat score	(*)	(*)	0.96	0.96	0.88	0.96	0.77	0.92	0.88	0.96
	Accuracy	1.00	1.00	1.00	1.00	0.92	1.00	0.90	0.73	0.91	0.83
	Bias score	(*)	(*)	1.00	1.00	0.33	1.00	0.78	0.78	0.88	0.88
	Hit rate	(*)	(*)	1.00	1.00	0.33	1.00	0.78	0.56	0.88	0.82
	False alarm rate	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.15	0.00	0.17
	Success index	(*)	(*)	0.98	0.98	0.60	0.98	0.67	0.53	0.57	0.52
	Threat score	(*)	(*)	1.00	1.00	0.92	1.00	0.90	0.73	0.91	0.83

461 (\*) Indeterminate form 0/0.

462 Table 3. Computed metrics for the assessment of the accuracy of the predictive tools in  
 463 predicting compliance with/exceedance of the *E. coli* values of 500, 250, 125, 50, and  
 464 25 *E. coli*/100 ml.

465

466 Regardless of the metric in Table 3 used, the predictive tools presented the following  
 467 pattern of performance: (1) the performances of the predictive tools for any  
 468 concentration value was the same at BP1, with a success index of 0.92; (2) the  
 469 predictive tools exhibited the same performance for the values of 500 and 250 *E.*  
 470 *coli*/100 ml, with a success index for the value of 250 *E.coli*/100 ml of 0.73, 0.48, and  
 471 0.98 at BP2, BP3, and BP4, respectively; (3) the ANN models performed better than the  
 472 process-based model for the value of 125 *E. coli*/100 ml, with a success index of the  
 473 process-based and ANN models of 0.79-0.88, 0.55-0.0.71, and 0.60-0.98 at BP2, BP3,  
 474 and BP4, respectively; and (4) the process-based model performed better than the ANN  
 475 models for low values (50 and 25 *E. coli*/100 ml) at BP2 and BP4 and worse than these  
 476 models for low values at BP3. For instance, the success index of the process-based and  
 477 the ANN models for the value of 50 *E. coli*/100 ml was 0.76-0.70, 0.56-0.68, and 0.67-

478 0.53 at BP2, BP3, and BP4, respectively. Overall, these metrics indicated that the  
 479 process-based and ANN models satisfactorily predicted the compliance  
 480 with/exceedance of *E. coli* concentrations of 500, 250, 125, 50, and 25 *E. coli*/100 ml  
 481 and, hence, adequately classified the bathing sites located in the Eo Estuary.

482

### 483 3.3. Configuration and computational trade-off of artificial neural networks

484 The final ANN configuration was obtained with 15  $n_h$ , a tan-sigmoid function for the  
 485  $f_h$ , a log-sigmoid function for the  $f_o$ , a Levenberg-Marquardt backpropagation method,  
 486 and a  $T:V:T$  ratio of 70:15:15. Table 4 summarizes the configuration of ANN models  
 487 developed in other studies, including the predicted FIO,  $n_i$ ,  $n_h$ ,  $f_h$ ,  $f_o$ , training method,  
 488  $n_e$ ,  $T:V:T$ , and  $R^2$ .

Study	FIO(*)	$n_i$	$n_h$	$f_h(**)$	$f_o(**)$	Training method	$n_e$	$T:V:T$	$R^2$
Chandramouli et al. (2007)	FC	7	9	Log	Log	Back-propagation	(***)	75:15:10	0.63-0.94
Mas and Ahlfeld (2007)	FC	6	16	Tan	Tan	Levenberg-Marquardt	$10^3$	64:16:20	(***)
Kim et al. (2008)	EC	3	1	Tan	Tan	Back-propagation	$5 \cdot 10^4$	72:8:20	0.90-0.96
He and He (2008)	TC	7	3	(***)	(***)	Back-propagation	(***)	56:24:20	0.79
He and He (2008)	FC	12	6	(***)	(***)	Back-propagation	(***)	56:24:20	0.82
He and He (2008)	EN	7	8	(***)	(***)	Back-propagation	(***)	56:24:20	0.86
Tufail et al. (2008)	EC	2	4	Log	Log	Back-propagation	$10^4$	80:20:(***)	0.58-0.73
Kazemi Yazdi and Scholz (2010)	EN	4	8	Tan	Tan	Levenberg-Marquardt	$10^3$	65:15:20	0.15-0.80
Keeratipibul et al. (2011)	EC	6	5	Tan	Log	Back-propagation	(***)	70:30:(***)	0.72
Thoe et al. (2012)	FC	7	5	Log	Lin	Gradient descent with momentum	$10^3$	60:20:20	0.29-0.75
Motamarri and Boccelli, (2012)	FC	5	6	Tan	Lin	Levenberg-Marquardt	$10^3$	99:1 (leave-one-out)	(***)
Thoe et al. (2014)	FC	12	5	Log	Lin	Gradient-descent	$2 \cdot 10^4$	60:20:20	0.38-0.58
Zhang et al. (2015)	FC	14	(***)	(***)	(***)	Back-propagation	(***)	60:20:20	0.68
This study (2018)	EC	9	15	Tan	Log	Levenberg-Marquardt	$10^3$	70:15:15	0.55-0.75

489 (\*) FC: *Faecal coliform*, TC: *Total coliform*, EC: *E. coli*, EN: *Intestinal enterococci*.

490 (\*\*) Log: Log-sigmoid, Tan: Tan-sigmoid, Lin: Linear.

491 (\*\*\*) Non-specified in the study.

492 Table 4. Review of previous research predicting faecal indicator organisms (FIOs) with  
493 multilayer feedforward networks consisting of one input layer, one hidden layer, and  
494 one output layer.

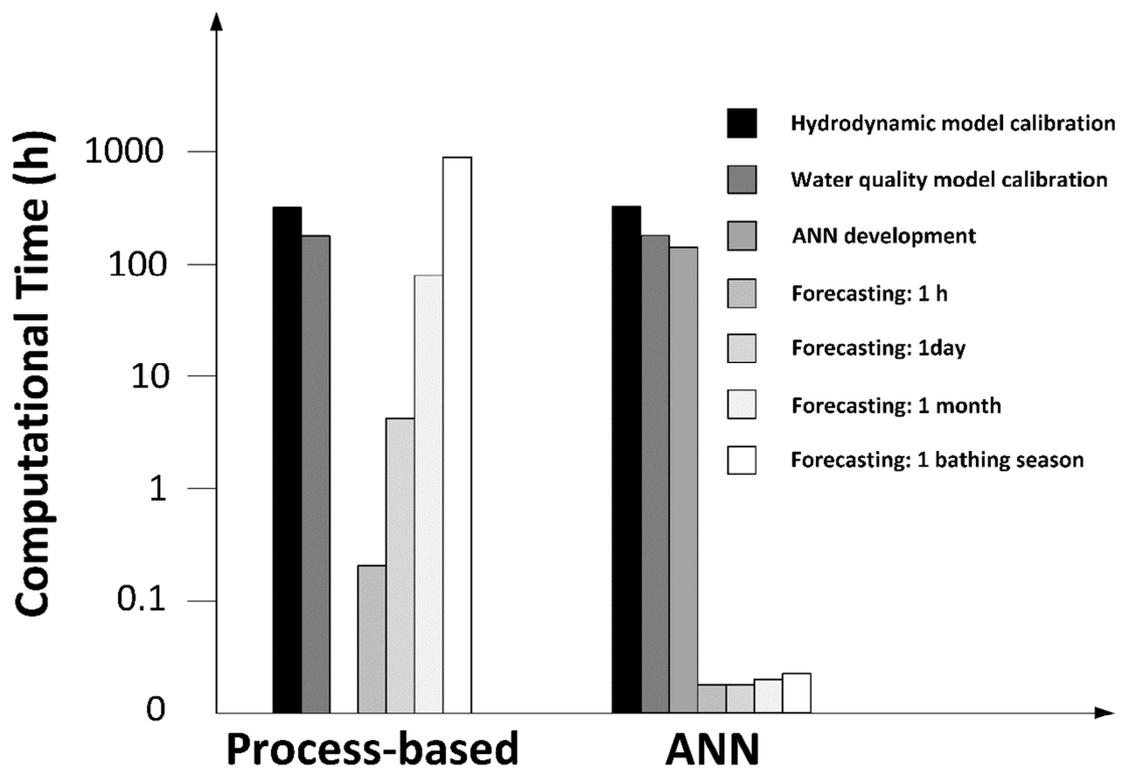
495

496 As displayed in Table 4, ANN models were applied to predict FC (50%), EC (29%), EN  
497 (14%), and TC (7%) concentrations. The ratio between  $n_h$  and  $n_i$  ( $n_h:n_i$ ) ranged from  
498 0.33 to 2.66, with a mean value of 1.17. For  $f_h$ , the log-sigmoid, tan-sigmoid and linear  
499 functions were used 4, 6, and 0 times, respectively. In the case of  $f_o$ , these functions  
500 were used 4, 3, and 3 times, respectively. Back-propagation was the most commonly  
501 used training method (56%), followed by the Levenberg-Marquardt (28%) and gradient  
502 descent methods (16%).  $n_e$  ranged between  $10^3$  and  $5 \cdot 10^4$ , with the most commonly  
503 used value being  $10^3$  (72%). Regarding  $T:V:T$ , the studies considered a range of the  
504 total data available from 56% to 80% for training, from 1% to 30% for validation, and  
505 from 0% to 20% for testing. Based on these ratios, the mean value of  $T:V:T$  was  
506 67:18:15. Finally, the  $R^2$  varied between 0.15 and 0.94, with a mean value of 0.68.

