

# Numerical simulation of bus aerodynamics on several classes of bridge decks

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## Abstract

This paper is focused on improving traffic safety in bridge under crosswind conditions because adverse wind conditions increase the risk of traffic accidents. In this work, two ways in order to improve traffic safety are proposed to study. Vehicle stability can be improved on the one hand by means of wind fences installed on bridge deck and on the other hand by modifying design parameters of the infrastructure. Specifically, this study examines the influence of different parameters related to bridge deck configuration on the aerodynamic coefficients acting on a bus model under crosswind conditions. The aerodynamic coefficients related to: side force; lift force and rollover moment, were obtained for three classes of bridge deck (box, girder and board) by numerical simulation. The FLUENT code was used in order to solve Reynolds-averaged Navier–Stokes (RANS) equations along with the SST  $k-\omega$  turbulence model. Two crash barriers located on the box bridge deck were replaced by an articulating wind fence model and then, the effect of angle between the wind fence and the horizontal plane on the bus aerodynamic was presented. The risk of having rollover accidents is slightly influenced by the bridge deck type for a yaw angle range between  $75^\circ$  and  $120^\circ$ . In order to study the effect of yaw angle on aerodynamic coefficients acting on bus, both the bus model and bridge model were simultaneously rotated. The minimum value of rollover coefficient was obtained for an angle  $60^\circ$  between the wind fence slope and the horizontal plane. The only geometry parameter of box bridge deck which significantly affects bus aerodynamics is the box height. The present research highlights: the usefulness of computational fluid dynamics codes for improving traffic safety, the performance of articulating wind fence, which geometry parameters of box deck have a significant influence on bus stability.

**Keywords:** Crosswind; Bridge decks; Heavy vehicle aerodynamics; Finite volume method (FVM); Computational fluid dynamics (CFD).

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## 34 **1. Introduction**

35 Wind conditions in locations such as bridges and viaducts may be especially negative for vehicle  
36 stability. Particularly, the control of high-sided vehicles requires more attention because they are  
37 more likely to undergo rollover or lane changing accidents (Baker & Reynolds, 1992 and Dorigatti  
38 et al., 2012). Nevertheless, in Cheung and Chan (2010), it is demonstrated that light-weight  
39 vehicles are also likely to suffer lack of comfort while driving on bridges under relatively low  
40 wind velocity. Nowadays, some authorities around the world opt for closing bridges when the  
41 wind velocity exceeds a limit value. In some cases this wind velocity limit is set based on previous  
42 experience instead of being the result of a quantitative procedure, which better guarantees user  
43 safety.

44 The interruption of traffic on some bridges may involve huge economic losses, especially if the  
45 bridges are associated with the local market logistics. Therefore, viaducts or bridges usually  
46 exposed to cross-wind conditions can be the cause of safety and economic issues. As a  
47 consequence, several research works have dealt with the outcome of crosswind on bridges (Wang,  
48 Xu, Zhu, Cao & Li, 2013 and Wang, Xu, Zhu & Li, 2014). Some of them have focused on the  
49 development of procedures to regulate traffic such as Cheung and Chan (2010) and Guo and Xu  
50 (2006), while other research studied wind fence efficiency (Rocchi, Rosa, Sabbioni, Sbroisi &  
51 Belloli, 2012 and Kozmar, Procino, Borsani & Bartoli, 2012). Improving knowledge about the  
52 aerodynamic behaviour of wind fences located on bridge decks is necessary, since many  
53 researchers have focused on the design of wind fences located on the ground where the wind  
54 conditions are different (Judd, Raupach & Finnigan, 1996 and Chen, Wang, Sun & Li, 2012).

55 Another aspect studied is the huge influence of wind conditions (wind velocity, approaching  
56 turbulence, wind direction, etc.) on vehicle stability. Kozmar *et al.* (2012) highlighted that high-  
57 sided vehicles suffer higher wind loads as the angle formed by the wind direction and the  
58 horizontal line in a vertical plane was increased. Charuvisit, Kimura and Fujimo (2004) indicated  
59 that an increase in wind velocity reduced the comfort during driving. In addition, the worst value  
60 of the horizontal angle formed by wind direction and the normal to bridge direction was 30° for

61 the stability of vehicle. However, Bettle, Holloway and Benart (2003) particularized the most  
62 critical wind direction for the windward/leeward lane as  $90^\circ$  and  $56.3^\circ$  respectively. Another wind  
63 characteristic which should be considered when evaluating the risk of accident on roads is the  
64 presence of wind gusts because of their negative influence on vehicle stability (Kozmar, Butler  
65 & Kareem 2009).

66 Vehicles suffer huge instabilities under cross-wind conditions (Argentini, Ozkan, Rocchi, Rosa  
67 & Zasso, 2011 and Wang et al., 2014) at the towers on the bridges. In Charuvisit *et al.* (2004) the  
68 effect of tower geometry on vehicle stability was studied. The maximum yawing acceleration on  
69 the vehicle was higher for one of the tower models, so some modifications in the tower design  
70 could benefit traffic safety. Other part of bridges which can affects vehicle stability, is the bridge  
71 deck model's geometry (Dorigatti et al., 2012 and Suzuki, Tanemoto & Maeda, 2003). In  
72 Dorigatti *et al.* (2012), the aerodynamic coefficients of three types of vehicles (van, truck and  
73 bus) were obtained for two bridge deck models, and the bus stability was sensitive to the different  
74 geometries. Suzuki *et al.* (2003) found out that an increase in the thickness of a bridge girder also  
75 causes the aerodynamic side force coefficient of vehicles to rise. Cheli, Corradi, Rocchi, Tomasini  
76 and Maestrini (2010) and Bettle *et al.* (2003) obtained the aerodynamic loads acting on vehicles  
77 located in the windward lane and the leeward lane. In both studies, the results indicated that  
78 aerodynamic loads were higher when the vehicles are travelling closer to the windward edge of  
79 the deck. Specifically, the rollover moment in the leeward lane was 30% lower than in the  
80 windward lane. To carry out these studies, the most frequently used techniques are (Bettle et al.,  
81 2003, Cheli, Corradi, Sabbioni & Tomasini, 2011 and Hibino, Shimomura & Tanifuji, 2010):  
82 numerical simulation (CFD), wind tunnel test and full scale experiments. In many cases the results  
83 from numerical simulations are contrasted with the other techniques (Sterling et al., 2010 and  
84 Sun, Zhang, Guo, Yang & Liu, 2014).

85 This study has been proposed to help competent authorities in traffic safety management on  
86 bridges under adverse crosswind conditions. As a consequence, the following objectives are  
87 established:

- 88 • Identify which type of bridge decks most adversely affects bus aerodynamics.
- 89 • Obtain the relationship between the angle of the wind fence slope and the aerodynamic
- 90 coefficient acting on the bus model when it is located on a bridge.
- 91 • Determine whether it is possible to reduce the aerodynamic coefficients of bus by
- 92 modifying the design parameters of a bridge deck.

93 To achieve these objectives, 3D CFD numerical simulations were carried out in order to study the  
94 stability of a 1:40 scale model bus located on a bridge under cross-wind conditions. During this  
95 study, the main difficulties were found when: setting the grid parameters, selecting one turbulence  
96 model between the options provided by FLUENT and proposing the most interesting study cases.  
97 In order to overcome these difficulties, on the one hand several numerical models with different  
98 grid sizes and turbulence models were solved and, on the other hand, investigations focused on  
99 the effect of crosswind conditions on traffic safety in bridge decks were studied in detail to  
100 propose interesting study cases (Wang et al., 2013; Wang et al., 2014 and Dorigatti et al., 2012).

101 In section 2, both the numerical setup and mathematical method required to solve the studied  
102 cases are defined. Then, in section 3, the procedure used both to select the turbulence model and  
103 to define the grid size setup is presented considering experimental data (Dorigatti et al., 2012). In  
104 section 4, the geometric parameters of a bridge deck with box are defined which were studied by  
105 using surface response methodology along with the Design of Experiment (DOE) technique. In  
106 section 5, results of bus aerodynamics and flow behavior around the bridge decks and an  
107 articulating wind fence are indicated and discussed. In the last section, the main conclusions from  
108 the results of this study are explained.

## 109 **2. Numerical method**

110 All numerical models were solved by using the CFD code, FLUENT-ANSYS. Next, the  
111 geometries for the bus and the bridge decks proposed to study are presented.

### 112 **2.1. Bridge decks and aerodynamic loads**

113 The influence of the bridge deck typology on vehicle stability was studied by obtaining the  
114 aerodynamic coefficients from the bus model. Among the types of bridge deck sections built  
115 nowadays, the following three were proposed for study: box, board, and girder (see Fig. 1). The  
116 aerodynamic coefficients acting on the bus located on the bridge decks were obtained for four  
117 yaw angle values: 75°, 90°, 105° and 120°. Detailed information about the dimensions of both the  
118 bus and box bridge deck (model scale 1:40) can be found in Dorigatti et al. (2012). This  
119 experimental study in wind tunnel was used to fit the numerical setup parameters and then this  
120 setup was applied to the other cases proposed to study. Four crash barriers 1250 mm high at full  
121 scale and porosity (ratio between open area and total area projected on the normal plane to wind  
122 direction) approximately 35%, were installed on the three types of bridge deck. These barriers are  
123 composed of two strips with a width of 406.25 mm and a gap between them of 218.75 mm in full  
124 scale. An additional model was built for the box bridge deck in which two of the crash barriers  
125 were replaced by solid and articulating wind fences (porosity 0%). The wind fence model was  
126 divided into two parts of equal length, but the upper part varied its slope angle with the road plane  
127 while the lower part was kept in vertical position (90° with the road plane) for all cases.  
128 Specifically, five values of slope angle,  $\beta$ , between 60° and 120° were studied. In vertical position,  
129 the articulating wind fence keeps the same height of crash barrier. Furthermore, the effect of the  
130 box deck design parameters (Fig 1 a) on the aerodynamic loads acting on the bus was studied by  
131 applying the response surface methodology.

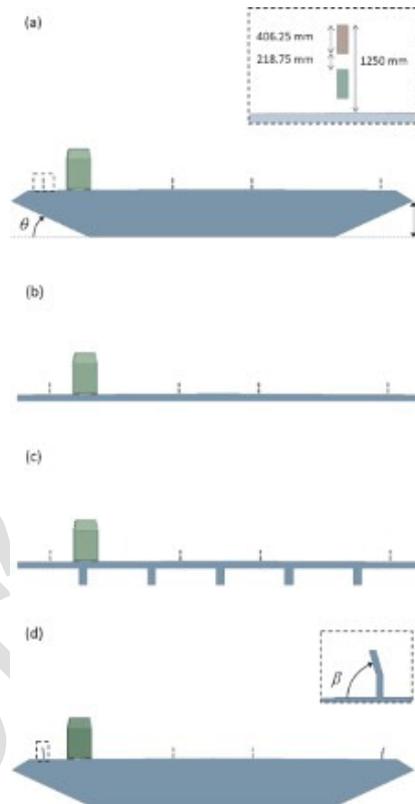
132 On the other hand, the aerodynamic loads and moments acting on the bus obtained are side force  
133 ( $F_S$ ), lift force ( $F_L$ ) and rollover moment ( $M_R$ ) (Fig. 2). The moments caused by side force and  
134 lift force were obtained by integrating the pressure about origin of reference system (point O in  
135 Fig. 2), due to wind force components acting in the  $x$  and  $y$  axes respectively. The rollover moment  
136 was calculated by adding the moments caused by side and lift forces. Then, these aerodynamic  
137 loads were become into non-dimensional coefficients using the following equations:

$$C_S = \frac{F_S}{\frac{1}{2}\rho U^2 A_S} \quad (1)$$

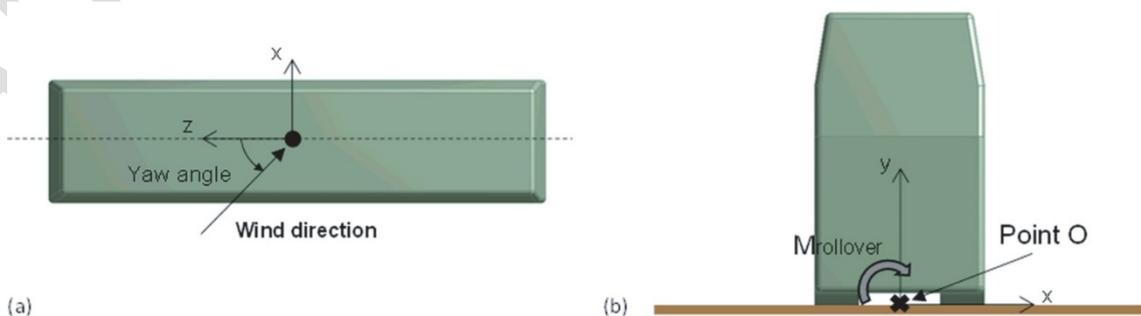
$$C_L = \frac{F_L}{\frac{1}{2}\rho U^2 A_S} \quad (2)$$

$$C_R = \frac{M_R}{\frac{1}{2}\rho U^2 A_S H} \quad (3)$$

138 where  $\rho$  is the density of the air,  $1.18 \text{ kg/m}^3$ ;  $A_S$  is the side area of the bus,  $27830 \text{ mm}^2$  (scale  
 139 model); and  $H$  is the height of the bus,  $110 \text{ mm}$  (scale model) and  $U$  is the undisturbed wind speed  
 140 measured  $7 \text{ m}$  upstream of the bridge deck section model.



141  
 142 **Fig 1** Configurations of bridge decks studied: (a) box, (b) board, (c) girder and (d) box with solid fence.  
 143



144 (a) (b)  
 145 **Fig 2** Sign convention for forces and moment and origin of coordinate reference system.

## 146 2.2. Mathematical approach

147 The lower region of the atmosphere where transport infrastructure are located is characterized by  
148 turbulent flows. Consequently, the Reynolds-averaged Navier-Stokes (RANS) equations in  
149 steady state along with a turbulence model were solved to predict the aerodynamic coefficients  
150 acting on the bus by using the finite volume method. In this work, a steady state analysis is applied  
151 instead of transient analysis because in order to achieve the objectives of study is not required. In  
152 addition, the computational cost and CPU time is quite higher for unsteady simulation as  
153 compared to the steady approach. For example, in turbomachinery applications as a rough  
154 estimation, Large Eddy Simulation (LES) would need around 5000 times the computational time  
155 of a steady analysis concerning RANS (Gourdain, Gicquel & Collado, 2012). The flow field  
156 around a vehicle is unsteady and very complex, including various time and length scales.  
157 Therefore, if the study requires high accuracy in the result obtained it would be necessary to carry  
158 out a transient analysis. However, if the goal is to predict which structural configuration  
159 influences more negatively the vehicle stability, as in the present study, the steady approach  
160 should be accurate enough. Nevertheless, to study the effect of using a steady approach instead  
161 of an unsteady one, the aerodynamic coefficients acting on the bus were obtained by both  
162 procedures for the box bridge deck (Section 4). The RANS equations govern the fluid movement  
163 through the three fundamental conservation principles: mass, momentum and energy. On the other  
164 hand, the turbulence models help to estimate the Reynolds stress and consequently, to close the  
165 equation system composed by the RANS equations. Among the potential turbulence model  
166 implemented in the CFD code, the bus aerodynamic coefficients were obtained for three of them:  
167 Spalart-Allmaras (Spalart & Allmaras, 1994), standard  $k - \varepsilon$  (Launder & Spalding, 1974) and SST  
168  $k - \omega$  (Menter, 1994). The near wall region is solved by different methods according to the  
169 turbulence model applied. The Spalart-Allmaras model uses a formulation that blends  
170 automatically from a viscous sublayer formulation to a logarithmic formulation based on the value  
171 of  $y^+$ . Therefore, this wall treatment can be used to solve the near wall region with independence  
172 of the refinement level of the grid. As for the standard  $k - \varepsilon$  turbulence models, an enhanced wall