507 All simulations were executed on a desktop machine with an Intel Core i7-3770 3.4  
508 GHz, 64-bit, and 16 GB RAM. Fig. 7 displays the computational times to simulate *E.*  
509 *coli* concentrations by the process-based and ANN approaches. In Fig. 7, note that  
510 Forecasting: 1 h, Forecasting: 1 day, Forecasting: 1 month, and Forecasting: 1 bathing  
511 season refer to the simulation times.

512 The process-based model calibration was the first step for both approaches, requiring  
513 336 and 168 h for the calibration of hydrodynamics and water quality modules,  
514 respectively. The second step was applied only in the ANN approach, requiring 144 h  
515 for the development of ANN models. At this step, both approaches were ready to  
516 forecast FIO concentrations, with computational times (in hours) of the process-based

517 and ANN models for 1 h, 1 day, 1 month and 1 bathing season of 0.25 and 0.01, 6 and  
 518 0.01, 78 and 0.02, and 0.03 and 949, respectively.



519

520 Fig. 7. Computational times used to simulate FIO concentrations by the process-based  
 521 model and by the ANN model using the proposed methodology. Note that Forecasting:  
 522 1 h, Forecasting: 1 day, Forecasting: 1 month, and Forecasting: 1 bathing season refer to  
 523 the simulation times.

524

#### 525 4. Discussion

##### 526 4.1. Performance of predictive tools

527 While the results indicate that *E. coli* prediction using the process-based model  
 528 throughout the Eo Estuary is reasonably accurate, inconsistencies between measured  
 529 and predicted *E. coli* concentrations may still occur because the required numerical  
 530 precision is subject to the uncertainties in FIO enumeration methods, the complicated  
 531 relationships and processes related to FIO evolution, the impact of the changing

532 environment on FIO concentrations, and/or the model accuracy limits (Boehm, 2007;  
533 Gronewold and Wolpert, 2008; Shaw et al. 2017).

534 Since the ANN models were trained by means of the process-based model outputs, their  
535 predictions were slightly worse because they were also biased by the process-based  
536 model errors (see Fig. 6). In this regard, the ANN models mostly  
537 underestimated/overestimated *E. coli* concentrations compared with the process-based  
538 model for magnitudes higher/lower than a specific value because the neural network  
539 approach smoothed the results provided by the process-based model (see Figs. S5 to S7  
540 in the supplementary materials). For instance, *E. coli* concentrations were  
541 underestimated/overestimated for magnitudes higher/lower than 20, 80, 50, and 90 *E.*  
542 *coli*/100 ml at BP1, BP2, BP3, and BP4, respectively (see Fig. 5). This effect was  
543 generated by the kernel of the network consisting of nonlinear relationships that  
544 prioritized larger weights for the values with a higher frequency of input data because  
545 the networks were designed to minimize statistical errors.

546 Moreover, predictions were better in BP2 than in BP1, BP3 and BP4 because this beach  
547 is the most influenced by hydrodynamics, i.e., advection processes were more  
548 significant than diffusion and reaction processes. The factors that may influence these  
549 differences are the discharge locations and beach locations related to the main estuarine  
550 water inflows and outflows. The three discharges are located in the main channel close  
551 to the eastern margin, such that faecal pollution is transported by the main estuarine  
552 water flows along the main channel until it reaches the adjacent coastal area (advection).  
553 Thus, *E. coli* levels presented higher values with less variability at the main channel and  
554 were higher at the eastern margin than at the western margin. In other estuarine areas  
555 such as tidal flats or the western margin, diffusion processes become significant for  
556 transporting faecal pollution due to lateral dispersion with respect to the main flow

557 direction; as a result, the *E. coli* levels presented lower values with more variability.  
558 Lastly, the coastal areas outside the estuary displayed the lowest *E. coli* concentrations  
559 because the reaction processes are significant in the transport of faecal pollution due to  
560 the greater distance to the discharge locations, which increases the travel time and,  
561 subsequently, the bacterial mortality.

562 First, BP2 is located in the main channel at the eastern margin and close to FD2 (the  
563 major faecal discharge in the estuary). Due to the location of this point, the evolution of  
564 *E. coli* concentrations presented higher values with less variability than that at BP1, BP3  
565 and BP4, increasing the accuracy of both predictive tools. Second, BP3 and BP4 are  
566 located outside the main channel at the western margin and close to FD2 and FD3,  
567 respectively. Due to the locations of these points, the evolution of *E. coli* concentrations  
568 presented lower values with more variability than that at BP2, decreasing the accuracy  
569 of both predictive tools. Finally, BP1 is located at the adjacent western coastal area,  
570 outside the estuary. Due to the location of this point, the evolution of *E. coli*  
571 concentrations presented the lowest values and less variability than that at BP3 and BP4  
572 and more than that at BP2, leading to a better accuracy of both predictive tools at this  
573 point than at BP3 and BP4 and a worse accuracy than at BP2.

574 One way to minimize the impact of imprecise and variable data quality is to categorize  
575 data into overlapping groups and frequencies that have meaning relative to the system  
576 under study rather than focusing on predicting a specific concentration (Chandramouli  
577 et al., 2007). Thus, we used a contingency table as an error metric to calculate the  
578 accuracy of predictive tools for bathing water quality management. For the *E. coli* value  
579 of 500 at BP1, BP2, BP3 and BP4, the performance of both predictive tools was the  
580 same because this performance is heavily influenced by the most common category,  
581 namely, “correct negative” (see Table 1), due to the concentration measurements always

582 being below this threshold. This performance was also observed at BP1 for the *E. coli*  
583 values of 250 and 125. The ANN models performed better than the process-based  
584 model for intermediate values and worse for low values because the neural network  
585 approach smoothed the results.

586 Efforts are currently underway to expand this methodology to include a neural network  
587 approach using deep learning (Schmidhuber, 2015), considering the real-time flow,  
588 salinity, temperature and *E. coli* concentration of faecal discharges (Bravo et al., 2017),  
589 including the effect of other forcings such as wind and/or waves (Dunn et al., 2014),  
590 and taking into account the effect of extreme events such as those produced after heavy  
591 rain or due to a failure in the sewer system.

592

#### 593 **4.2. Configuration and computational trade-off of artificial neural networks**

594 The application of ANNs to the Eo Estuary presented here was in accordance with the  
595 ANN configurations proposed in other studies. Our final ANN configuration confirmed  
596 the tendency to develop ANN models with an  $n_h:n_i$  ratio higher than 1 and the validity  
597 of the proposed Eq. (8) as an indicator of the suitable range for trials with  $n_h$ . Moreover,  
598 our review suggests that the best configuration for predicting FIOs with ANNs might be  
599 structured with a  $1 < n_h:n_i < 2$  ratio, a tan-sigmoid function for the  $f_h$ , a log-sigmoid  
600 function for the  $f_o$ , the Levenberg-Marquardt method, a  $10^3 n_e$ , and a  $T:V:T$  ratio of  
601 67:18:15. However, it should be emphasized that there is not a predefined ANN  
602 configuration that ensures the best approximation of the outputs for the targets.

603 Although ANN models need to be trained and validated, which is a time-consuming  
604 process, one of the most valuable characteristics of ANNs is their ability to perform  
605 long-term forecasting with computational times that barely exceed one minute. For  
606 instance, this study highlighted that during the model setup of both predictive tools, the

607 computational time used by the process-based approach was 0.78 times smaller than  
608 that used by the ANN approach due to the additional time spent on ANN development  
609 (see Fig. 7). Conversely, the computational costs of forecasting are considerably  
610 reduced by the ANN models compared with the process-based model, with decreases of  
611 25, 600, 3900, and 31633 times for forecasting 1 h, 1 day, 1 month and 1 bathing  
612 season, respectively. Thus, the longer the forecasting period, the greater the reduction in  
613 computational time by ANN models.

614 Therefore, both approaches have advantages for different purposes. The value of the  
615 ANN model presented here is that it is very quick to implement and can be used for  
616 nowcasting of bathing water quality, whereas a process-based model can be used to  
617 investigate processes that govern the levels of *E. coli* in the estuary. Once the ANN  
618 model is trained and validated, it can be easily used by bathing water managers to  
619 identify potential risks for users, support decision-making tasks and allow  
620 administrations to promote preventive management actions.

621

## 622 **5. Conclusions**

623 The proposed methodology forecasts FIO concentrations (*E. coli* in this study) and  
624 classifies bathing sites for any period, integrating the benefits of laboratory analyses,  
625 numerical modelling, and machine learning. Our study demonstrated that the proposed  
626 method allows the evolution of FIO concentrations to be calculated for any period at the  
627 bathing sites, optimizing the trade-off between computational cost and the result  
628 accuracy of conventional process-based models and data-driven models. Thus, ANN  
629 models are viable emulators of highly nonlinear process-based models driven by highly  
630 variable forcings. However, surrogate validity outside of the training region is difficult  
631 to evaluate and should be further researched.

632 FIO concentrations were the focus here, but the method could be adapted to address the  
633 concentration of other water constituents such as total dissolved oxygen, nutrients,  
634 suspended sediments, heavy metals, organic micropollutants, and/or microplastics or to  
635 predict FIO concentrations in shellfish, with the aim of protecting consumers from  
636 faeces-contaminated shellfish.