173 treatment was chosen to solve near wall region instead of a standard wall function, because of the  
174 higher accuracy of this method to predict the flow behavior in the air regions close to walls. This  
175 approach combines a two-layer model with the so-called enhanced wall functions. If the near-  
176 wall mesh is fine enough to be able to resolve the viscous sublayer ( $y^+ \approx 1$ ), a two-layer approach  
177 is applied, while if mesh is coarse, enhanced wall functions are used. The enhanced wall functions  
178 formulate the law of the wall as a single law for the entire wall region (viscous sublayer, buffer  
179 region and fully-turbulent outer region) by blending the linear (laminar) and logarithmic  
180 (turbulent) law-of-the-wall. This feature allows solving the near wall regions with different  
181 density of grids. The main difference between the standard  $k - \varepsilon$  model and  $SST k - \omega$  model  
182 regarding the near wall treatment applied, consists of the fact that the  $\omega$ -equation can be solved  
183 through the viscous sublayer without the need for a two-layer approach that has to be used with  
184 the  $\varepsilon$ -equation. The results obtained for each turbulence model studied will be presented in Section  
185 3. Detailed information on the RANS equations and the turbulence models equations can be found  
186 in FLUENT user manual.

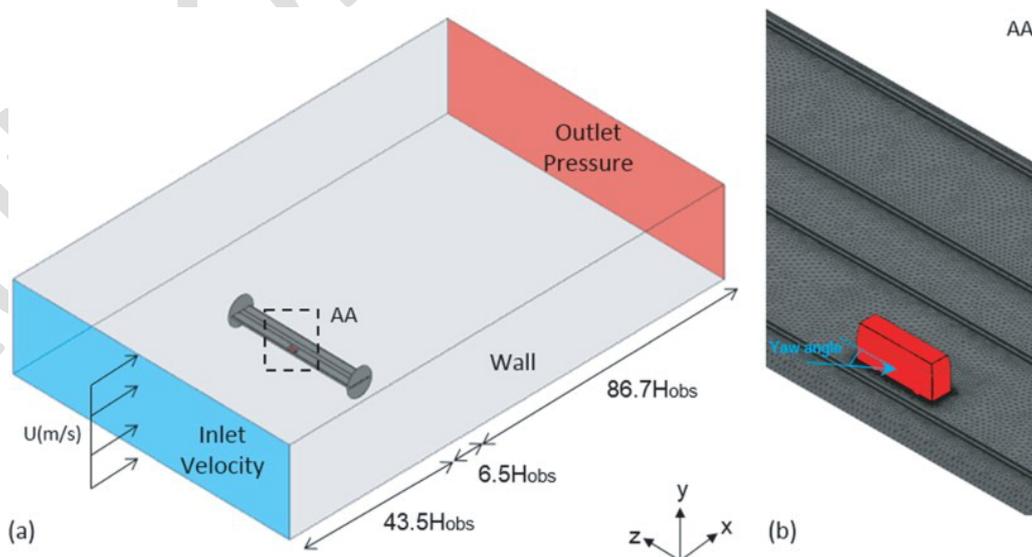
187 In the finite volume method, the fluid domain is divided into a finite number of cells with nodal  
188 points. The shape and position of control volumes with respect to grid cells is defined according  
189 to a cell-centered scheme. Therefore, the control volumes are equal to the grid cell both in shape  
190 and position. These control volumes are delimited by the nodal point in the grid and the variables  
191 values are stored at centroids of the grid cells. The governing partial differential equations are  
192 integrated over the control volumes to evaluate the convective and viscous fluxes as well as the  
193 source term. Then, the equations in integral form are discretized to transform them into algebraic  
194 equations by applying quadrature formulae. These algebraic equations contain the values of  
195 variables and fluxes at the control volume faces which will be expressed in terms of the center  
196 values by interpolation scheme.

197 In the present study, a second-order upwind scheme was used for the moment equations and the  
198 turbulence quantities and, second order scheme for pressure equation during the spatial

199 discretization. The variable gradients between the cell centroids were evaluated by the Least  
200 Squares Cell-Based method. The SIMPLE algorithm of Patankar and Spalding (1972) was used  
201 to solve pressure–velocity coupling. Finally, the algebraic equation system was solved by an  
202 iterative method.

### 203 2.3. Boundary conditions and grid

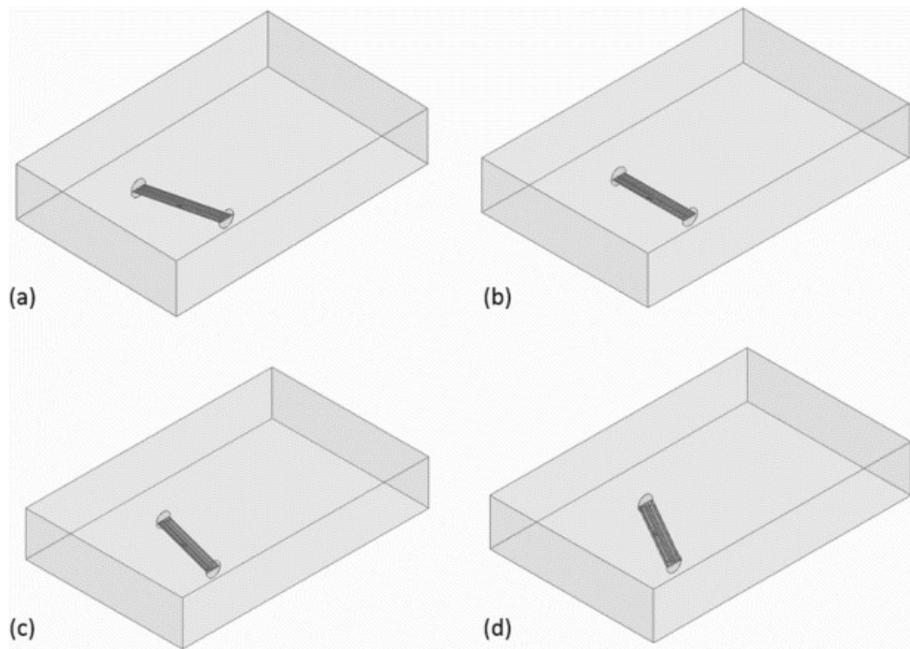
204 The three-dimensional domain, which contains the regions of air around both the bus and bridge  
205 deck models, has a cross section with the same dimensions that Wind Tunnel section of  
206 Polytechnic of Milano, 14 m x 4 m (Bocciolone, Cheli, Corradi, Muggiasca & Tomasini, 2008).  
207 The upstream and downstream distance between the bridge deck and the boundary surfaces (Fig.  
208 3) exceeded the minimum values established under the European regulation EN 14067-6:2010.  
209 These distances are expressed as function of the obstacle height,  $H_{obs}$  (distance between the top  
210 surface of bus and the bottom surface of bridge deck). The numerical simulation was carried out  
211 with still bus model without reproducing the relative movement between bus and bridge deck  
212 because computational cost is greater and, vehicle motion has no significant influence on the force  
213 coefficients according to Bocciolone et al. (2008). In order to obtain the aerodynamic coefficients  
214 for each value of the yaw angles studied when the bus model is located on the three types of  
215 bridge decks, the bus and bridge deck were rotated together as it is shown in Fig. 4.