637 From a technical perspective, the ANN models have a strong predictive ability for  
638 nonlinear systems and can enhance the overall reliability and applicability of process-  
639 based models. From the operational perspective, the implementation of ANN models is  
640 highly efficient at a very low cost compared to the implementation of process-based  
641 models (see subsection 3.3). This capability is particularly useful in scenarios where on-  
642 the-spot decisions are needed (e.g., temporary closure of a bathing site), for which the  
643 use of complex and detailed process-based models can be cumbersome. Thus, ANN  
644 models could be applied in early warning systems for the public to minimize contact  
645 with bathing waters impacted by high faecal levels (daily planning of bathing sites).  
646 Nevertheless, the accuracy of river flows and meteorological forecasts must be  
647 considered for any temporal horizon.

648

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654

#### 655 **References**

- 656 1. Bárcena, J.F., Claramunt, I., García-Alba, J., Pérez, M.L., García, A., 2017a. A  
657 method to assess the evolution and recovery of heavy metal pollution in estuarine  
658 sediments: Past history, present situation and future perspectives. *Marine Pollution*  
659 *Bulletin* 124 (1), 421-434.
- 660 2. Bárcena, J.F., Gómez, A.G., García, A., Álvarez, C., Juanes, J.A., 2017b.  
661 Quantifying and mapping the vulnerability of estuaries to point-source pollution  
662 using a multi-metric assessment: The Estuarine Vulnerability Index (EVI).  
663 *Ecological Indicators* 76, 159-169.
- 664 3. Bedri, Z., Corkery, A., O'Sullivan, J.J., Alvarez, M.X., Erichsen, A.C., Deering,  
665 L.A., Demeter, K., O'Hare, G.M.P., Meijer, W.G., Masterson, B., 2014. An  
666 integrated catchment-coastal modelling system for real-time water quality forecasts.  
667 *Environmental Modelling and Software* 61, 458-476.
- 668 4. Bedri, Z., Corkery, A., O'Sullivan, J.J., Deering, L.A., Demeter, K., Meijer, W.G.,  
669 O'Hare, G., Masterson, B., 2016. Evaluating a microbial water quality prediction  
670 model for beach management under the revised EU Bathing Water Directive.  
671 *Journal of Environmental Management* 167, 49-58.
- 672 5. Bennett, N.D., Croke, B.F.W., Guariso, G., Guillaume, J.H.A., Hamilton, S.H.,  
673 Jakeman, A.J., Marsili-Libelli, S., Newham, L.T.H., Norton, J.P., Perrin, C., Pierce,  
674 S.A., Robson, B., Seppelt, R., Voinov, A.A., Fath, B.D., Andreassian, V., 2013.  
675 Characterising performance of environmental models. *Environmental Modelling*  
676 *and Software* 40, 1-20.
- 677 6. Besmer, M.D., Weissbrodt, D.G., Kratochvil, B.E., Sigrist, J.A., Weyland, M.S.,  
678 Hammes, F., 2014. The feasibility of automated online flow cytometry for in-situ  
679 monitoring of microbial dynamics in aquatic ecosystems. *Frontiers in Microbiology*  
680 5, 265.

- 681 7. Boehm, A.B., 2007. Enterococci Concentrations in Diverse Coastal Environments  
682 Exhibit Extreme Variability. *Environmental Science and Technology* 41 (24),  
683 8227-8232.
- 684 8. Boehm, A.B., Grant, S.B., Kim, J.H., Mowbray, S.L., McGee, C.D., Clark, C.D.,  
685 Foley, D.M., Wellman, D.E., 2002. Decadal and Shorter Period Variability of Surf  
686 Zone Water Quality at Huntington Beach, California. *Environmental Science and*  
687 *Technology* 36 (18), 3885-3892.
- 688 9. Bravo, H.R., McLellan, S.L., Val Klump, J., Hamidi, S.A., Talarczyk, D., 2017.  
689 Modeling the fecal coliform footprint in a Lake Michigan urban coastal area.  
690 *Environmental Modelling and Software* 95, 401-419.
- 691 10. Castelletti, A., Galelli, S., Ratto, M., Soncini-Sessa, R., Young, P.C., 2012. A  
692 general framework for Dynamic Emulation Modelling in environmental problems.  
693 *Environmental Modelling and Software* 34, 5-18.
- 694 11. Chandramouli, V., Brion, G., Neelakantan, T.R., Lingireddy, S., 2007. Backfilling  
695 missing microbial concentrations in a riverine database using artificial neural  
696 networks. *Water Research* 41 (1), 217-227.
- 697 12. Chapra, S.C., 1997. *Surface Water-Quality Modeling*, McGraw-Hill Companies,  
698 Inc., USA.
- 699 13. de Brauwere, A., Ouattara, N.K., Servais, P., 2014. Modeling fecal indicator  
700 bacteria concentrations in natural surface waters: a review. *Critical Reviews in*  
701 *Environmental Science and Technology* 44 (21), 2380-2453.
- 702 14. De los Ríos, A., Echavarri-Erasun, B., Lacorte, S., Sánchez-Ávila, J., De Jonge, M.,  
703 Blust, R., Orbea, A., Juanes, J. A., Cajaraville, M. P., 2016. Relationships between  
704 lines of evidence of pollution in estuarine areas: Linking contaminant levels with

- 705 biomarker responses in mussels and with structure of macroinvertebrate benthic  
706 communities. *Marine Environmental Research* 121, 49-63.
- 707 15. de Paz, L., Patrício, J., Marques, J.C., Borja, A., Laborda, A.J., 2008. Ecological  
708 status assessment in the lower Eo Estuary (Spain). The challenge of habitat  
709 heterogeneity integration: A benthic perspective. *Marine Pollution Bulletin* 56 (7),  
710 1275-1283.
- 711 16. del Río, S., Herrero, L., Fraile, R., Penas, A., 2011. Spatial distribution of recent  
712 rainfall trends in Spain (1961-2006). *International Journal of Climatology* 31 (5),  
713 656-667.
- 714 17. Diffey, B.L., 2002. Sources and measurement of ultraviolet radiation. *Methods* 28  
715 (1), 4-13.
- 716 18. Directive (2006/7/EC) of the European Parliament and of the Council, of 15  
717 February 2006, concerning the management of bathing water quality, OJ L376/14.
- 718 19. Dunn, R.J.K., Zigic, S., Shiell, G.R., 2014. Modelling the dispersion of treated  
719 wastewater in a shallow coastal wind-driven environment, Geographe Bay, Western  
720 Australia: implications for environmental management. *Environmental Monitoring  
721 and Assessment* 186 (10), 6107-6125.
- 722 20. Flor, G., Fernández-Pérez, L.A., Cabrera-Ceñal, R., 1993. Aspectos morfológicos  
723 del estuario del Eo. *Trabajos de Geología* 19, 75-95 (in Spanish).
- 724 21. FLTQ, 1990. Análisis de las Condiciones Morfodinámicas de la Ría del Eo - Fase  
725 II, Informe Final, Fundación Leonardo Torres Quevedo (FLTQ). Consejería de  
726 Medio Rural y Pesca del Principado de Asturias, Oviedo, Spain (in Spanish).
- 727 22. García, A., Juanes, J.A., Álvarez, C., Revilla, J.A., Medina, R., 2010. Assesment of  
728 the response of a shallow macrotidal estuary to changes in hydrological and

- 729 wastewater inputs through numerical modelling. *Ecological Modelling* 221 (8),  
730 1194-1208.
- 731 23. Gronewold, A.D., Wolpert, R.L., 2008. Modeling the relationship between most  
732 probable number (MPN) and colony-forming unit (CFU) estimates of fecal  
733 coliform concentration. *Water Research* 42 (13), 3327-3334.
- 734 24. Hagan, M.T., Menhaj, M.B., 1994. Training feedforward networks with the  
735 Marquardt algorithm. *IEEE Transactions on Neural Networks* 5 (6), 989-993.
- 736 25. He, L., He, Z., 2008. Water quality prediction of marine recreational beaches  
737 receiving watershed baseflow and stormwater runoff in southern California, USA.  
738 *Water Research* 42 (10-11), 2563-2573.
- 739 26. Højris, B., Christensen, S.C.B., Albrechtsen, H.J., Smith, C., Dahqvist, M., 2016. A  
740 novel, optical, on-line bacteria sensor for monitoring drinking water quality.  
741 *Scientific Reports* 6, 23935.
- 742 27. Huang, G., Falconer, R.A., Lin, B., 2017. Integrated hydro-bacterial modelling for  
743 predicting bathing water quality. *Estuarine, Coastal and Shelf Science* 188, 145-  
744 155.
- 745 28. Jiang, Y., Nan, Z., Yang, S., 2013. Risk assessment of water quality using Monte  
746 Carlo simulation and artificial neural network method. *Journal of Environmental*  
747 *Management* 122, 130-136.
- 748 29. Kazemi Yazdi, S., Scholz, M., 2010. Assessing storm water detention systems  
749 treating road runoff with an artificial neural network predicting fecal indicator  
750 organisms. *Water, Air, and Soil Pollution* 206 (1-4), 35-47.
- 751 30. Keeratipibul, S., Phewpan, A., Lursinsap, C., 2011. Prediction of coliforms and  
752 *Escherichia coli* on tomato fruits and lettuce leaves after sanitizing y using Artificial  
753 Neural Networks. *LWT - Food Science and Technology* 44 (1), 130-138.