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**Fig 3** (a) Geometrical model of the numerical domain and boundary conditions. (b) Bus model on the bridge deck for the numerical simulation.

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**Fig 4** Yaw angle positions studied by numerical simulation: (a) 75°; (b) 90°; (c) 105°; (d) 120°.

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The domain was broken up in two sub domains (far domain and near domain in Fig. 5) to build a finer grid in the air region close to the bus model where strong gradients of the flow variables originate. In the near domain two types of cells were used, specifically wedge cells for the air regions near bus surface by applying a inflation control and tetrahedral cells for the other region of domain, while in the far domain was only used tetrahedral cells. The wedge grid performs well in solving the near-wall region problem, which can be subdivided into three layers: viscous sublayer; buffer layer; and log-law region. A total of ten inflated layers of wedge with a growth rate of 1.1 make up the wedge grid, the thickness of the first layer being set to obtain an  $y^+$  not exceeding 1. The variable  $y^+$  is the dimensionless distance from the wall, related to the distance from the wall  $y$ , shear velocity  $u_\tau$  (value of the friction velocity obtained from the experimental wind profile) and kinematic viscosity  $\nu$  as follows:

$$y^+ = \frac{u_\tau \cdot y}{\nu} \quad (4)$$

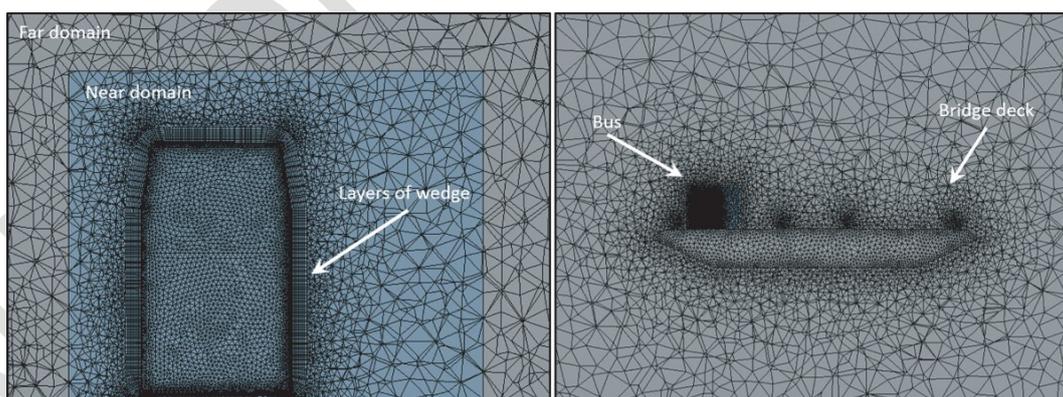
234 A finer grid was built for both the air region close to curved surface and small gap of air between  
235 walls by using curvature and proximity controls. In the next section, the boundary condition setup  
236 is detailed (Tu, 2013, Moaveni, 2014 and Madenci & Guven, 2015):

237 • **Inlet Velocity:** A uniform profile of 13.5 m/s was defined for the flow velocity,  $U$  (see  
238 Fig 3).  $V, W = 0$  (components of wind velocity in  $y$  and  $z$  directions are zero). The turbulent  
239 length scale,  $l$  and turbulence intensity,  $I$  are  $\sim 30$  m (full scale value) and 6% respectively  
240 according to experimental conditions (Dorigatti et al., 2012). The flow is incompressible  
241 and subsonic (Versteeg & Malalasekera, 2007):

$$\text{Ma} = \frac{U}{c} = \frac{13.5 \text{ m/s}}{340 \text{ m/s}} = 0.04 \ll 0.3 \Rightarrow \nabla \cdot \vec{u} = 0 \quad (5)$$

242 • **Outlet Pressure:** Relative pressure  $p = 0$ . The normal gradients of all variables were set  
243 equal to zero (Neumann boundary condition). Under back flow conditions, the average  
244 turbulence intensity,  $I$ , and turbulent length scale,  $l$ , were assigned the inlet boundary  
245 condition values.

246 • **Solid walls:** A non-slip condition ( $U, V, W=0$ ) was adopted on the solid surfaces of the  
247 domain. The roughness height was set to a null value, therefore the boundary surface  
248 behaves as a smooth surface.



249  
250 **Fig 5** View of the grid employed for the different regions of the domain.

### 251 3. Grid size and turbulence closure model

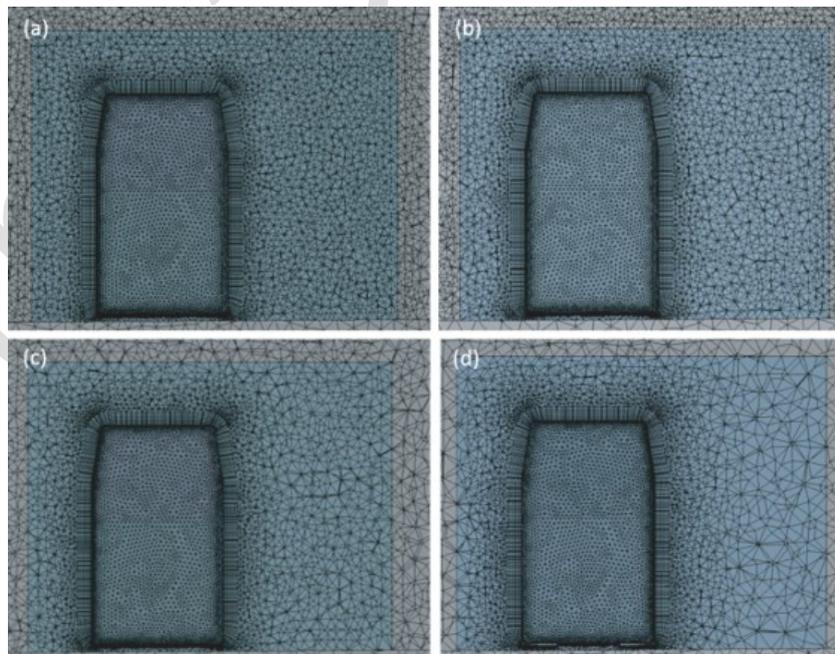
252 The spatial discretization error can be decreased by diminishing the cell size but a smaller cell  
253 size increases the total number of cells in the grid and, in consequence the computational cost.  
254

255 Therefore, a grid size independence study was carried out to avoid wasting computational power.  
256 In particular, the aerodynamic coefficients acting on the bus located on the box bridge deck with  
257 a yaw angle of  $90^\circ$  were obtained for four grid sizes: 13.4; 16.2; 19.1 and 22.8 million. The  
258 distribution of elements by types for the grid size built is exhibited in Table 1. In the sensitivity  
259 analysis of grid size, the  $SST k - \omega$  model was used instead of the Spalart-Allmaras and standard  
260  $k - \varepsilon$  models. This is due to the harder requirements required by this model on the mesh  
261 refinement as compared to the others.