- 754 31. Khalil, B., Ouarda, T.B.M.J., St-Hilaire, A., 2011. Estimation of water quality  
755 characteristics at ungauged sites using artificial neural networks and canonical  
756 correlation analysis. *Journal of Hydrology* 405 (3-4), 277-287.
- 757 32. Kim, M., Choi, C.Y., Gerba, C.P., 2008. Source tracking of microbial intrusion in  
758 water systems using artificial neural networks. *Water Research* 42 (4-5), 1308-  
759 1314.
- 760 33. Lesser, G.R., Roelvink, J.A., van Kester, J.A.T.M., Stelling, G.S., 2004.  
761 Development and validation of a three-dimensional morphological model. *Coastal*  
762 *Engineering* 51 (8-9), 883-915.
- 763 34. López, I., Álvarez, C., Gil, J.L., García, A., Bárcena, J.F., Revilla, J.A., 2013. A  
764 method for the source apportionment in bathing waters through the modelling of  
765 wastewater discharges: Development of an indicator and application to an urban  
766 beach in Santander (Northern Spain). *Ecological Indicators* 24, 334-343.
- 767 35. Los, F.J. J., Troost, T.A.A., Van Beek, J.K.L., 2014. Finding the optimal reduction  
768 to meet all targets-Applying Linear Programming with a nutrient tracer model of  
769 the North Sea. *Journal of Marine Systems* 131, 91-101.
- 770 36. Maier, H.R., Jain, A., Dandy, G.C., Sudheer, K.P., 2010. Methods used for the  
771 development of neural networks for the prediction of water resource variables in  
772 river systems: Current status and future directions. *Environmental Modelling and*  
773 *Software* 25 (8), 891-909.
- 774 37. Mancini, J.L., 1978. Numerical estimates of coliform mortality rates under various  
775 conditions. *Journal Water Pollution Control Federation* 50 (11), 2477-2484.
- 776 38. Manzato, A., 2007. Sounding-derived indices for neural network based short-term  
777 thunderstorm and rainfall forecasts. *Atmospheric Research* 83 (2-4), 349-365.

- 778 39. Mas, D.M.L., Ahlfeld, D.P., 2007. Comparing artificial neural networks and  
779 regression models for predicting faecal coliform concentrations. *Hydrological*  
780 *Sciences Journal* 52 (4), 713-731.
- 781 40. Metcalf and Eddy, Inc., 2003. *Wastewater Engineering: Treatment and Reuse*,  
782 Revised by G. Tchobanoglous, F.L. Burton, and H.D. Stensel, Mc-Graw-Hill, New  
783 York, Fourth Edition.
- 784 41. Motamarri, S., Boccelli, D.L., 2012. Development of a neural-based forecasting  
785 tool to classify recreational water quality using fecal indicator organisms. *Water*  
786 *Research* 46 (14), 4508-4520.
- 787 42. Nash, J.E., Sutcliffe, J.V., 1970. River flow forecasting through conceptual models  
788 part I – A discussion of principles. *Journal of Hydrology* 10 (3), 282-290.
- 789 43. Piedracoba, S., Souto, C., Gilcoto, M., Pardo, P.C., 2005. Hydrography and  
790 dynamics of the Ría de Ribadeo (NW Spain), a wave driven estuary. *Estuarine,*  
791 *Coastal and Shelf Science* 65 (4), 726-738.
- 792 44. Postma, L., Boderie, P., van Gils, J., van Beek, J., 2003. Component software  
793 system for surface water simulations. *Lecture Notes in Computer Science* 2657,  
794 649-658.
- 795 45. Roberts, P.J.W., Villegas, B., 2017. Modeling and Design of the Buenos Aires  
796 Outfalls. *Journal of Hydraulic Engineering* 143 (2), 05016007.
- 797 46. Rompré, A., Servais, P., Baudart, J, Renée-de-Roubin, M, Laurent, P., 2002.  
798 Detection and enumeration of coliforms in drinking water: current methods and  
799 emerging approaches. *Journal of Microbiological Methods* 49, 31-54.
- 800 47. Rumelhart, D.E., Hinton, G.E., William, R.J., 1986. Learning representation by  
801 back-propagating errors. *Nature* 323, 533-536.

- 802 48. Schmidhuber, J., 2015. Deep Learning in neural networks: An overview. Neural  
803 Networks 61, 85-117.
- 804 49. Shaw, A.R., Smith Sawyer, H., LeBoeuf, E.J., McDonald, M.P., Hadjerioua, B.,  
805 2017. Hydropower Optimization Using Artificial Neural Network Surrogate  
806 Models of a High-Fidelity Hydrodynamics and Water Quality Model. Water  
807 Resources Research 53 (11), 9444-9461.
- 808 50. Sotillo, M.G., Cailleau, S., Lorente, P., Levier, B., Aznar, R., Reffray, G., Amo-  
809 Baladrón, A., Chanut, J., Benkiran, M., Alvarez-Fanjul, E., 2015 The MyOcean IBI  
810 Ocean Forecast and Reanalysis Systems: operational products and roadmap to the  
811 future Copernicus Service. Journal of Operational Oceanography 8 (1), 63-79.
- 812 51. Thoe, W., Gold, M., Griesbach, A., Grimmer, M., Taggart, M.L., Boehm, A.B.,  
813 2014. Predicting water quality at Santa Monica Beach: Evaluation of five different  
814 models for public notification of unsafe swimming conditions. Water Research 67,  
815 105-117.
- 816 52. Thoe, W., Wong, S.H.C., Choi, K.W., Lee, J.H.W., 2012. Daily prediction of  
817 marine beach water quality in Hong Kong. Journal of Hydro-Environment Research  
818 6 (3), 164-180.
- 819 53. Tufail, M., Ormsbee, L., Teegavarapu, R., 2008. Artificial Intelligence-Based  
820 Inductive Models for Prediction and Classification of Fecal Coliform in Surface  
821 Waters. Journal of Environmental Engineering 134 (9), 789-799.
- 822 54. van der Merwe, R., Leen, T.K., Lu, Z., Frolov, S., Baptista, A.M., 2007. Fast neural  
823 network surrogates for very high dimensional physics-based models in  
824 computational oceanography. Neural Networks 20 (4), 462-478.

- 825 55. Vang, O.K., Corfitzen, C.B., Smith, C., Albrechtsen, H-J., 2014. Evaluation of ATP  
826 measurements to detect microbial ingress by wastewater and surface water in  
827 drinking water. *Water Research* 64, 309-320.
- 828 56. Walker, D.I., McQuillan, J., Taiwo, M., Parks, R., Stenton, C.A., Morgan, H.,  
829 Mowlem, M.C., Lees, D.N., 2017. A highly specific *Escherichia coli* qPCR and its  
830 comparison with existing methods for environmental waters. *Water Research* 126,  
831 101-110.
- 832 57. Wang, X., Zhang, J., Babovic, V., 2016. Improving real-time forecasting of water  
833 quality indicators with combination of process-based models and data assimilation  
834 technique. *Ecological Indicators* 66, 428-439.
- 835 58. Washington, W.M., Buja, L., Craig, A., 2009. The computational future for climate  
836 and earth system models: on the path to petaflop and beyond. *Philosophical*  
837 *Transactions of the Royal Society Academy Series A* 367 (1890), 833-846.
- 838 59. Wu, W., Dandy, G.C., Maier, H.R., 2014. Protocol for developing ANN models  
839 and its application to the assessment of the quality of the ANN model development  
840 process in drinking water quality modelling. *Environmental Modelling and*  
841 *Software* 54, 108-127.
- 842 60. Zhang, Z., Deng, Z., Rusch, K.A., 2015. Modeling Fecal Coliform Bacteria Levels  
843 at Gulf Coast Beaches. *Water Quality, Exposure and Health* 7 (3), 255-263.
- 844 61. Zou, R., Lung, W-S., Wu, J., 2007. An adaptive neural network embedded genetic  
845 algorithm approach for inverse water quality modeling. *Water Resources Research*  
846 43 (8), W08427.

847

848 **Figure and Table captions**

849 Fig. 1. Map of the Eo River Basin and the Eo Estuary, indicating the locations of the  
850 tidal gauges (TG1-TG4), monitoring points (MP1-MP3), flow gauge (FG1),  
851 meteorological station (MS1), bathing water quality control points (BP1-BP4), and  
852 faecal discharges (FD1-FD3) used in the setup of the predictive tools. Bathymetry is  
853 also presented with a zoomed-in image of the outer and inner areas of the Eo Estuary  
854 (UTM projection ED50 30N).

855 Fig. 2. Schematic view of a feedforward neural network with five nodes in the input  
856 layer, three nodes in the hidden layer and one node in the output layer. Synapses are  
857 oriented from left to right.

858 Fig. 3. Overall methodological approach.

859 Fig. 4. Schematic view of the proposed methodology to develop artificial neural  
860 networks to analyse bathing water quality criteria in estuaries.

861 Fig. 5. Performance of the final artificial neural networks (outputs) in emulating *E. coli*  
862 concentrations (*E. coli*/100 ml) computed by the process-based model (targets) at BP1  
863 (a), BP2 (b), BP3 (c), and BP4 (d). The bias,  $R^2$ , and CE magnitudes are also shown for  
864 the four bathing sites (BP1-BP4). The colorbar shows the occurrence probability of the  
865 scatter dots defined by the *E. coli* concentration of targets (process-based model) and  
866 outputs (ANN model).