262 Table 1. Distribution of elements for several grid sizes.  
263

Grid size (million)	Tetrahedrons (%)	Wedges (%)
13.4	94.02	5.98
16.2	95.05	4.95
19.1	89.7	10.3
22.8	96.48	3.52

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265 The different levels of refinement were obtained by applying a size control function on the near  
266 domain, which is the air region where the variable gradients are stronger and a smaller cell size  
267 is likely required (Fig 6).



268  
269 **Fig 6** Grid in the region where the refinement was applied for the following grid sizes: (a) 22.8; (b) 19.1;  
270 (c) 16.2 and (d) 13.4 million.

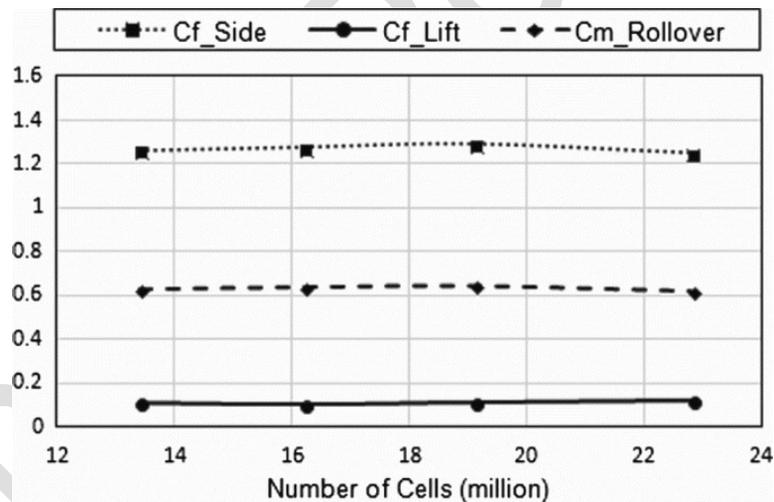
271 The results indicate that the aerodynamic coefficients acting on the bus are quite independent of  
 272 the grid size for the studied range of cells number (Fig. 7). Thus, the grid setup defined for 13.4  
 273 million cells was applied to the other numerical simulations.

274 The grid size varies with the yaw angle studied for the three types of bridge decks. Specifically,  
 275 the maximum variation of grid size with the yaw angle taking as the reference the grid size value  
 276 for 90° yaw angle in each bridge deck type and, keeping the same grid setup, is shown in the Table  
 277 2.

278 **Table 2.** Yaw angle where the maximum variation of grid size with respect to 90° of yaw angle was obtained  
 279 for each bridge deck.  
 280

Bridge deck	Yaw angle (°)	Maximum variation of grid size (million)
Box	75	1
Board	120	0.4
Girder	120	1.9

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283 **Fig 7** Influence of grid size on aerodynamic coefficients of bus for box bridge deck.

284 Then, the relative errors between the aerodynamic coefficients obtained by numerical modelling  
 285 with three turbulence models (Spalart-Allmaras, standard  $k-\varepsilon$  and  $SSTk-\omega$ ) and, by  
 286 experimental test (Dorigatti et al., 2012) were determined to select the turbulence model.

287 The lowest relative error in the three coefficients was obtained with the  $SSTk-\omega$  model (see Table  
 288 3); therefore, this model was finally used in the other scenarios. The lift coefficient exhibits the

289 highest relative error, this could be because the components, which were used to link the balance  
290 and the bus model in the experimental test, were not defined in the numerical simulation since  
291 these geometric details are not indicated in Dorigatti et al. (2012). Specifically, the experimental  
292 value of lift coefficient is lower than the value obtained by numerical model, due to the smaller  
293 air gap between the bus model and the road surface as consequence of components used to link  
294 the bus model and the balance in the experimental test. This smaller gap causes higher values of  
295 velocity and lower values of static pressure in the air flow under the bus and consequently, the  
296 lift force diminishes as compared with numerical values. On the other hand, these components  
297 are actually supposed to modify the air flow through the gap between the bus and road surface  
298 with respect to real conditions.

299 The results of numerical models can be considered accurate enough to reach the objective set for  
300 this study, due to the following reasons: the weight of lift coefficient on the rollover coefficient  
301 is rather softer than the side coefficient; the lift force values are quite lower than the side force  
302 and as consequence when the difference between numerical and experimental values are  
303 expressed in terms of relative error, the error relative of lift coefficients is quiet higher than the  
304 others; and finally the relative error of the side coefficient is low enough to rely on this value.

305 One of the main characteristic of  $SST k - \omega$  model is its good performance in order to solve low  
306 Reynolds flows as those present in the near wall regions (ANSYS Inc. 2011 and Tu, 2013). Many  
307 authors recommend that the  $SST k - \omega$  model should replace the standard  $k - \epsilon$  model as the first  
308 choice (Andersson et al., 2011).

309 **Table 3.** Relative error for the aerodynamic coefficients as a function of turbulence model in the box bridge  
310 deck.

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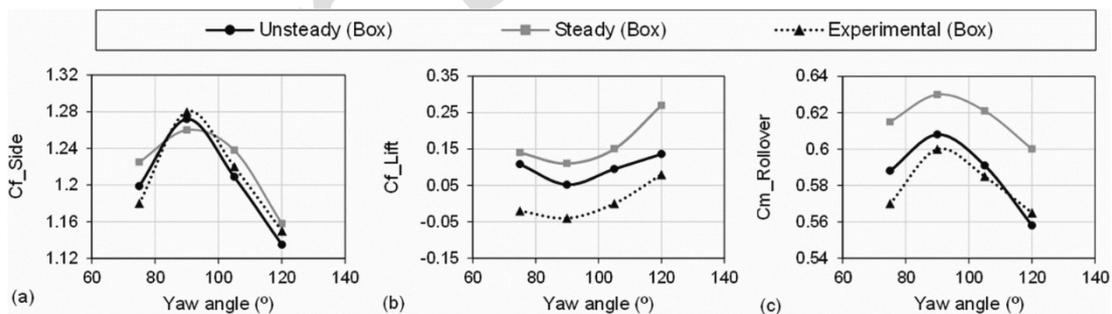
Turbulence Model	Aerodynamic Coefficients		
	Cf_Side	Cf_Lift	Cm_Rollover
$K-\epsilon$	0.18	7.00	0.12
$SST k-\omega$	0.01	3.75	0.05
<i>Spalart-Allmaras</i>	0.25	6.50	0.23

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313

#### 314 4. Comparison between unsteady and steady aerodynamic coefficients

315 An unsteady numerical simulation with the  $SSTk-\omega$  model was carried out prior to the use of the  
316 steady approach for the proposed cases. Thus, the box bridge deck was used to calculate the  
317 aerodynamic coefficients of bus by applying both a steady approach as unsteady. The  
318 nondimensional time step was set as  $\Delta t^* = \Delta t \cdot U_\infty / H = 0.097$  ( $H$  is the height of bus as in Ai &  
319 Mak, (2015)), keeping a CFL number (Courant–Friedrichs–Lewy) below 1 in the most of the cells  
320 of regions with flow detaching. The simulations were run for a time of  $2712 \Delta t^*$ , the time  
321 required by the air flow to cover 3 times the domain. The first  $556 \Delta t^*$  were not considered to  
322 calculate the average values of aerodynamic coefficient because the values were not stable. Fig 8  
323 shows the relationships between the average values of the aerodynamic coefficients and the yaw  
324 angle for the two numerical approaches (steady and unsteady) and the experimental test (Dorigatti  
325 et al. (2012)). The unsteady analysis exhibits values of aerodynamic coefficients closer to  
326 experimental measurements, however, the variations of the aerodynamic coefficients with the  
327 yaw angle are quiet similar by applying both approaches. Therefore, the steady approach will  
328 allow the obtention of accurate enough trends as for reaching the objectives of this study.