867 Fig. 6. Performance of the process-based model (filled markers) and the ANN models  
868 (unfilled markers) in simulating the *E. coli* concentrations (*E. coli*/100 ml) at BP1  
869 (squares), BP2 (circles), BP3 (diamonds), and BP4 (triangles) during the bathing season  
870 of 2013 (red), 2014 (green), and 2015 (blue). The bias,  $R^2$ , and CE magnitudes are also  
871 shown for the four bathing sites (BP1-BP4) and considering all the bathing seasons and  
872 locations at the same time (global).

873 Fig. 7. Computational times required to simulate FIO concentrations by the process-  
874 based model and by the ANN model using the proposed methodology. Note that  
875 Forecasting: 1 h, Forecasting: 1 day, Forecasting: 1 month, and Forecasting: 1 bathing  
876 season refer to the simulation times.

877 Table 1. (a): Contingency table used to assess the accuracy of predictive tools for the  
878 prediction of faecal indicator organism (FIO) concentrations. (b): Error metrics of the  
879 contingency table (Source: Manzato, 2007; Bennett et al., 2013; Bedri et al. 2016).

880 Table 2. Model parameters used in the calculation of *E. coli* transport and mixing.

881 Table 3. Computed metrics for the assessment of the accuracy of the predictive tools in  
882 predicting compliance with/exceedance of the *E. coli* values of 500, 250, 125, 50, and  
883 25 *E. coli*/100 ml.

884 Table 4. Review of previous research predicting faecal indicator organisms (FIOs) with  
885 multilayer feedforward networks consisting of one input layer, one hidden layer, and  
886 one output layer.

		Observed Exceedances		
		yes	no	
Predicted Exceedances	yes	Hits	False alarms	Predicted yes
	no	Misses	Correct negatives	Predicted no
		Observed yes	Observed no	Total

a) Contingency table

Metric	Formula	Range of values	Ideal value	Notes
Accuracy (fraction correct)	$\frac{Hits + Correct\ negatives}{Total}$	0-1	1	It is heavily influenced by the most common category, usually "no event".
Bias score (frequency bias)	$\frac{Hits + False\ alarms}{Hits + Misses}$	0-∞	1	Indicates if the model tends to under- (<1) or over- (>1) estimate.
Hit rate (Probability of detection)	$\frac{Hits}{Hits + Misses}$	0-1	1	Sensitive to hits but ignores false alarms. Good for rare events.
False alarm rate (Probability of false detection)	$\frac{False\ alarms}{False\ alarms + Correct\ negatives}$	0-1	0	Sensitive to false alarms but ignores misses.
Success index	$\frac{1}{2} \cdot \left[ \frac{Hits}{Hits + Misses} + \frac{Correct\ negatives}{Total} \right]$	0-1	1	Weights equally the ability of the model to correctly detect occurrences and non-occurrences of events.
Threat score	$\frac{Hits + Correct\ negatives}{Total}$	0-1	1	Measures the fraction of observed cases that were correctly modelled. It penalizes both misses and false alarms.

b) Error metrics

Constant	Value	Units	Source
$D_H, D_V$	Time series	m <sup>2</sup> /s	Hydrodynamic module
$T$	Time series	°C	Hydrodynamic module
$C_{Cl}$	Time series	g/m <sup>3</sup>	Hydrodynamic module
$I_0$	Time series	W/m <sup>2</sup>	Meteorological station (MS1)
$K_B$	0.8	1/days	Chapra (1997)
$DL$	1	days	(*)
$f_{uv}$	0.12	-	Diffey (2002)
$\varepsilon$	0.35	1/m	FLTQ (1990); Eq. (5)
$K_T$	1.07	-	This study (calibration)
$k_{rd}$	0.086	m <sup>2</sup> /W·days	This study (calibration)
$k_{Cl}$	$2 \cdot 10^{-4}$	m <sup>3</sup> /g·days	This study (calibration)

(\*) Day-night variations are considered within the irradiation ( $I_0$ ).

Bathing site	Contingency table (metrics)	Value = 500 <i>E. coli</i> /100 ml		Value = 250 <i>E. coli</i> /100 ml		Value = 125 <i>E. coli</i> /100 ml		Value = 50 <i>E. coli</i> /100 ml		Value = 25 <i>E. coli</i> /100 ml	
		Process-based	ANN	Process-based	ANN	Process-based	ANN	Process-based	ANN	Process-based	ANN
BP1	Accuracy	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00
	Bias score	(*)	(*)	(*)	(*)	(*)	(*)	1.00	1.00	1.00	1.00
	Hit rate	(*)	(*)	(*)	(*)	(*)	(*)	1.00	1.00	1.00	1.00
	False alarm rate	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00
	Success index	(*)	(*)	(*)	(*)	(*)	(*)	0.92	0.92	0.92	0.92
	Threat score	(*)	(*)	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00
BP2	Accuracy	1.00	1.00	0.88	0.88	0.96	1.00	0.96	0.92	0.96	0.84
	Bias score	(*)	(*)	1.33	1.33	0.86	1.00	1.09	1.00	0.93	0.78
	Hit rate	(*)	(*)	0.67	0.67	0.86	1.00	1.00	0.92	0.93	0.78
	False alarm rate	0.00	0.00	0.09	0.09	0.00	0.00	0.07	0.08	0.00	0.00
	Success index	(*)	(*)	0.73	0.73	0.79	0.88	0.76	0.70	0.67	0.53
	Threat score	(*)	(*)	0.88	0.88	0.96	1.00	0.96	0.92	0.96	0.84
BP3	Accuracy	1.00	1.00	0.96	0.96	0.88	0.96	0.77	0.92	0.88	0.96
	Bias score	(*)	(*)	0.00	0.00	0.25	0.50	0.85	0.82	0.83	0.94
	Hit rate	(*)	(*)	0.00	0.00	0.25	0.50	0.69	0.82	0.83	0.94
	False alarm rate	0.00	0.00	0.00	0.00	0.00	0.00	0.15	0.00	0.00	0.00
	Success index	(*)	(*)	0.48	0.48	0.55	0.71	0.56	0.68	0.56	0.62
	Threat score	(*)	(*)	0.96	0.96	0.88	0.96	0.77	0.92	0.88	0.96
BP4	Accuracy	1.00	1.00	1.00	1.00	0.92	1.00	0.90	0.73	0.91	0.83
	Bias score	(*)	(*)	1.00	1.00	0.33	1.00	0.78	0.78	0.88	0.88
	Hit rate	(*)	(*)	1.00	1.00	0.33	1.00	0.78	0.56	0.88	0.82
	False alarm rate	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.15	0.00	0.17
	Success index	(*)	(*)	0.98	0.98	0.60	0.98	0.67	0.53	0.57	0.52
	Threat score	(*)	(*)	1.00	1.00	0.92	1.00	0.90	0.73	0.91	0.83

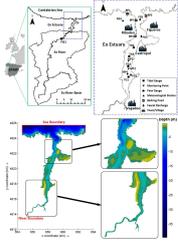
(\*) Indeterminate form 0/0.

Study	FIO(*)	$n_i$	$n_h$	$f_h(**)$	$f_o(**)$	Training method	$n_e$	T:V:T	$R^2$
Chandramouli et al. (2007)	FC	7	9	Log	Log	Back-propagation	(***)	75:15:10	0.63-0.94
Mas and Ahlfeld (2007)	FC	6	16	Tan	Tan	Levenberg-Marquardt	$10^3$	64:16:20	(***)
Kim et al. (2008)	EC	3	1	Tan	Tan	Back-propagation	$5 \cdot 10^4$	72:8:20	0.90-0.96
He and He (2008)	TC	7	3	(***)	(***)	Back-propagation	(***)	56:24:20	0.79
He and He (2008)	FC	12	6	(***)	(***)	Back-propagation	(***)	56:24:20	0.82
He and He (2008)	EN	7	8	(***)	(***)	Back-propagation	(***)	56:24:20	0.86
Tufail et al. (2008)	EC	2	4	Log	Log	Back-propagation	$10^4$	80:20:(***)	0.58-0.73
Kazemi Yazdi and Scholz (2010)	EN	4	8	Tan	Tan	Levenberg-Marquardt	$10^3$	65:15:20	0.15-0.80
Keeratipibul et al. (2011)	EC	6	5	Tan	Log	Back-propagation	(***)	70:30:(***)	0.72
Thoe et al. (2012)	FC	7	5	Log	Lin	Gradient-descent with momentum	$10^3$	60:20:20	0.29-0.75
Motamarri and Boccelli, (2012)	FC	5	6	Tan	Lin	Levenberg-Marquardt	$10^3$	99:1 (leave-one-out)	(***)
Thoe et al. (2014)	FC	12	5	Log	Lin	Gradient-descent	$2 \cdot 10^4$	60:20:20	0.38-0.58
Zhang et al. (2015)	FC	14	(***)	(***)	(***)	Back-propagation	(***)	60:20:20	0.68
This study (2018)	EC	9	15	Tan	Log	Levenberg-Marquardt	$10^3$	70:15:15	0.55-0.75

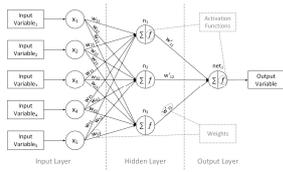
(\*) FC: *Faecal coliform*, TC: *Total coliform*, EC: *E. coli*, EN: *Intestinal enterococci*.

(\*\*) Log: Log-sigmoid, Tan: Tan-sigmoid, Lin: Linear.

(\*\*\*) Non-specified in the study.

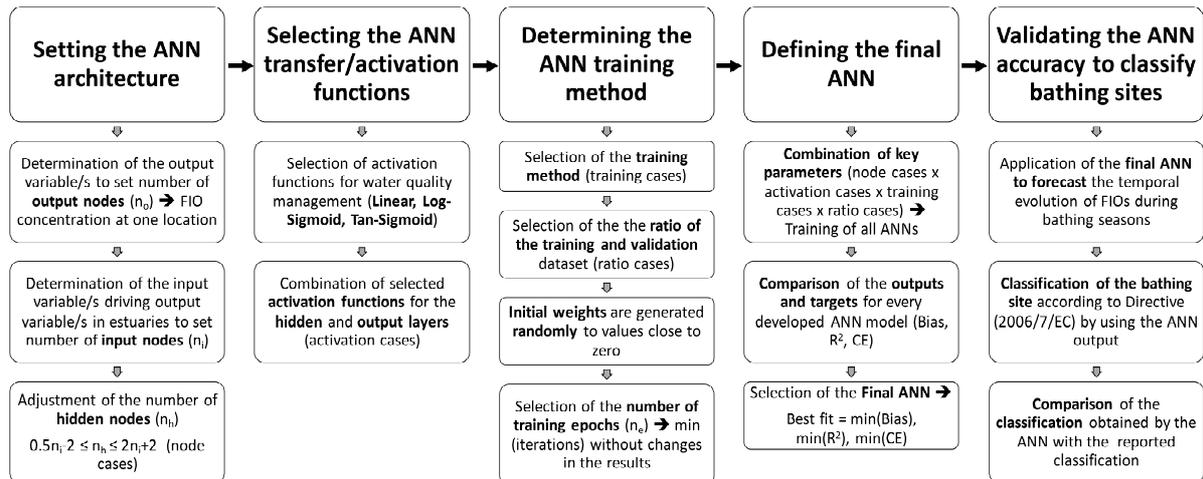


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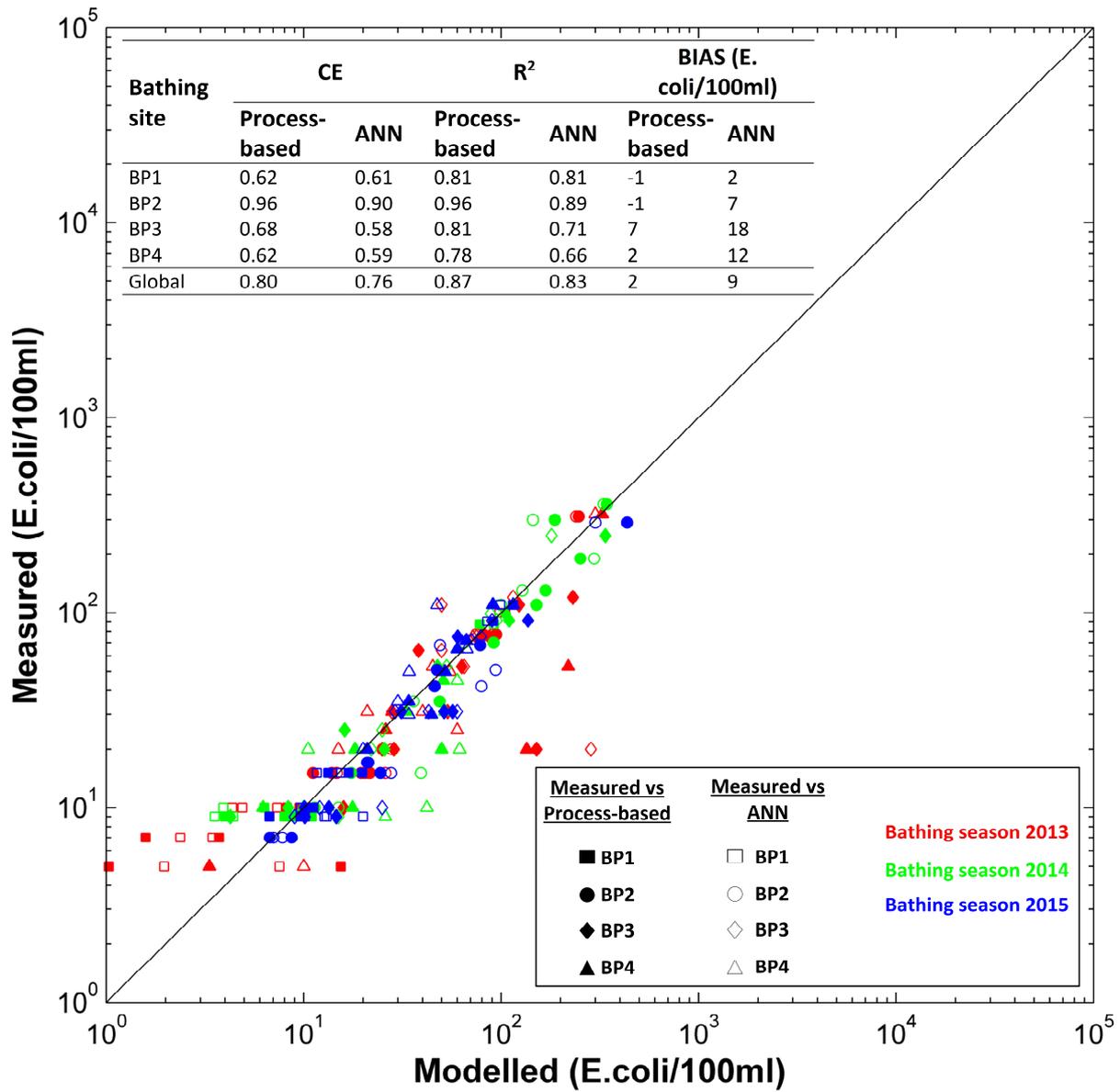