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331 **Fig 8** Comparison between the aerodynamic coefficients –(a) side force, (b) lift force and (c) rollover  
332 moment– obtained by steady and unsteady approaches and experimental test (Dorigatti et al. (2012)).  
333

#### 334 5. DOE methodology

335 In order to study the effect of the box deck design parameters on the aerodynamic loads acting on  
336 the bus, a sensitivity analysis and a design of experiments (DOE) analysis were carried out. In  
337 this sense, the result from DOE analysis enables the optimization of the box deck configuration.  
338 A central composite design (CCD) was chosen to determine the number of cases required to

339 perform the study as a part of DOE methodology (Myers, Montgomery & Anderson-Cook, 2009  
340 and Del Coz Díaz, Serrano López, López-Colina & Álvarez Rabanal, 2012). Then, the output and  
341 input variables were selected throughout the range of study in the case of the latter. Each  
342 combination of input variables requires calculating the output variables by means of a new volume  
343 finite analysis. A response surface model is obtained according to the second order polynomial  
344 regression model set and the results from the DOE study. The response surface is an explicit  
345 approximation function, which expresses the output data as a function of input data by the fitting  
346 algorithm indicated in the DOE methodology.

347 As a part of the DOE procedure the higher-order derivatives are evaluated from the results  
348 generated for each design point, the order of the derivatives indicates the order of the  
349 approximation expressions. The second-order model applied in the present work considering two  
350 input variables can be written as follow:

$$Y = \lambda_0 + \lambda_1 x_1 + \lambda_2 x_2 + \lambda_{11} x_1^2 + \lambda_{22} x_2^2 + \lambda_{12} x_1 x_2 + error \quad (6)$$

351 where,  $Y$  is the predicted response variable, the  $X$ s are the factors or input variables. There are 1  
352 two-way interaction terms according to  $p(p-1)/2 = 2 \times 1/2 = 1$ , two quadratic terms and two  
353 linear terms. The regression coefficients,  $\lambda$ s were calculated by the ordinary least squares (OLS)  
354 procedure, where the OSL estimator can be written as:

$$\vec{\lambda}_{OLS} = \left( \vec{X}^T \vec{X} \right)^{-1} \vec{X}^T \vec{Y} \quad (7)$$

355 where  $\vec{X}$  is the extended designed matrix for the input variables including the coded levels and  
356  $\vec{Y}$  is a column vector of output variable values obtained for the specify points in the DOE. The  
357 input variables over their variation range (maximum, minimum and current value) and the output  
358 variables are as follows:

- 359 • **Input variables** (see Fig. 1): the height of deck box,  $h$  and angle of deck box,  $\theta$ . On the  
360 one hand, the height of deck box is varied from 25 mm to 92.5 mm (in full scale from 1  
361 m to 3.7 m), the starting design value being of 58.75 mm (2.35 m in full scale). On the

362 other hand, the range of deck box angle is from  $15^\circ$  to  $45^\circ$ , with a starting design value of  
363  $30^\circ$ .

364 • **Output parameters:** the aerodynamic coefficients associated with side force, lift force  
365 and rollover moment.

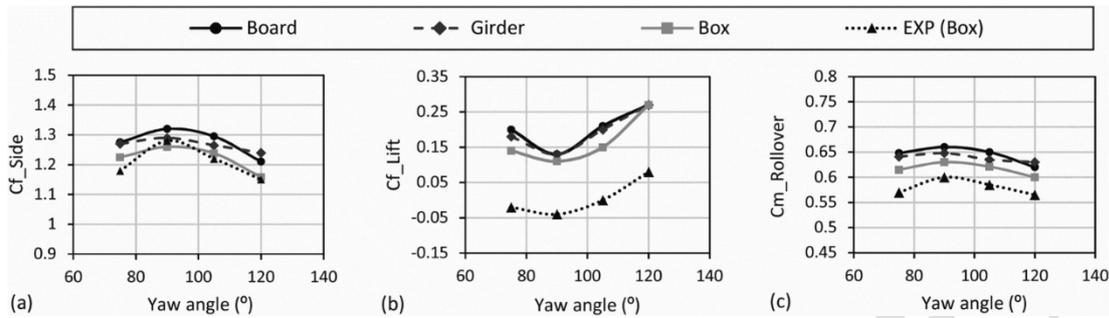
## 366 6. Result and discussion

367 In this section, the influence of both the bridge deck configuration and of wind fence slope on  
368 aerodynamic loads which contribute to the rollover accident under crosswind conditions, is shown  
369 and discussed.

### 370 6.1. Bridge deck type effect

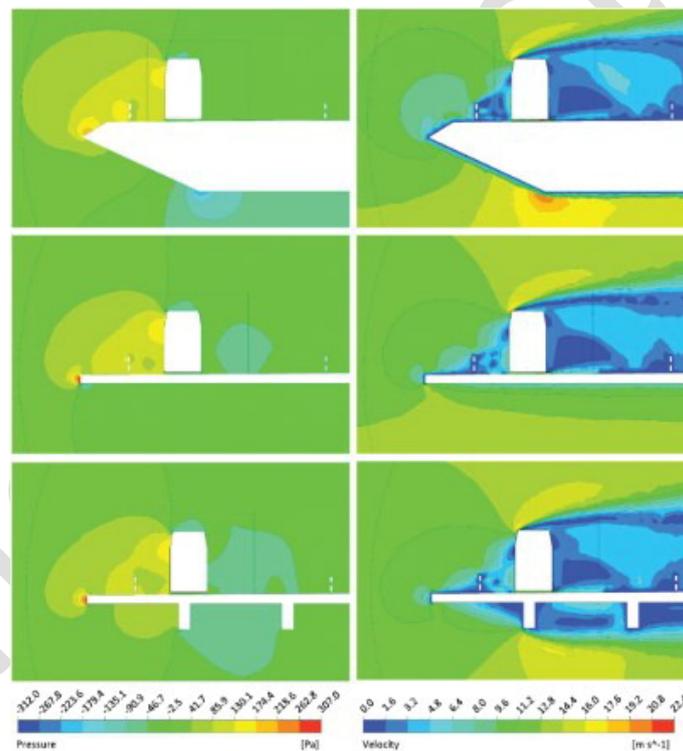
371 In order to study the effect of the bridge deck type on the stability of a bus model, the aerodynamic  
372 coefficients of bus were obtained in three types of bridge deck section, as it was indicated in  
373 Section 2.1. Fig. 9 illustrates the aerodynamic coefficients acting on the bus located on the three  
374 bridge decks considered for four yaw angle values:  $75^\circ$ ,  $90^\circ$ ,  $105^\circ$  and  $120^\circ$ . In order to obtain the  
375 aerodynamic coefficients for each value of yaw angle, the bus and the bridge deck were rotated  
376 together. While the side and the rollover coefficients approach the highest values for a yaw angle  
377 of  $90^\circ$ , the lift coefficient approach the lowest values. The side and the rollover coefficients show  
378 a similar trend with respect to the yaw angle due to the stronger influence above the rollover  
379 moment by the side force than the lift force. However, the lift coefficient exhibits an opposing  
380 behavior to the other coefficients as in Dorigatti et al. (2012). The side and rollover coefficients  
381 diminish when the yaw angle moves away from the perpendicular to the traffic direction and the  
382 lift coefficient increases. Moreover, the differences between aerodynamic coefficients for the  
383 three type of bridge decks are quite small but, the board type seems to influence more negatively  
384 the bus stability than the other decks for most of the yaw angle values. A sample of numerical  
385 results relative to static pressure and wind velocity in the air region around of bus for a yaw angle  
386 of  $90^\circ$ , is illustrated in Fig. 10. These results indicate that there are not great differences between  
387 the bridge decks with respect to the air flow velocity around the bus, as Fig. 10 shows. However,  
388 it is interesting to stress that the bus stability could be improved if the bridge deck model caused

389 a higher perturbation on the air flow hitting on the bus. The stronger gradients of pressure and  
 390 velocity at the air region below the bridge decks (Fig. 10) are caused by the girder and box types,  
 391 and these are the bridge decks where higher values of rollover coefficient are obtained.