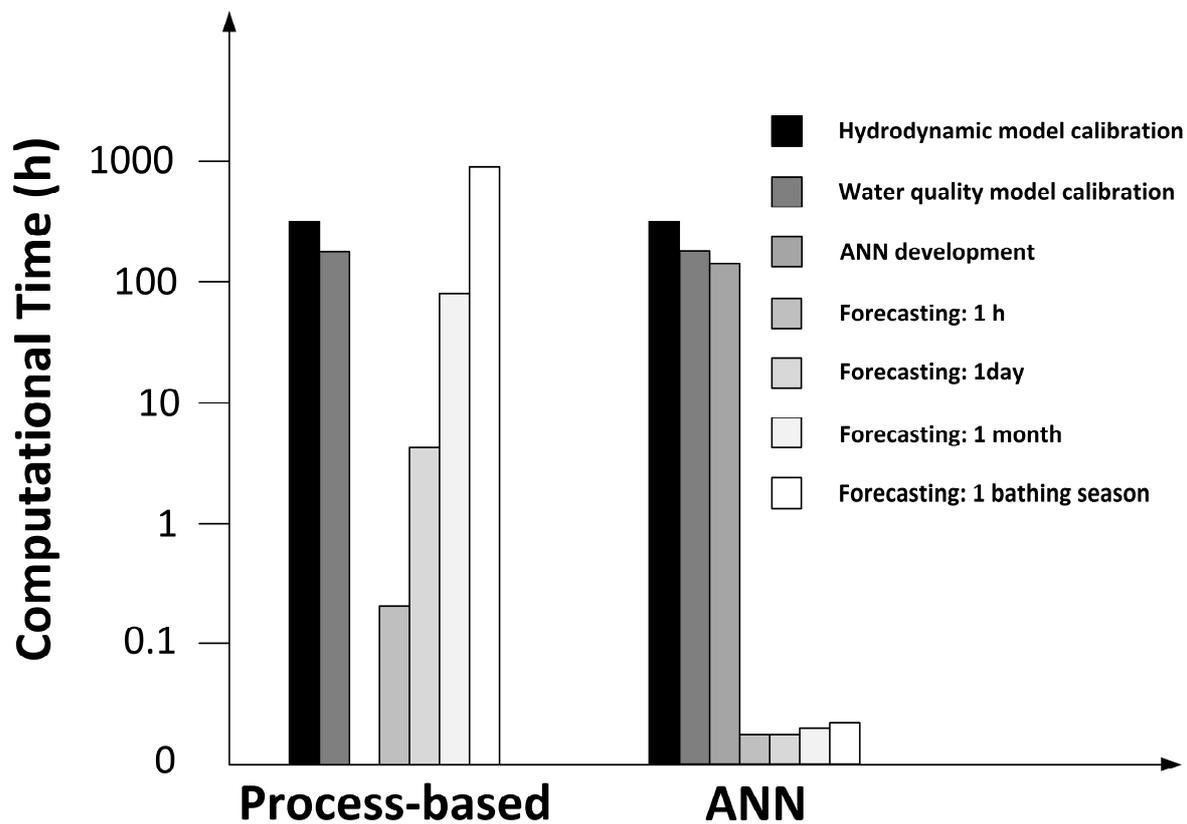
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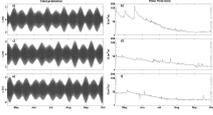
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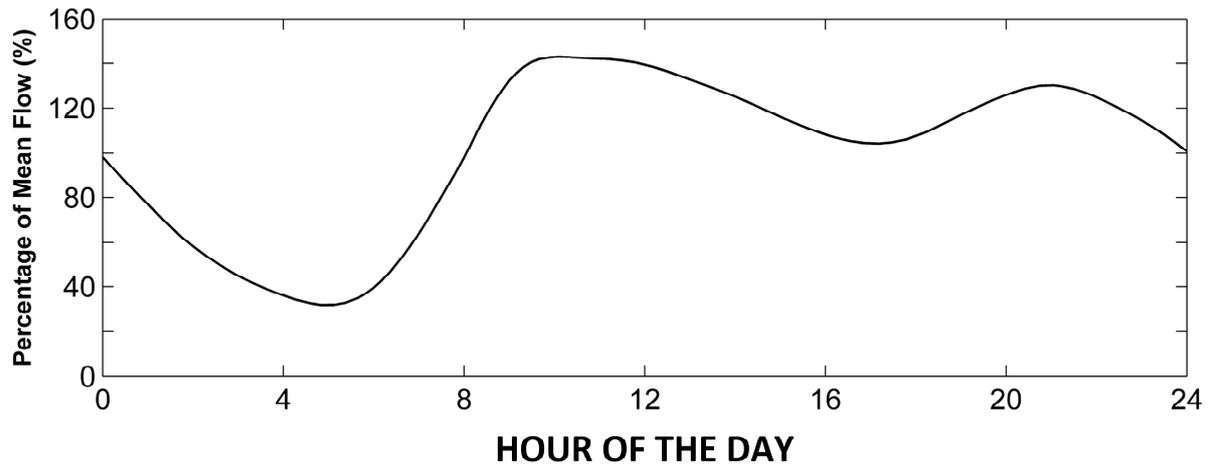
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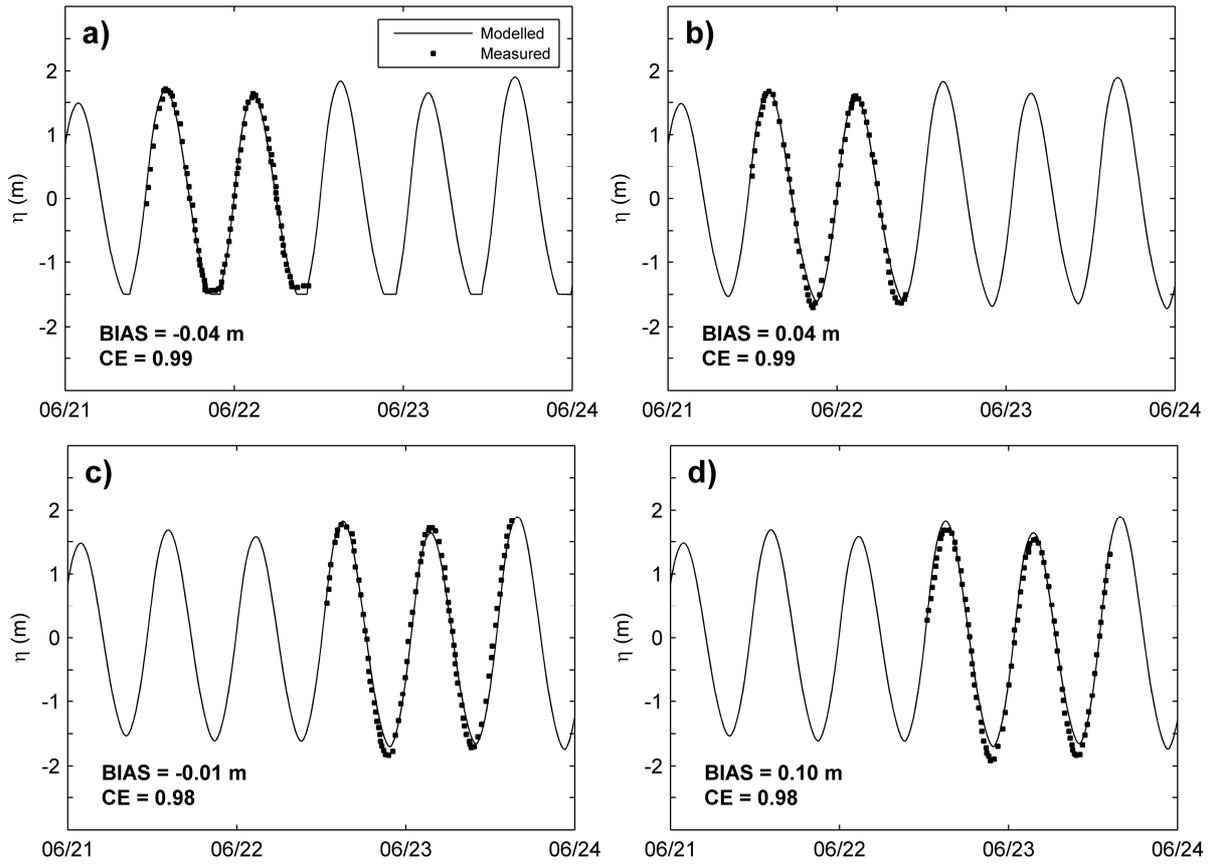