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**Fig 9** Relationships between the aerodynamic coefficients, obtained by CFD code and Dorigatti et al. (2012), and the yaw angle for different bridge decks. (a) Side force; (b) Lift force; (c) Rollover moment.



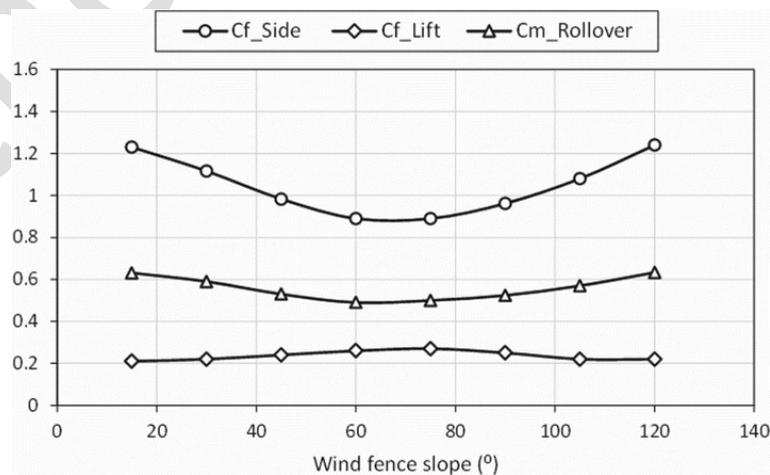
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**Fig 10** Pressure and wind velocity contours calculated for the three types of bridge deck with a yaw angle of 90°.

## 401 6.2. Influence of wind fence slope

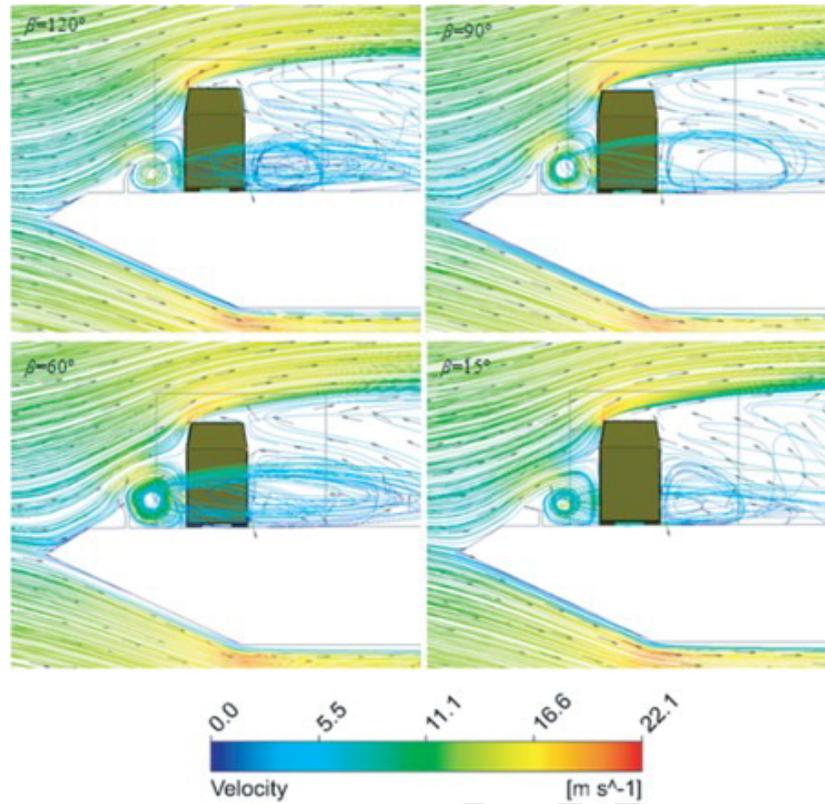
402 In this section, the relationships between the wind fence slope ( $\beta$  angle) and the aerodynamic  
 403 coefficients of the bus are studied under crosswind conditions (yaw angle of 90°). The most  
 404 important parameter with respect to cross-wind stability is the rollover moment coefficient  
 405 (Schober, Weise, Orellano, Deeg & Wetzel, 2010), therefore the wind fence performance was

406 evaluated through the reduction of this coefficient. Similar behaviour is exhibited in the side force  
407 coefficient and the rollover moment coefficient versus the wind fence slopes (Fig. 11), where two  
408 regions can be distinguished. In the first region, both coefficients decrease from a wind fence  
409 slope of 15° to 60°, where the minimum values are reached and keep quite constant until 75°,  
410 where coefficients begin to increase. The lift coefficient exhibits an opposite trend with respect  
411 to the rollover and side coefficients where the maximum value of lift coefficient is approached  
412 for a wind fence slope of 75° (Fig. 11). Among the slope angles of wind fence studied, 60°  
413 highlights as the position where the minimum value of rollover coefficient is obtained. For this  
414 slope angle value, a lower number of streamlines hit on the top zone of the windward surface of  
415 the bus in comparison with other values of wind fence slope, which result in a reduction of the  
416 rollover coefficient of the bus (Fig. 12). Specifically, this articulating wind fence reduces the  
417 rollover coefficient in relation to the crash barrier by a maximum value of 22% (wind fence slope  
418 angle of 60°). While the side coefficient of bus was higher when the crash barrier were installed,  
419 the lift coefficient was lower in comparison with the case of articulating wind fence. This  
420 difference in the lift coefficient is due in part to a lower air flow through the gap between the bus  
421 and the road for the articulating wind fence and, in consequence, the pressure is higher in the air  
422 region under the bus, what rises the difference of pressure between the top and underneath  
423 surfaces of bus.



424

425 **Fig 11** Relationship between aerodynamic coefficients of bus and wind fence slope for the box deck  
426 under cross wind conditions.



427

428 **Fig 12** Streamlines of velocity field around of bus for four values of wind fence slope angle,  $\beta$ .

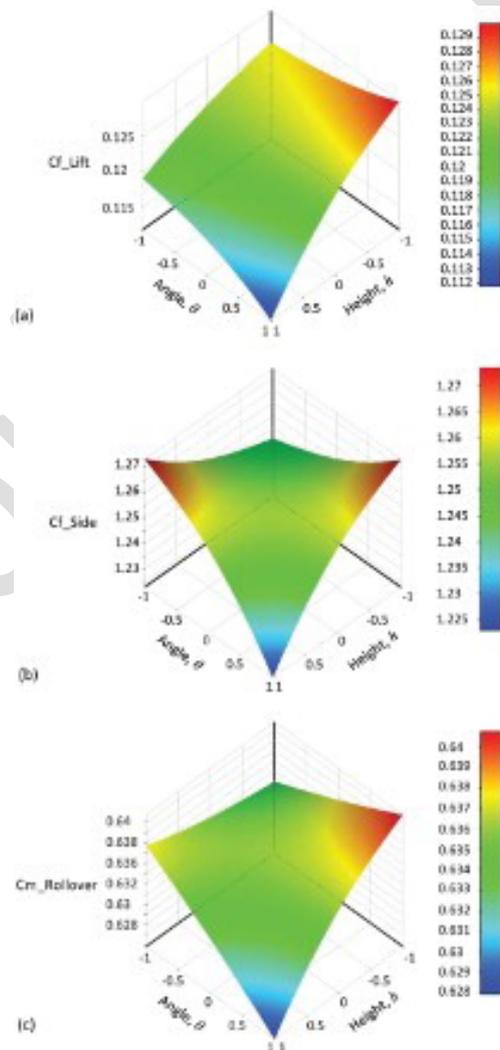
429 **6.3. Configuration of box bridge deck**

430 In this section, the influence of two geometrical parameters of box bridge deck on bus  
 431 aerodynamics was studied by solving 9 numerical models. A converged solution was reached  
 432 when the following requirements were fulfilled: the scaled residuals of all the variables were less  
 433 than  $1 \cdot 10^{-5}$ , the net flux imbalance was less than 1% of the smallest flux through the domain  
 434 boundary and the monitored aerodynamic coefficient keep constant in 4 significant figures  
 435 (ANSYS Inc. 2011). In order to carry out the simulations, a server with a CPU Intel Xeon 5630  
 436 @ 2.53 GHz (8 processors), 64 GB RAM memory, 4 TB hard disk were used and worked under  
 437 the Windows server 2003 operating system was used. The geometry input parameters described  
 438 in Section 4 were coded in three values (-1, 0, 1) by applying this expression (Montgomery, 2013):

$$x_{coded} = \frac{x - (x_{low} + x_{high})/2}{(x_{low} - x_{high})/2} \quad (8)$$

439 The response surface models fitted with the results obtained after solving the cases proposed by  
 440 the design of experiment are plotted in Fig. 13. These graphs show the maximum variation of  
 441 aerodynamic coefficients of the bus caused by the effect of deck box height and deck box angle

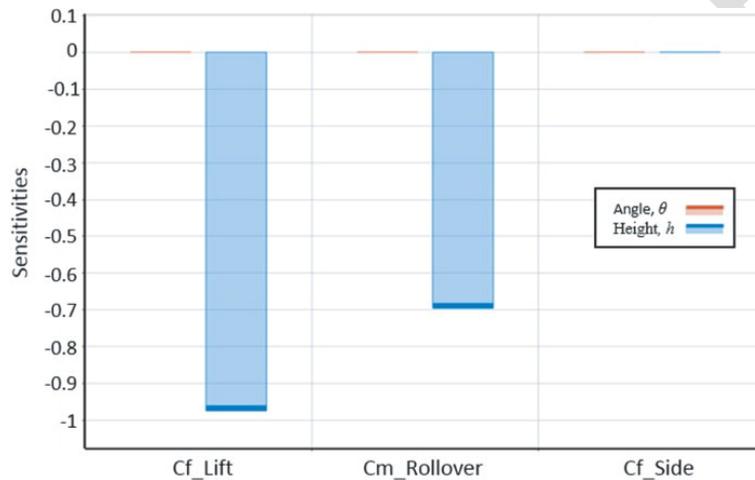
442 within a predetermined range of values. The adjusted coefficients of determination,  $R^2_{adj}$ , related  
443 to the response surface models are: 0.79 for the lift coefficient, 0.76 for the side coefficient and  
444 0.69 for the rollover coefficient. Among the cases solved, the best configuration of box deck will  
445 be the one for which the minimum coefficient of rollover is reached. Specifically, a minimum  
446 value of 0.628 for the rollover coefficient is obtained for a box angle of  $45^\circ$  (+1 coded value) and  
447 a height of 92.5 mm (+1 coded value) as it is shown in the Fig 13. However, the influence of this  
448 parameters on both the rollover coefficient and side coefficient is quiet modest because the  
449 response variation with respect to the average value is below 5%. In the case of lift coefficient, it  
450 reaches a maximum variation of 16% but its influence on the rollover coefficient is quite smaller  
451 than the side coefficient.



452  
453 **Fig 13** Response surfaces relating the geometrical parameters of a box deck (box angle and box height)  
454 with the following aerodynamic coefficients: lift force (a), side force (b) and rollover moment (c).

455 In addition, a sensitivity study was carried out for independent assessment of this geometrical  
456 parameter on the aerodynamic coefficient acting on the bus. The results indicate that the height  
457 of box significantly influences both the rollover coefficient and the lift coefficient while, the angle  
458 of box is not correlated with any aerodynamic coefficient (Fig. 14). The effect of height parameter  
459 above the rollover coefficient is due to the negative value of sensitivity between this parameter  
460 and the lift coefficient, because the side coefficient is not affected by the height of box. To sum  
461 up, the risk of rollover accident does not strongly depends on this geometry parameters of the box  
462 deck.

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**Fig 14** Global sensitivity values between the aerodynamic coefficients of the bus and the geometrical parameters of a box deck.

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## 7. Conclusions

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In this work, a methodology is developed to help distinguish scenarios on roads where crosswind conditions are more negative for traffic safety. The competent authorities will be able to use this information to decide, with more precise criteria, on issues such as: in which infrastructures it is most necessary to install a wind fence or when traffic must be closed on bridges due to strong crosswind. In addition, a new approach which consists in improving the traffic safety by modifying the structural configuration of bridge decks, was studied.

476

The main remarks from the quantitative results can be summarized as follows:

- 477 • Of the three types of bridge deck tested, the board type slightly influences more negatively  
478 bus stability than the other decks in the yaw angle range studied ( $75^\circ - 120^\circ$ ).
- 479 • The effect of wind fence slope angle on the aerodynamic coefficients of the bus was studied  
480 and, the results exhibits that the minimum value of rollover moment coefficient was obtained  
481 for an angle of  $60^\circ$  with respect to the horizontal plane.
- 482 • The articulating wind fence reveals as a better option to protect the vehicles against cross  
483 wind conditions than the crash barriers. Specifically, this wind fence model reduces the  
484 rollover coefficient in relation to the crash barrier by a maximum value of 22%.
- 485 • The rollover coefficient acting on the bus exhibits variations below 5% for the two geometry  
486 parameters of box bridge deck studied; therefore, it can be stated that the risk of having  
487 rollover accidents does not strongly depend on these parameters.
- 488 • As regards numerical setup, the best fit to experimental data was obtained by using the SST  
489  $k - \omega$  turbulence model.
- 490 • The finite volume method has proved to be a powerful tool for solving the Reynolds averaged  
491 Navier–Stokes (RANS) equations along with the SST  $k - \omega$  turbulence model.
- 492 • In the case of the box bridge deck case, the unsteady approach has shown to be more accurate  
493 than the steady approach. However, the trends in the result graphs are quiet similar for both  
494 approaches.
- 495 • In order to carry out a more detailed study of the unsteady behavior of the fluids around the  
496 bus, it might be interesting to apply other more accurate approaches with higher  
497 computational cost such as Large Eddy Simulation (LES), Detached Eddy Simulation (DES)  
498 or Scale Adaptive Simulation (SAS).

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