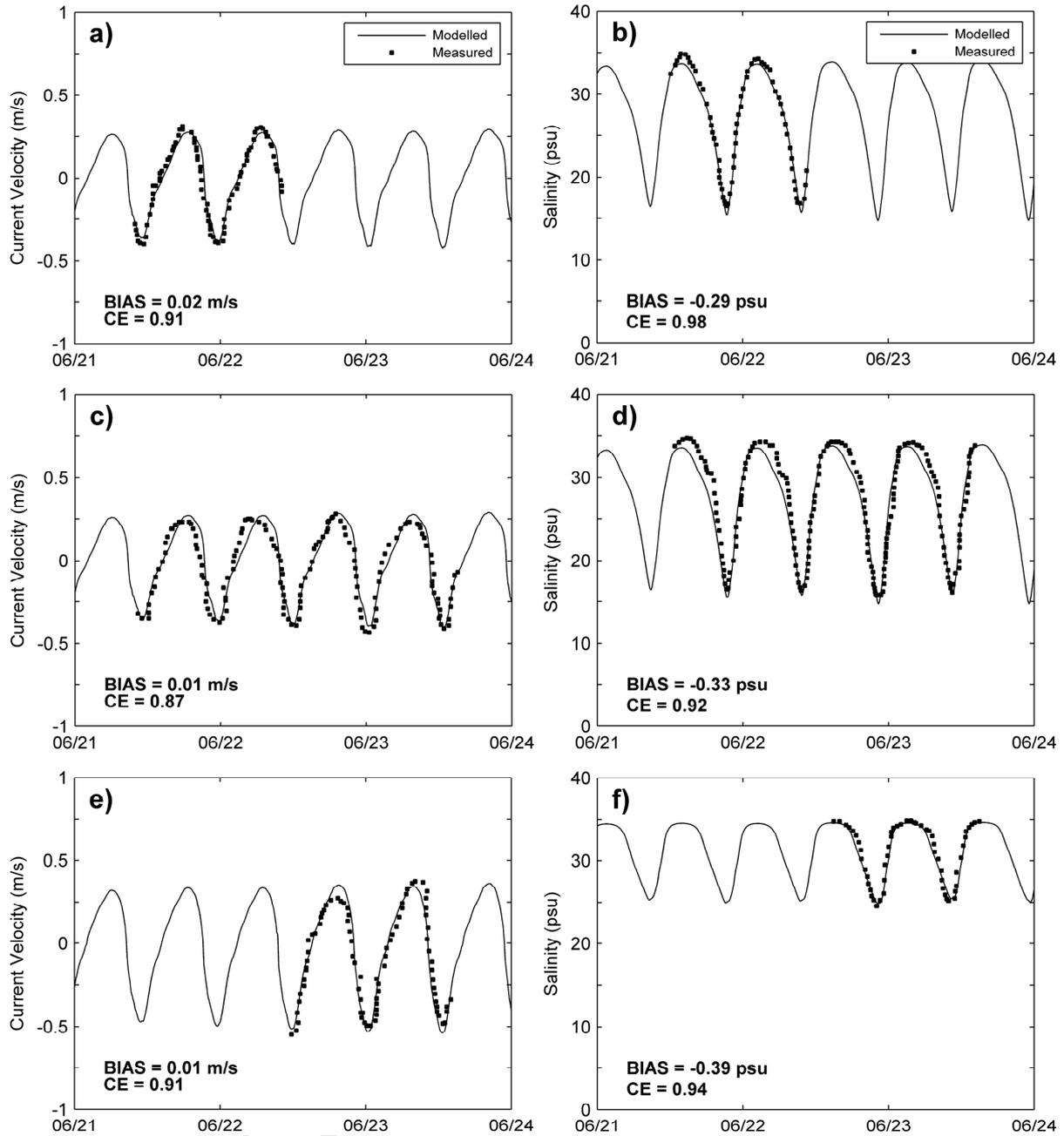


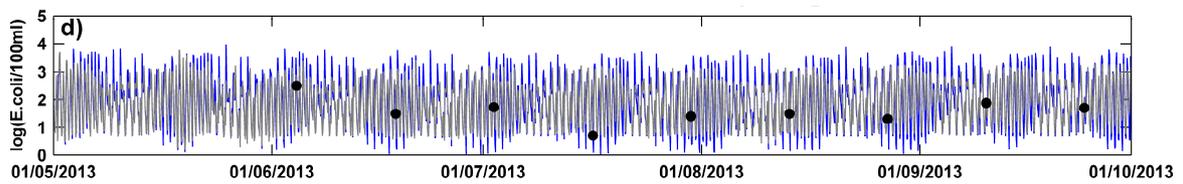
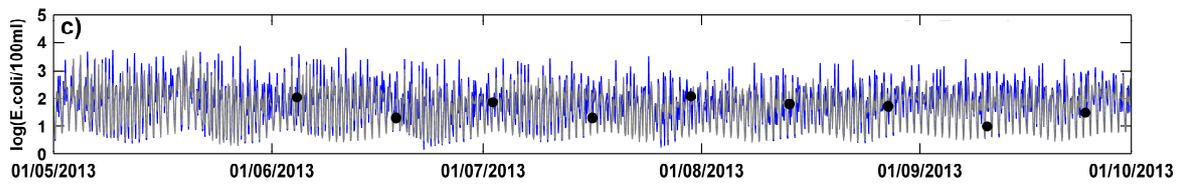
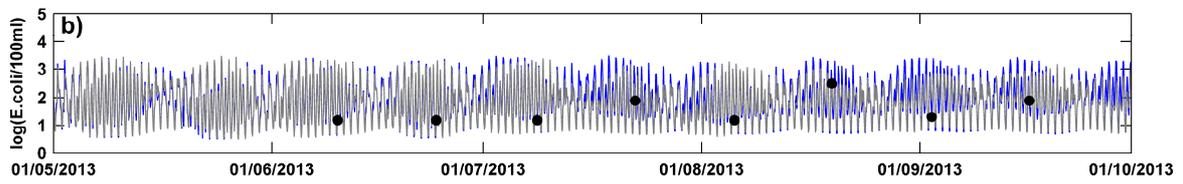
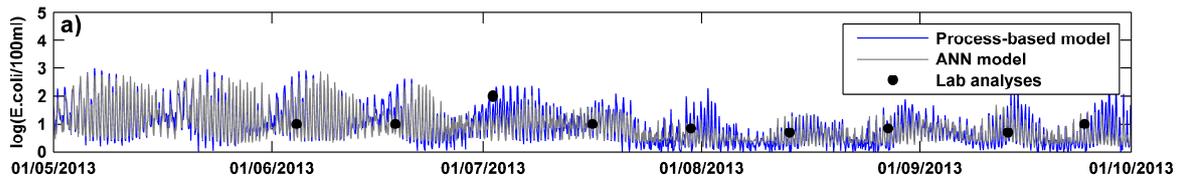
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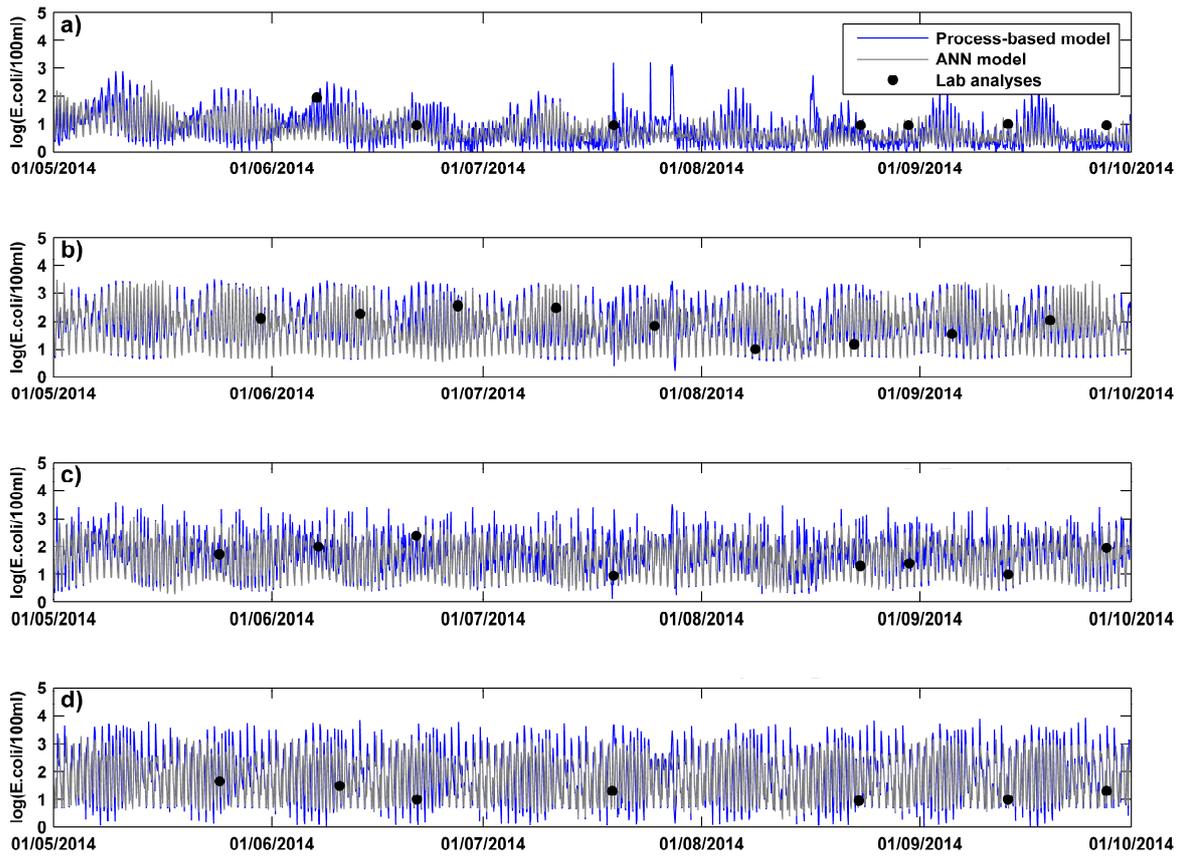
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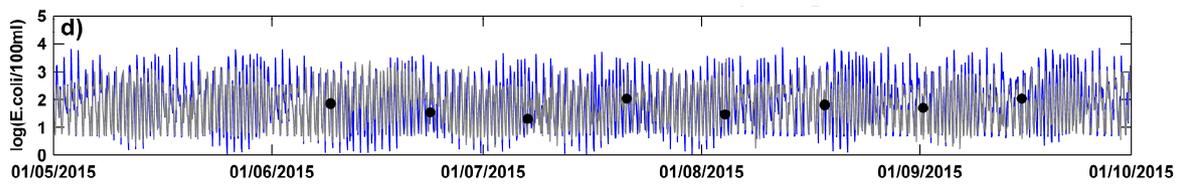
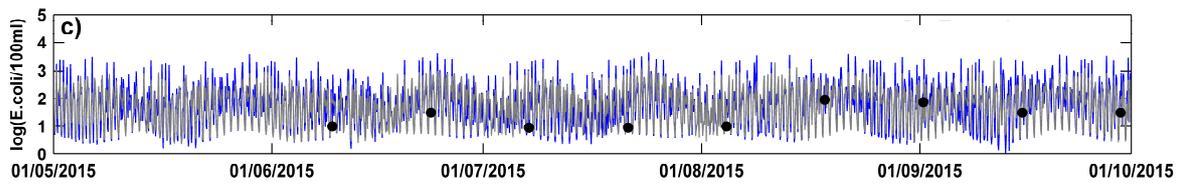
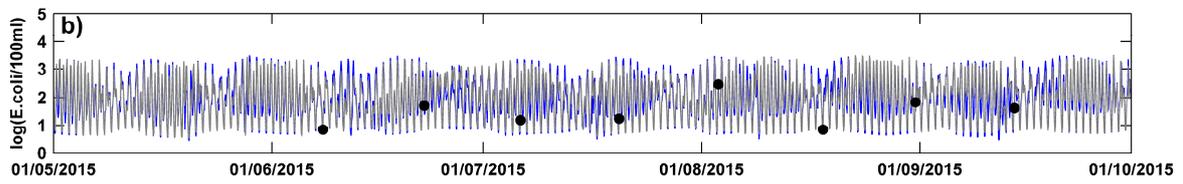
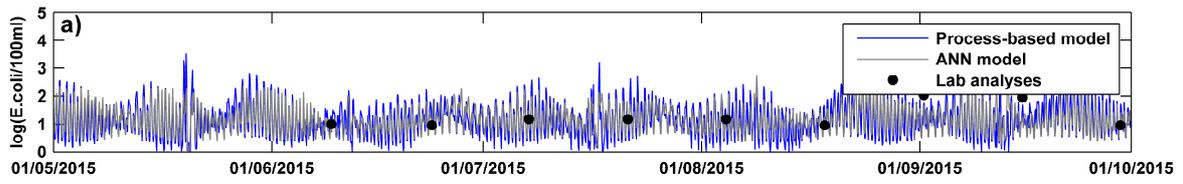






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- The method integrates laboratory analyses, numerical modelling and machine learning.
- ANN configuration for predicting *E. coli* concentration in estuaries is determined.
- ANNs are viable emulators of process-based models driven by highly variable forcing.
- The longer forecasting, the greater the reduction in computational time using ANN.
- Real-time management of bathing water quality is enabled by using ANNs.

**Declaration of interests**

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

The authors declare the following financial interests/personal relationships which may be considered as potential competing interests: